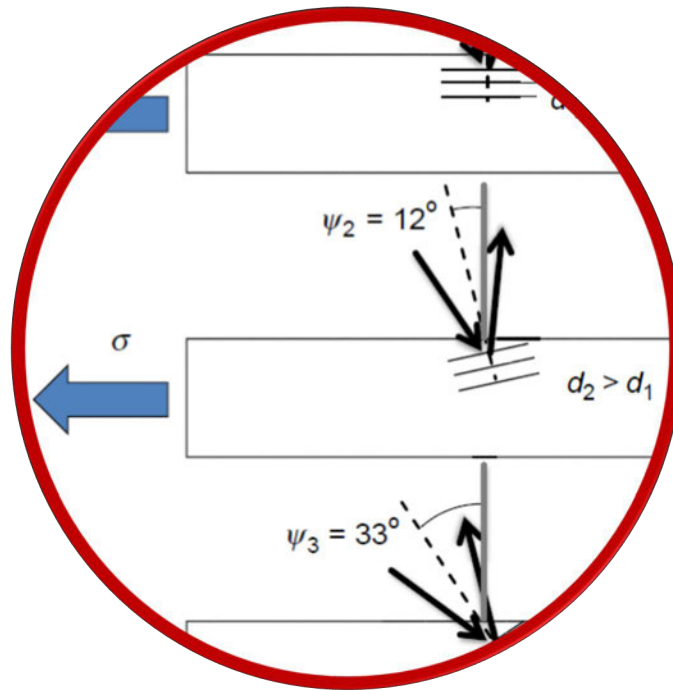


Disclaimer

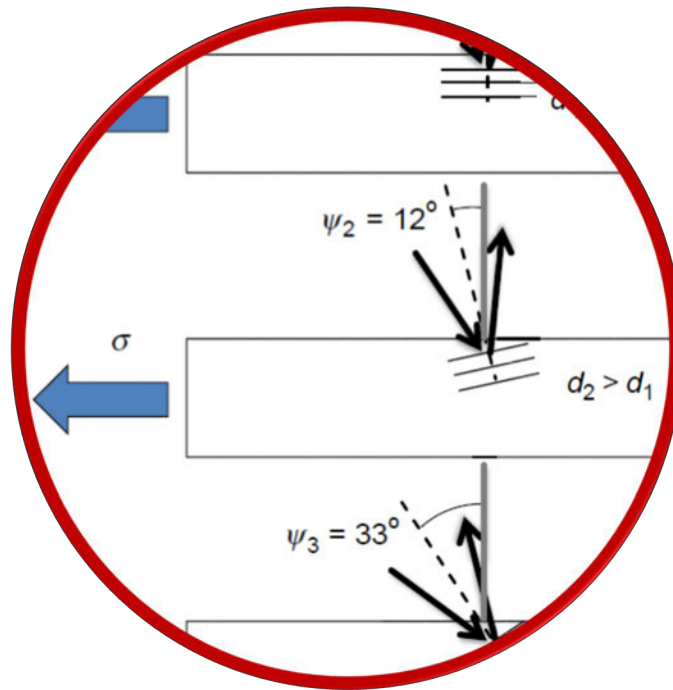
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Ch. 6: Small Scale Mechanical Testing



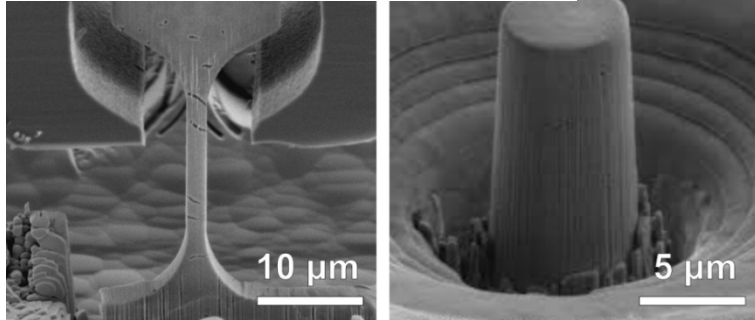
Sample fabrication techniques



Focused ion beam

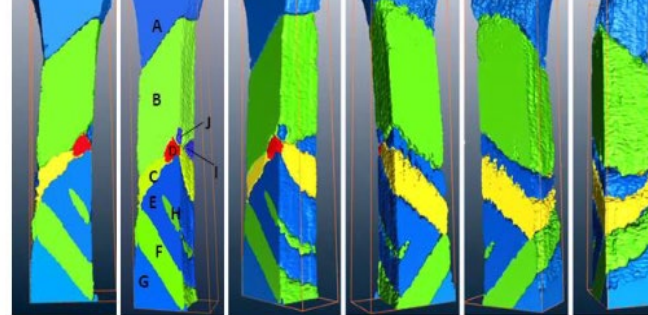
FIB applications examples

Micromechanical specimen fabrication



Casari et al., *Acta. Biomater.*, **120** (2021) Schwiedrzik et al., *Nat. Mat.*, **13** (2014)

FIB tomography + HR-EBSD



Della Ventura et al., *Mater. Des.*, **197** (2014)

3D nano structuring

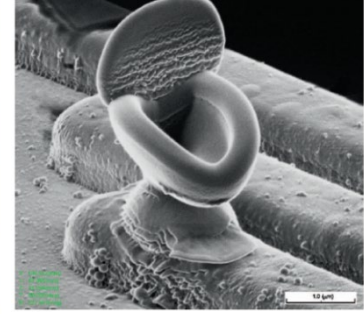
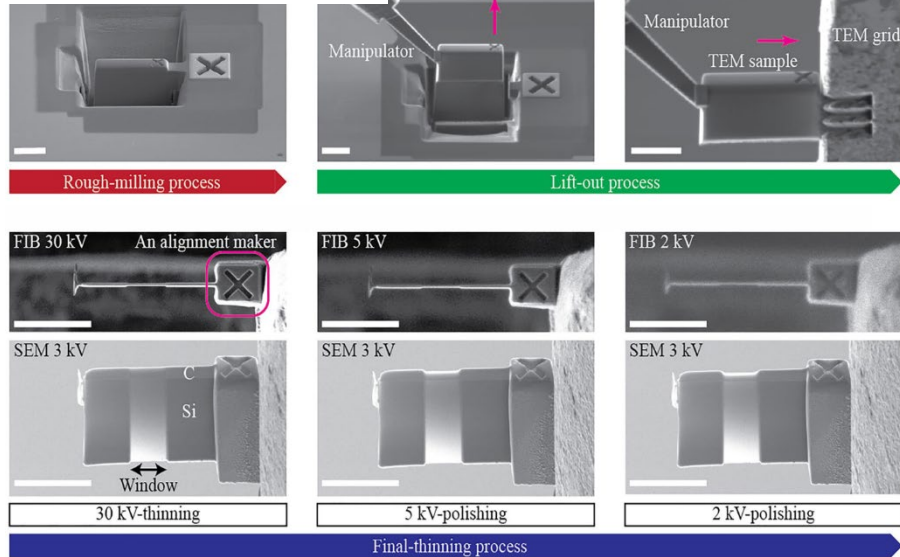


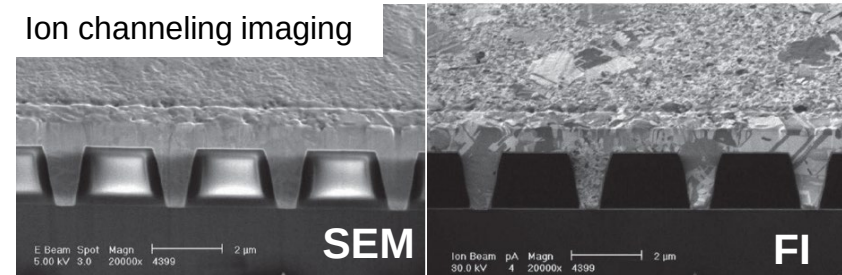
Image from Seiko instruments

TEM lamella preparation

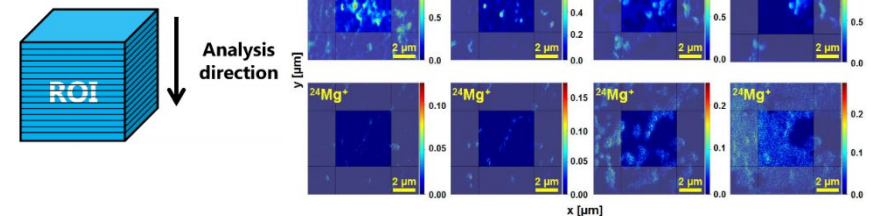


Tsurusawa et al., *Sci. Rep.*, **11** (2014)

Ion channeling imaging



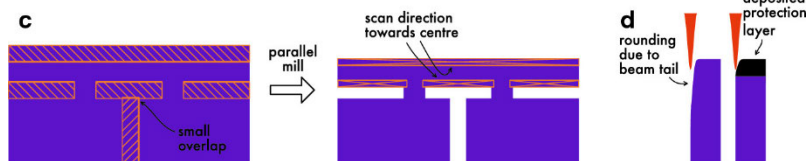
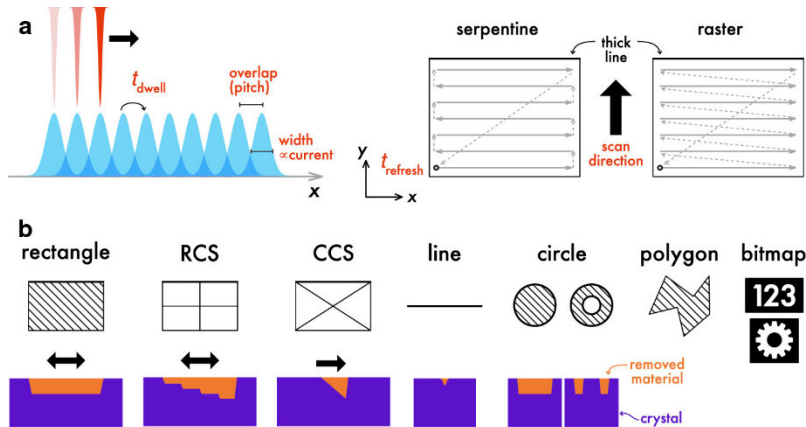
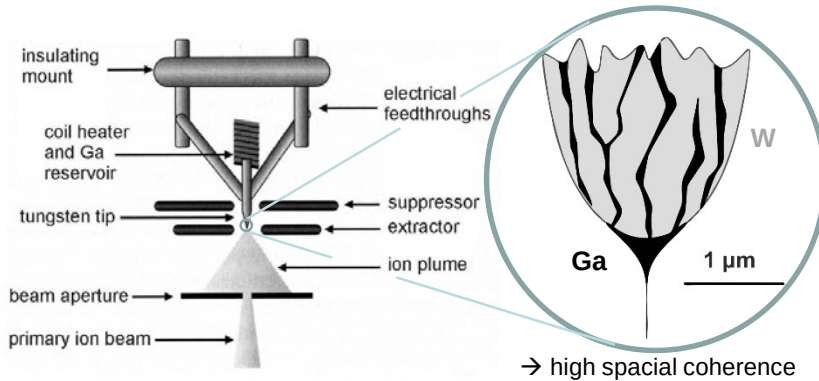
TOF-SIMS



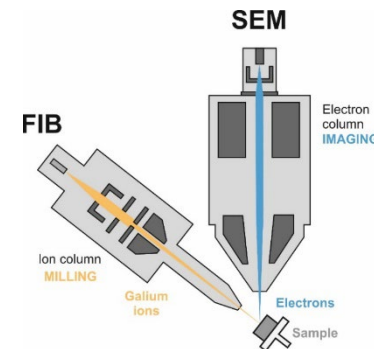
Priebe et al. EUFN Workshop poster (2018)

A quick overview on FIB

Schematic of a liquid-metal ion source (LMIS)

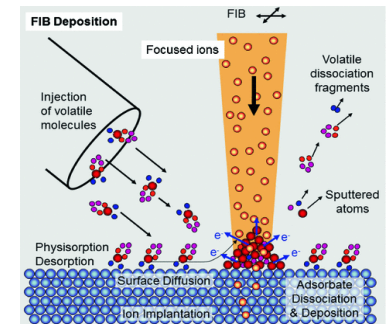
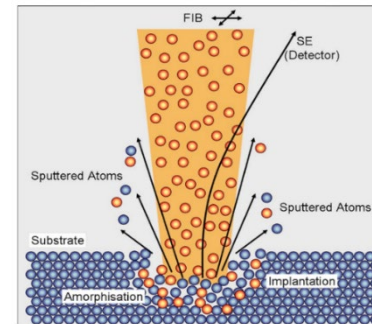
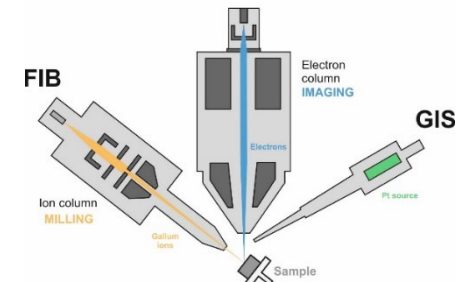


Standard milling



Gas induced deposition & etching

e.g. Pt, C, W e.g. Cl_2 , XeF_2



Utke et al., *J. Vac. Sci. Technol. B* 26 (2008)

Parameters we can control

- Dwell time
- Dose
- Spacing
- Beam irradiation path

Different FIB types and ion sources

Liquid metal ion source (LMIS)

Bassim et al., *MRS Bulletin* (2014)

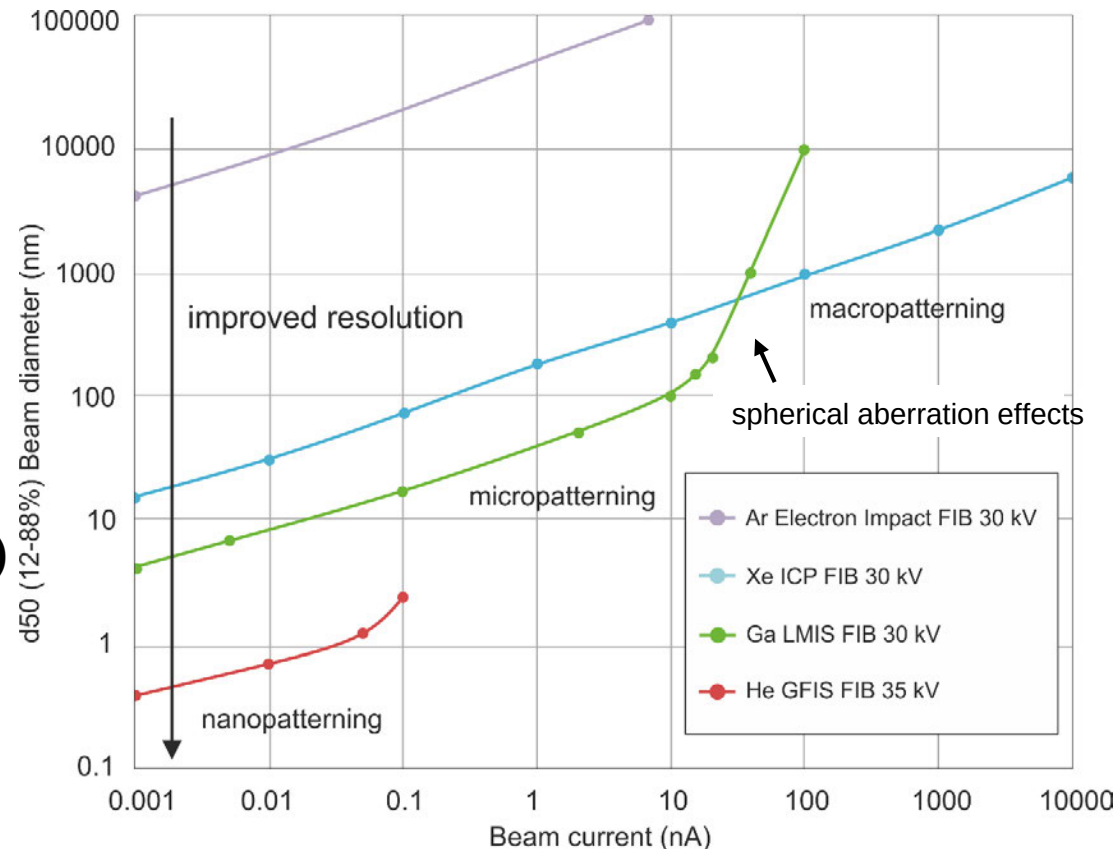
- Typically Ga
 - High stability
 - Alloy sources: Au, Bi, Si,
- Current range: 1 pA - 100 nA

Inductively coupled plasma (ICP)

- Typically Xe
- Current range: 100 pA – 1 μ A

Gas field ionization source (GFIS)

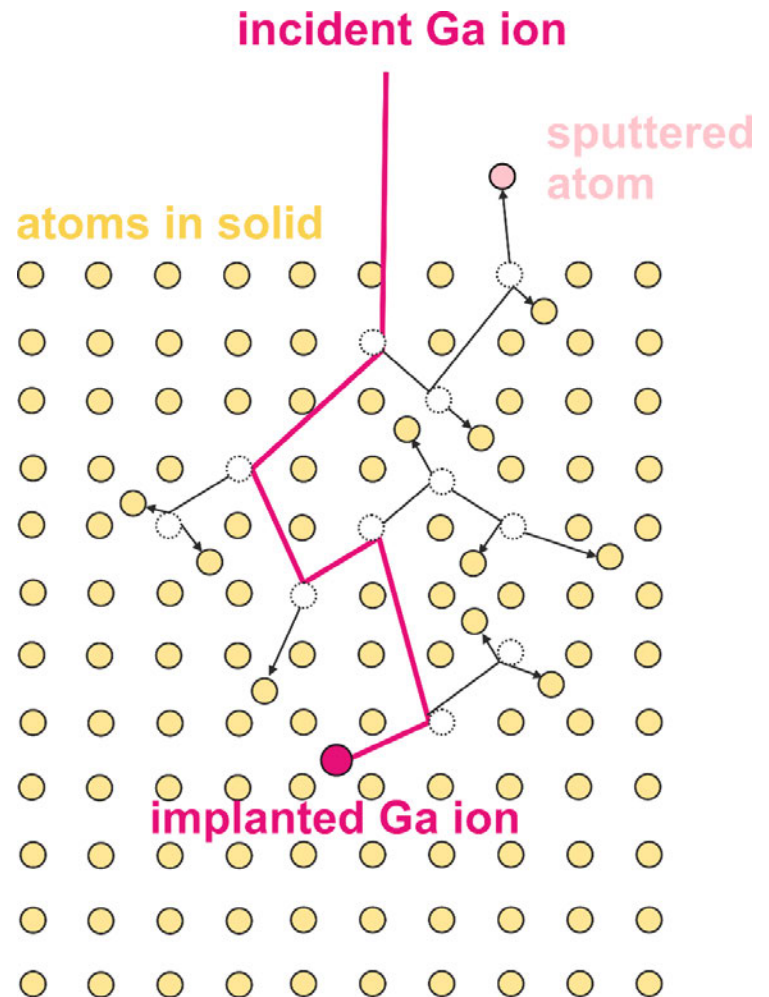
- Typically He or Ne
- High spatial resolution (<0.35 nm)
- Imaging insulating samples
- Current range: 0.1 pA – 100 pA



Collision cascade model

Ion-solid interaction

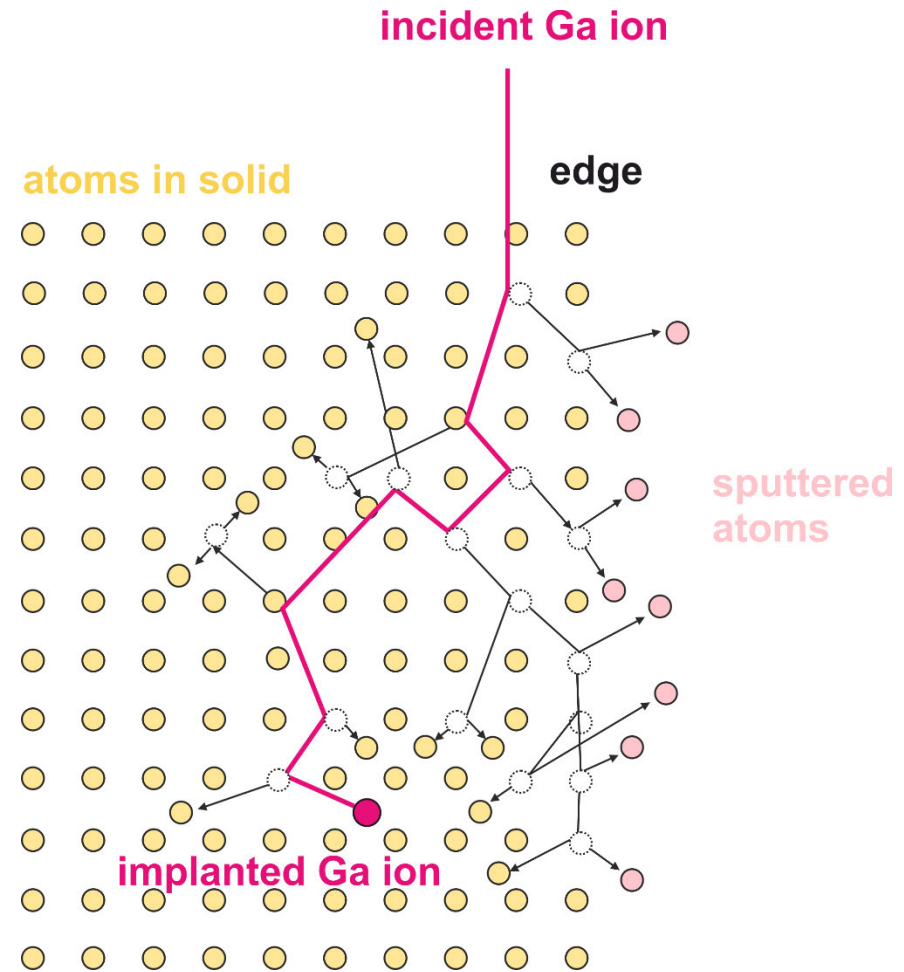
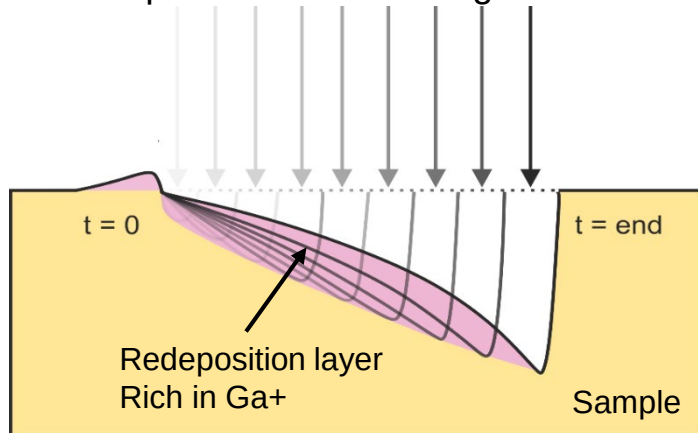
- Surface atoms can be ejected (sputtering /milling)
- Ca. 30 ps process
- Relaxation after first ca. 10 ps
- Implanted ions
- Amorphization
- Electrical damage zone
- 30 kV Ga⁺ on Si: ca. 30 nm
- Different possible sources: Ga, Xe, H, etc...



Milling at an edge

Edge effect

- Increased sputter yield (ca. 8x)
- Topographic effect (corner will mill even faster)
- Scan strategy matters
- Line-by-line milling is efficient
- Redeposition becomes significant



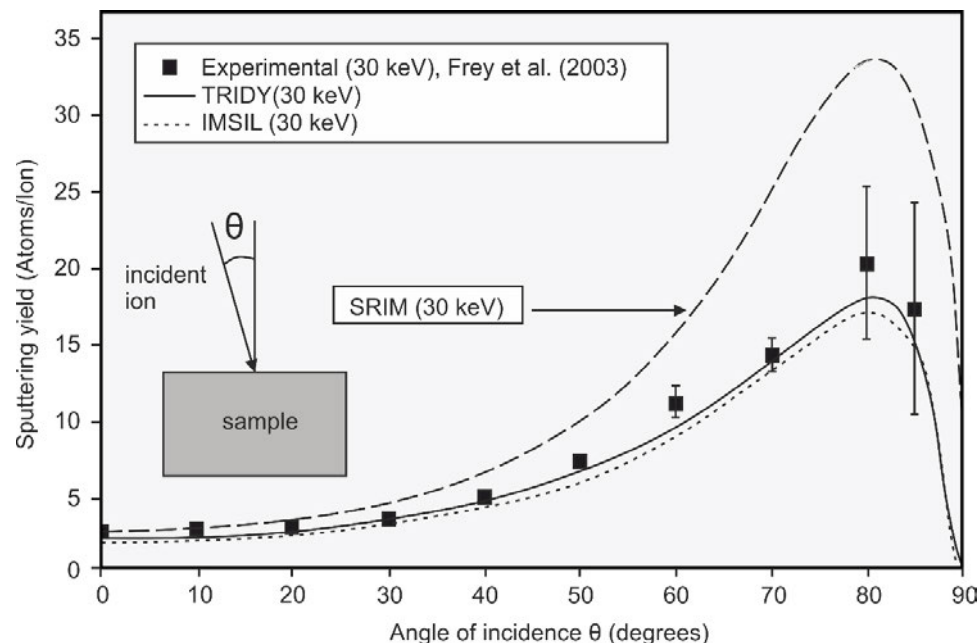
Tangential irradiation: increased sputtering rate

Sputter yield and sputter rate

Sputtering by 30 kV Ga⁺ normal incidence

Element	Sputter yield* Y (-)	Sputter rate** S ($\mu\text{m}^3/\text{nC}$)
C	1.69	0.18
Al	3.47	0.29
Si	2.78	0.24
Ti	2.28	0.46
Cr	5.15	0.10
Au	15.75	1.50
W	7.59	0.12

Max efficiency for an incident angle of 75-80°

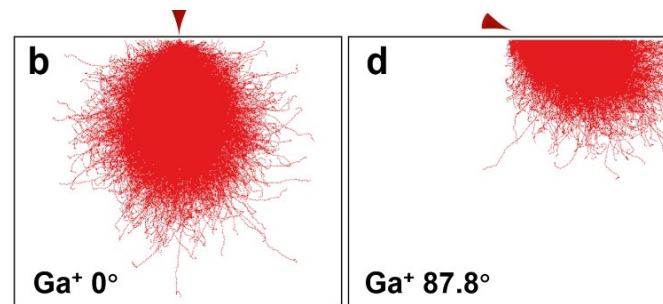


Sputtering yield Y : atoms sputtered per incoming ion

Sputtering rate S : volume removed per dose

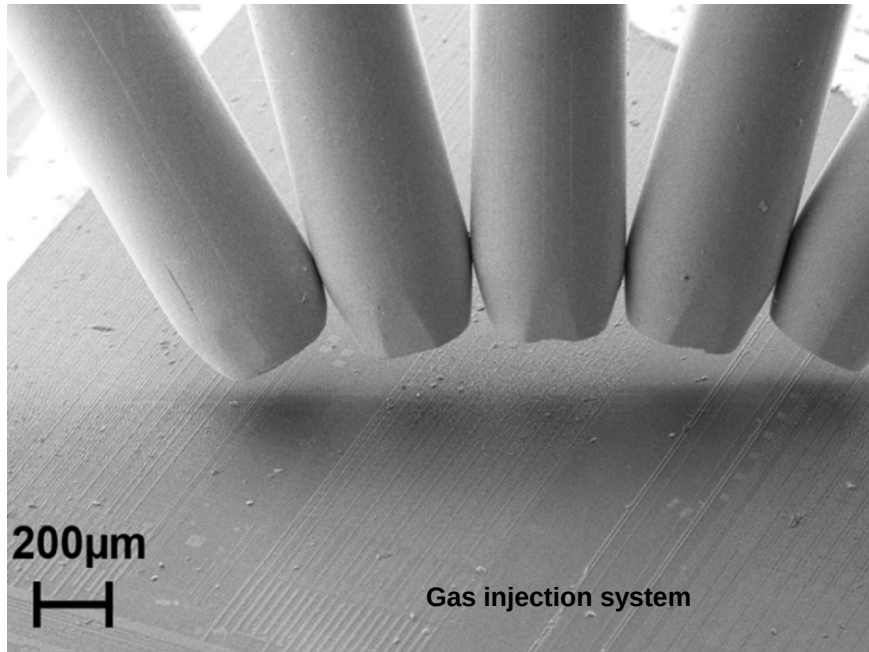
* SRIM data from: , Lucille A. Giannuzzi and Fred A. Stevie, Introduction to focused ion beams, Springer, 2005.

** Ivo Utke, Stanislav Moshkalev, Phillipp Russell, Nanofabrication using focused ion and electron beams, Oxford University Press, 2012.



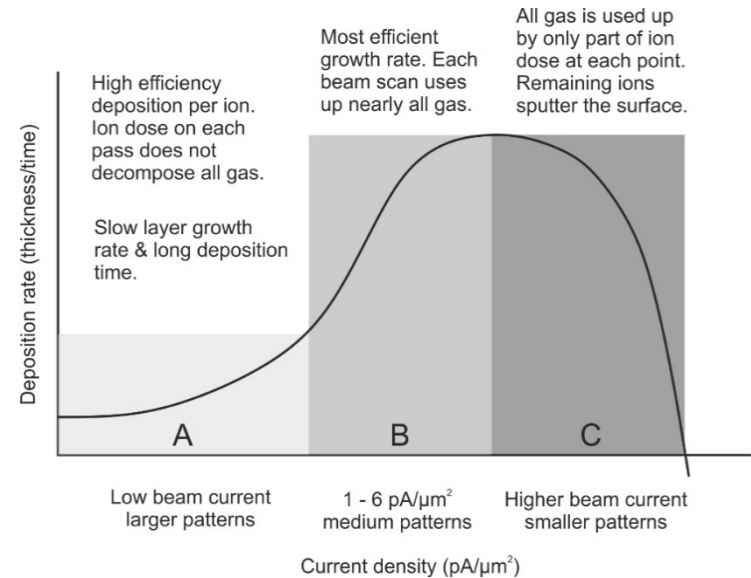
Liu et al., *Sci. Rep.*, **10** (2020)

Deposition induced by FIB



Deposited species is not pure: lots of Ga and C

Deposition without surface damage only by eBeam dep

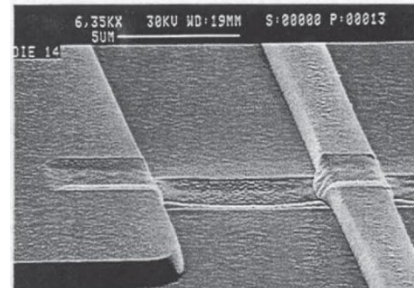


Good parameters for Ga⁺ ion Pt deposition

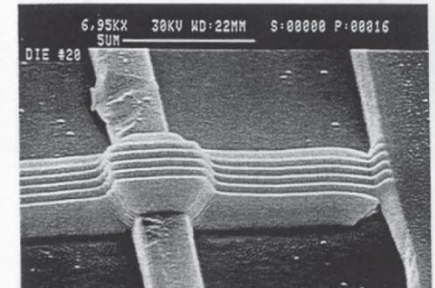
- Ion probe current = Area * 5 pA/µm² (i-dep)
- Pixel fill factor = 40 - 70 %
- Short dwell time (0.2 µs for Pt)

Good parameters for e- Pt deposition

- Electron probe current 2000 pA @ 5 kV (e-dep)



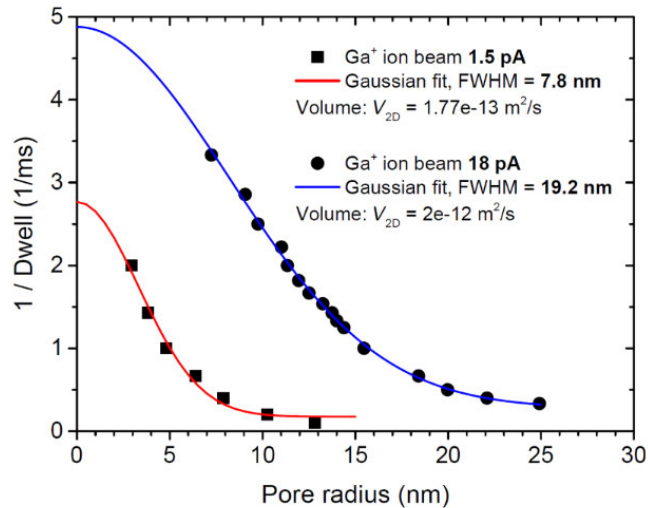
Bad parameters



Good parameters

Beam profile

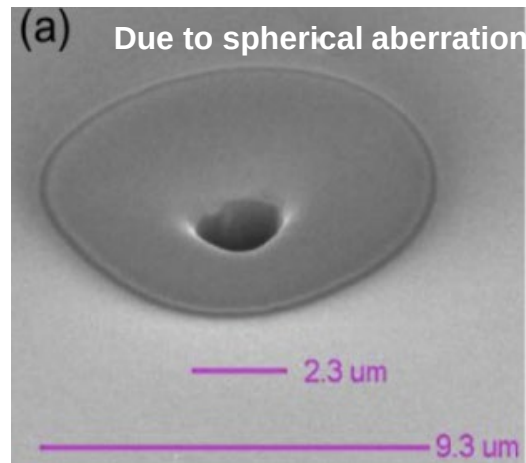
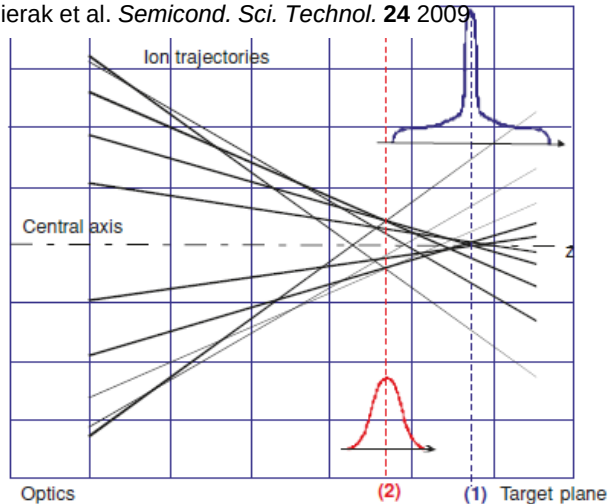
Shorubalko et al., *J. Nanotechnol.* **8** (2017)



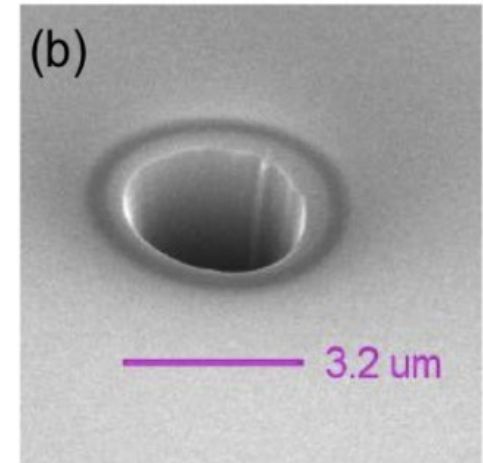
Beam traces

- Electromagnetic lenses $\rightarrow$ high current $\rightarrow$ **spherical aberration**
- Rounding of the milled edges
- Circle of less confusion at high currents lead to a better result than Gauss optimum

Gierak et al. *Semicond. Sci. Technol.* **24** 2009



27 nA no defocus

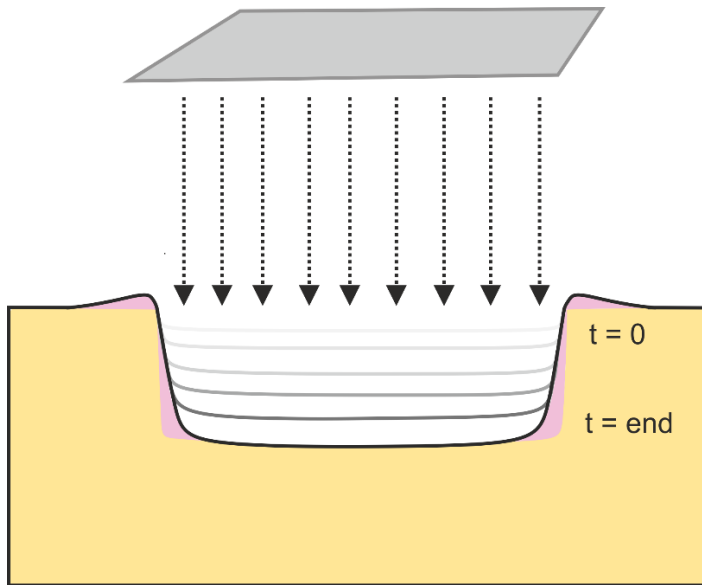


27 nA defocus

Two main milling strategies

Layer-by-layer

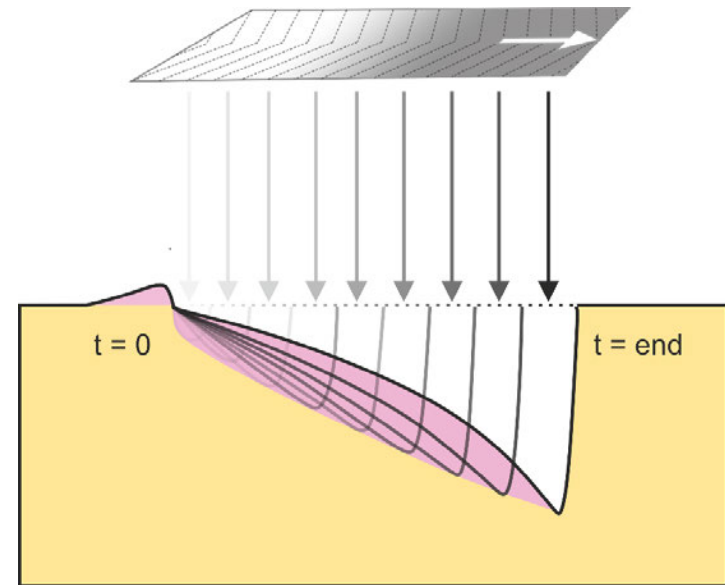
- Form a parallel floor
- Imaging
- Delayering
- Low redeposition but much slower



Layer-by-layer cut

Line-by-line (polishing)

- Tilted floor: shallow to deep
- Used for cutting (cross sections /polishing)
- Fast removal of large volumes
- Redeposition on floor and sides



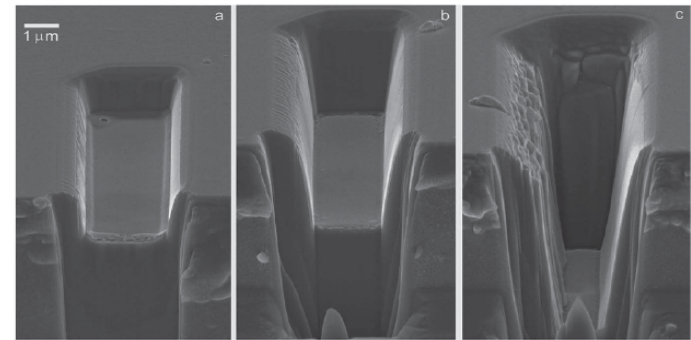
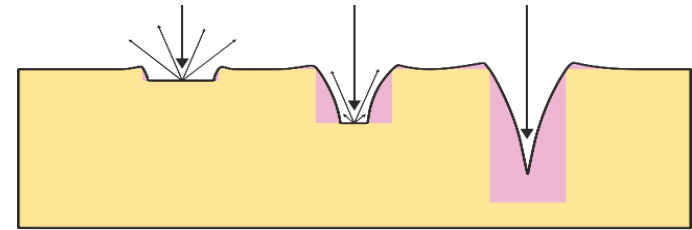
Line-by-cut (polishing)

Aspect ratio and tapering

Redeposition limits the milling aspect ratio

When the rate of redeposition equals the rate of sputtering: dynamic equilibrium (V-shaped trench).

- Generally maximum aspect ratio holes $\sim 5:1$
- Can be improved to $\sim 10:1$ with gas enhanced etching
- For small holes with size below 100 nm maximum aspect ratio of 1:1.

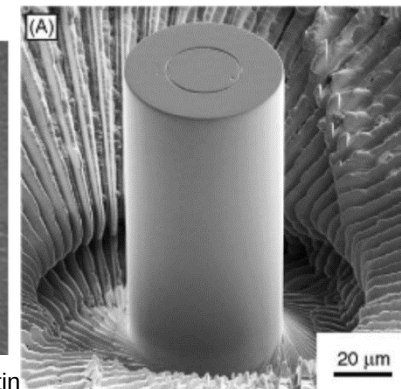
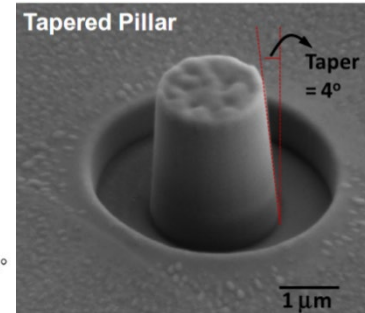
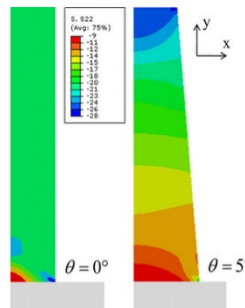


(100) Si milled at normal incidence by applying: (a) single fluence, (b) double fluence, and (c) triple fluence of Ga⁺ ions at 25 keV.

Sidewall tapering

- Material dependent
- Typical values $\sim 1-4^\circ$
- Some extreme cases e.g. Zn $\sim 14^\circ$

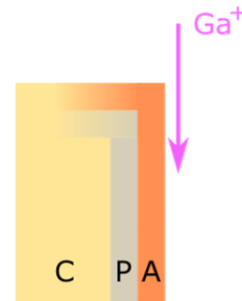
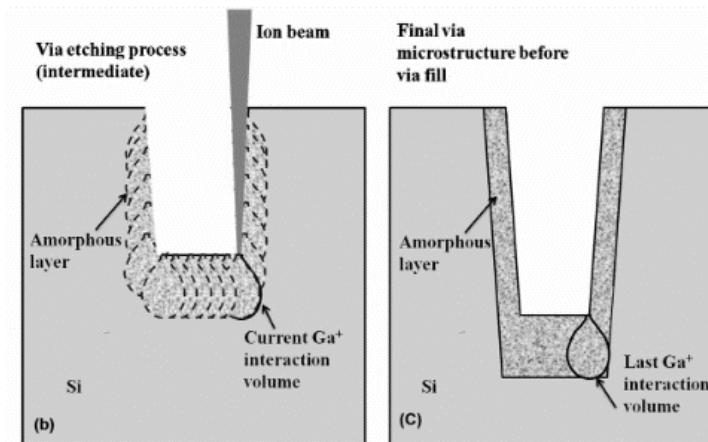
Fei et al. *J. Appl. Mech.*, **79** (2012)



Inhomogeneous axial stress during micromechanical testing

Solution: overtilt to compensate (if possible)

Amorphization layer



Reducing the amorphous layer

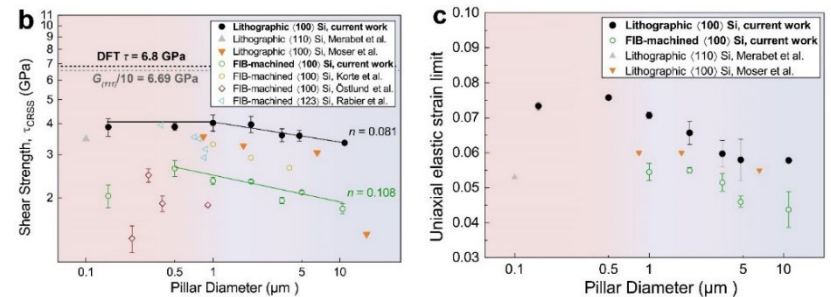
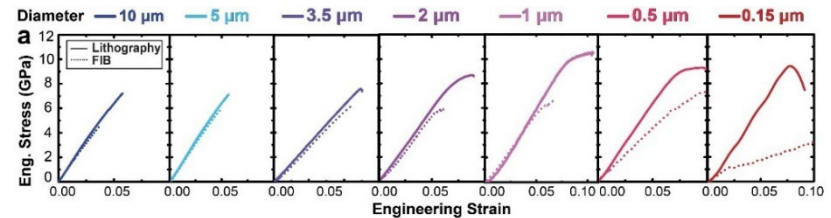
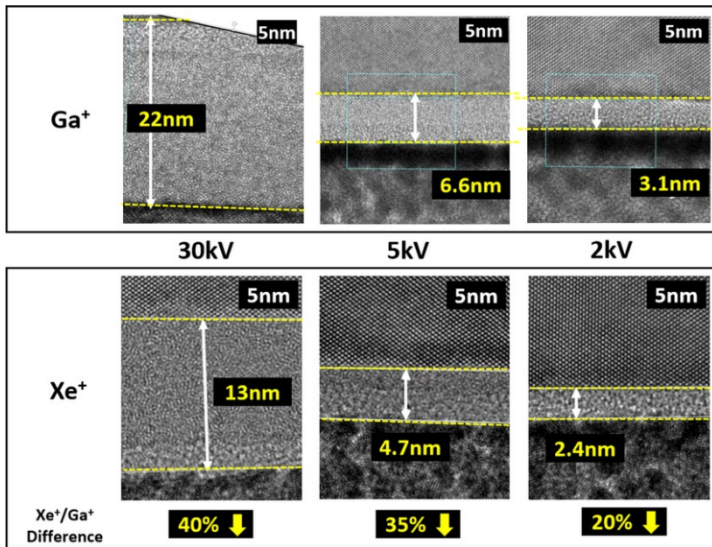
Low kV milling

- Larger ion
- Lower angles

Damage zones in a crystalline solid C

A = amorphized

P = point defects

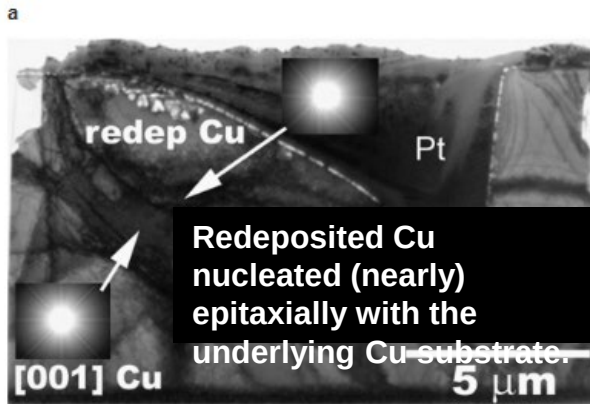
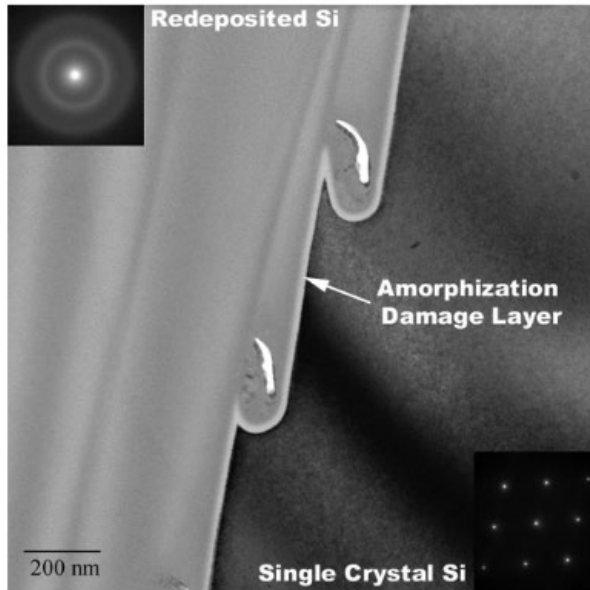


Does FIB induced damage influence the material behavior?
Something to keep in mind...

Burnett et al., *Ultramicroscopy* **161** (2016):

Amorphization on EBSD imaging

Matteson et al. *J. Electron. Mater.* 31 (2002)



Amorphous layer thickness

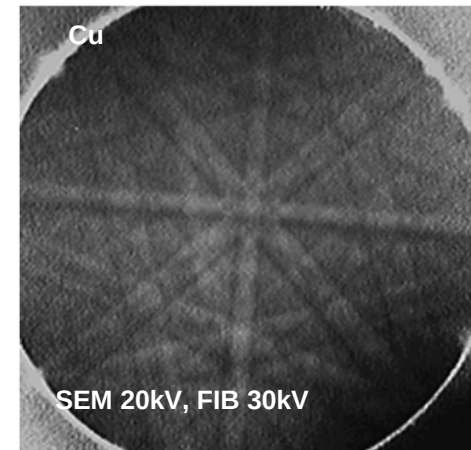
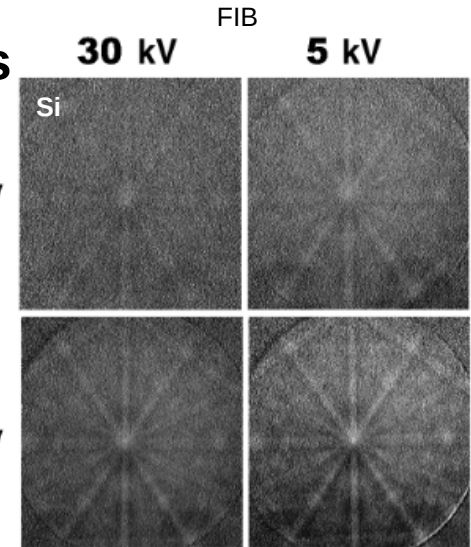
- ion energy (low kV: **thin layer**)
- angle of incidence (tan: **small**)
- ion species
- target material

Metastable phase

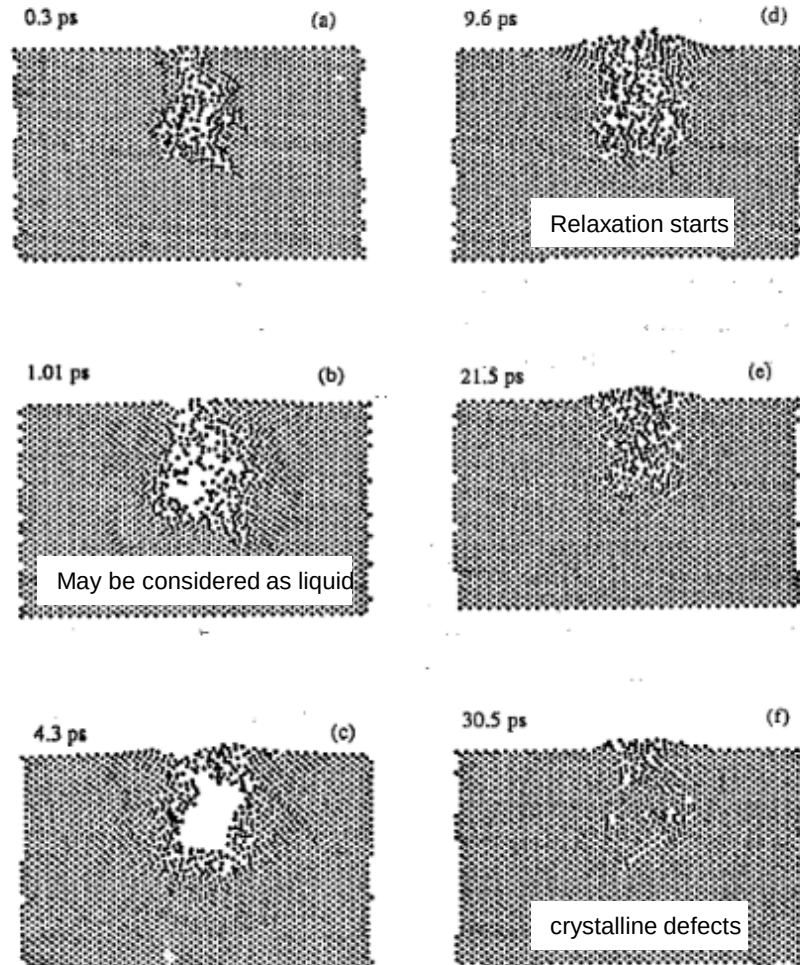
Formation depends on complexity and size of the unit cell

Not always amorphous?

Small unit-celled, as well as broad phase field materials are more difficult to amorphize.

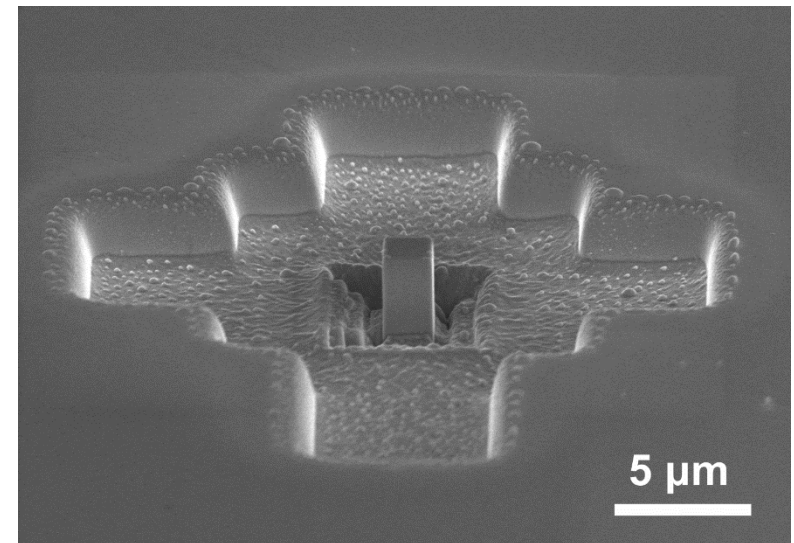


Local heating



MD simulation Au particle 10 keV on a (100) Au surface
Averback and Ghaly, *J. Appl. Phys.* 76 (1994)

- Heating **restricted** to the region defined by the **collision cascade** (a few tens of nm)
- If low dwell time < 5 μ s $\rightarrow$ most likely negligible for most materials.
- Be aware of polymers and low melting point materials (e.g. GaAs bleeding $\rightarrow$ reduce current)



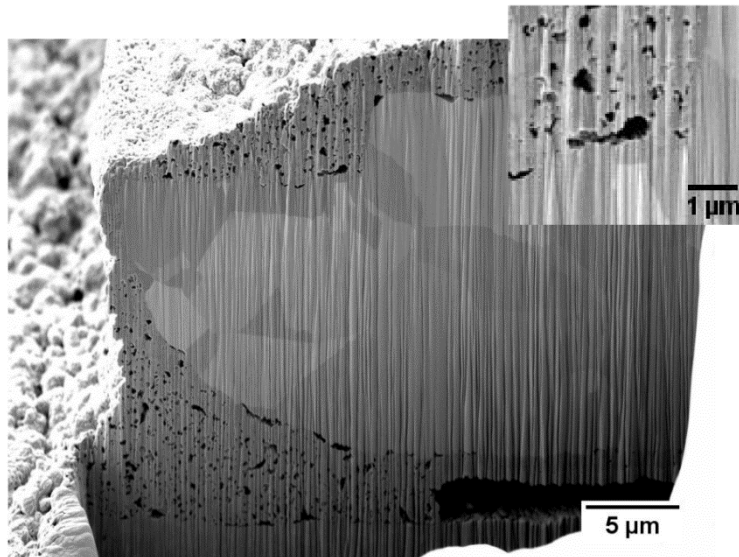
GaAs micropillar showing signs of bleeding due to local heating during milling

Curtaining

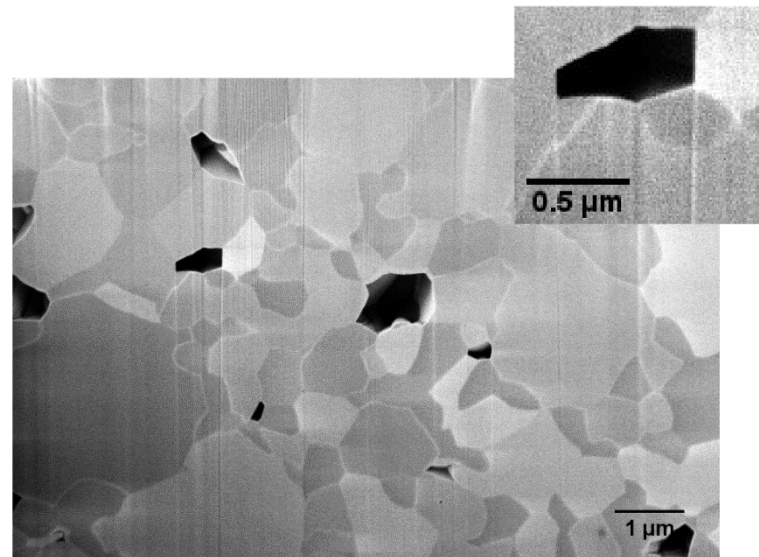
Curtaining (aka waterfall effect)

Milled face shows lines (more / less material was removed)
Irregular non flat surface: bad for quantitative image analysis

- Porous materials
- Rough surfaces
- Height steps (e.g. gates in semiconductors)
- Composites of hard and soft material
- Low kV milling



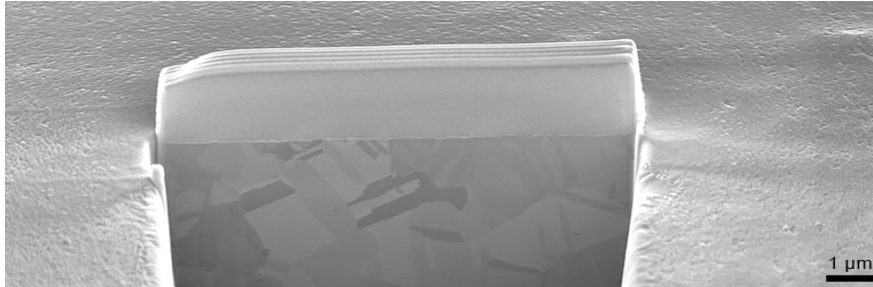
Porous ceramic on Ni: strong curtaining due to rough surface



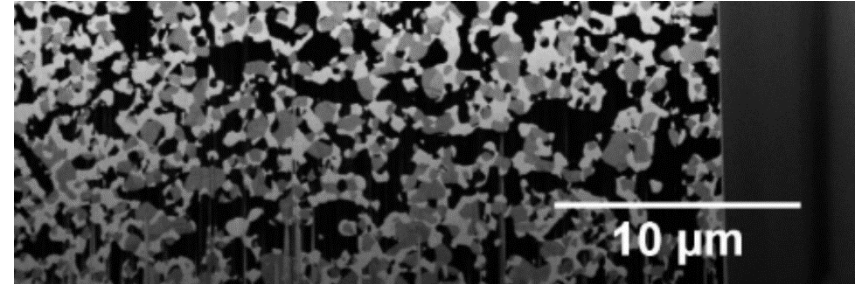
Porous cermet: mild curtaining due to pores

Curtaining is created by **spatial variation of the sputter rate** of the sample and **the modulation of the current density by forward scattering of the ions**.

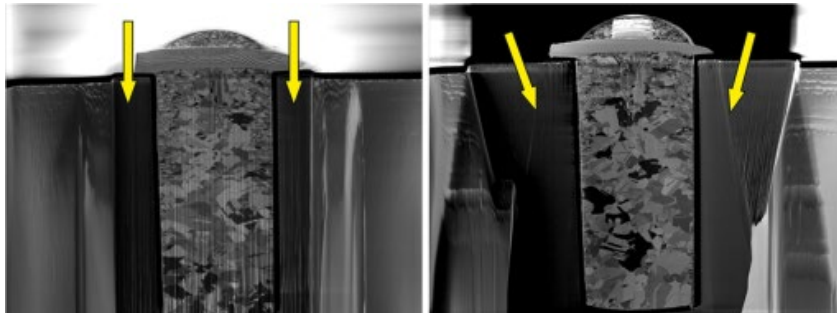
How to reduce curtaining?



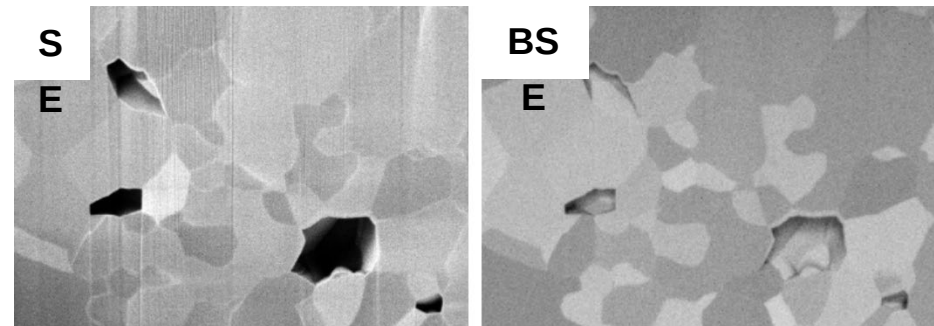
Thick protection layer



Resin infiltration



Rocking stage, sample rocking



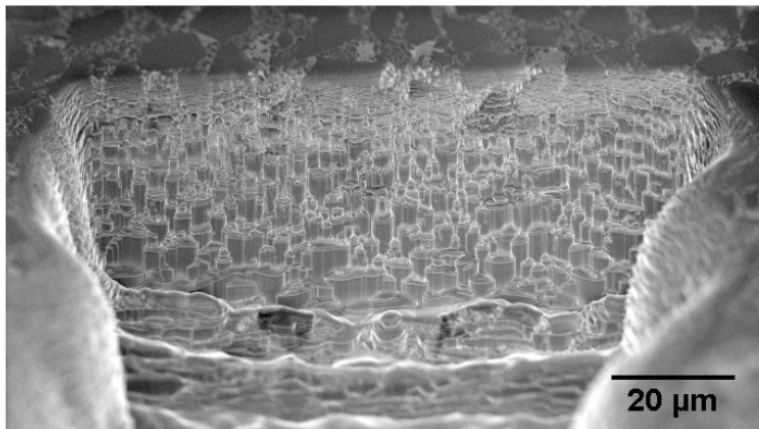
Hide it: BSE signal or post processing

1. Thick and dense FIB-deposited protective layer (W or Pt)
2. Stage rocking/tilting the specimen in the image axis
3. Increase the minimum dose
4. Resin infiltration
5. Backscattered electrons
6. Postprocessing

Rippling and how to avoid it?

Ion rippling

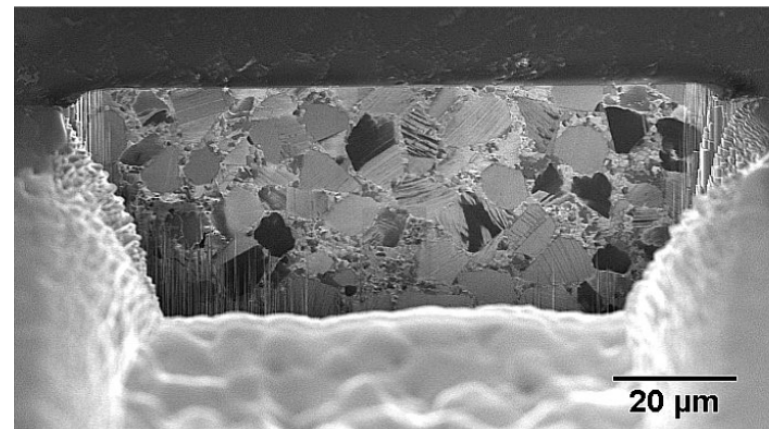
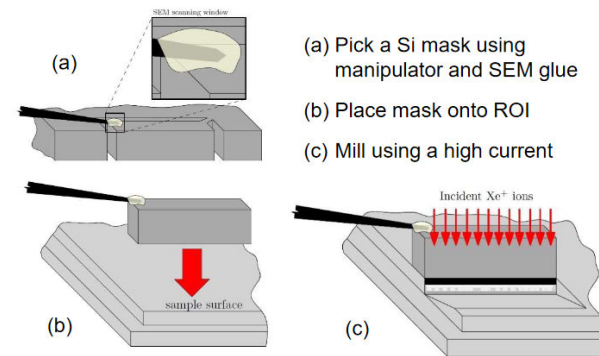
- Self organization
- Instability of process
- Material dependent
(silicate rocks are bad Al and Si are fine)
- Ion dependent (size of ion vs atoms in solid)
- Current density dependent
- Mostly see it in Xe PFIB



Massive ion rippling in SiC sample, microstructure completely obscured.

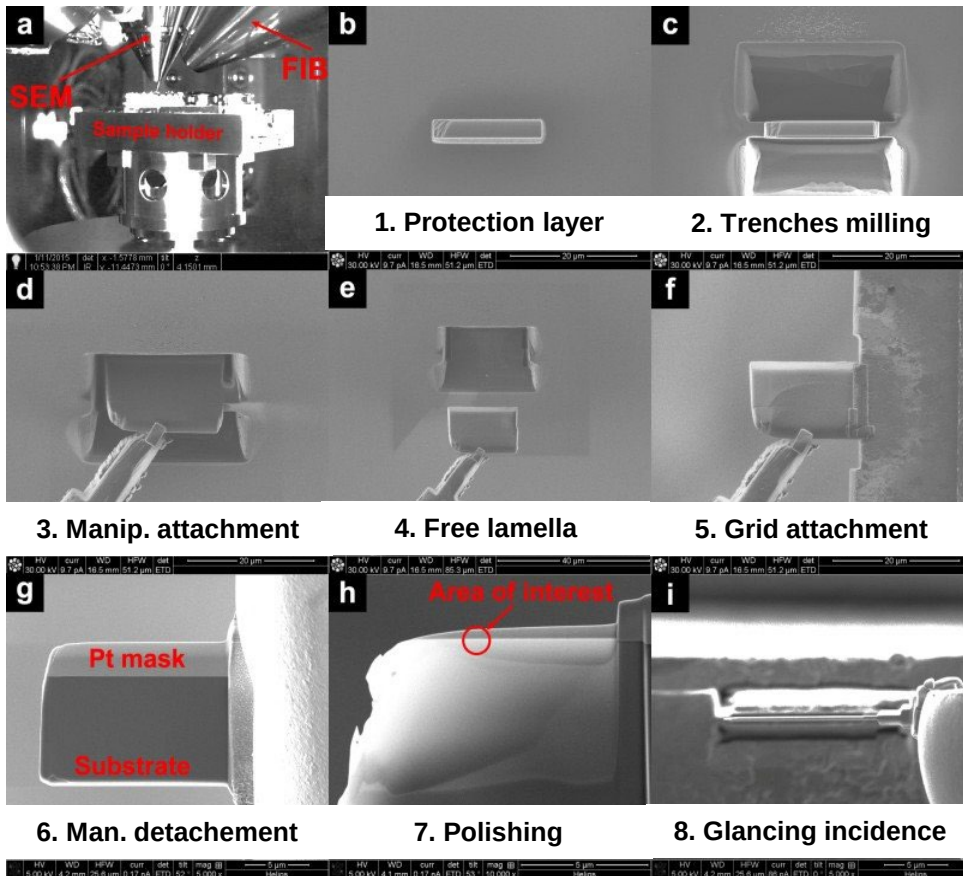
Solution

- Thick protection cap will help
- However masking works best



Cross section polished using Si mask, microstructure clearly visible.

Examples of TEM lamella prep.



Trenches milling

Mostly work at 30 kV (most materials behave ok)
 Leave a few μm from ROI at high currents (beam traces)
 Sequentially reduce current e.g. 10 nA, 2nA, 200 pA
 2 μm lamella ok to lift-out
 Keep in mind the aspect ratio (tall lamella $\rightarrow$ larger trench)

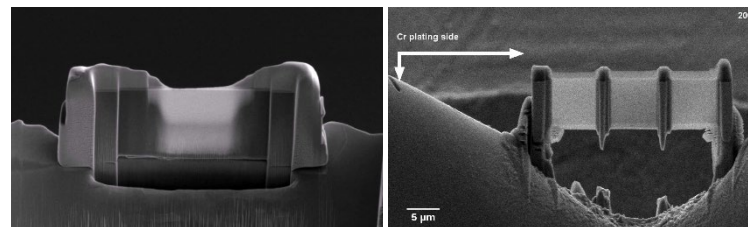
Polishing and thinning

30 kV 1nA (1 μm thickness) $\rightarrow$ 100 pA (100 nm thickness)
 Overtilt to keep the surface parallel (most cases $\pm 2^\circ - 3^\circ$)
 Grazing incidence 2-5 kV +/- 5-7° (1 - 3 min)

Pt. Deposition

First perform e-beam deposition (5 kV, 2000 pA)
 Ion deposition 10-15 kV will be denser
 Thick is good!

- Ion current = Area $\times$ 5 pA/ μm^2
- Pixel fill factor = 40 - 70 %
- Short dwell time (0.2 μs for Pt)

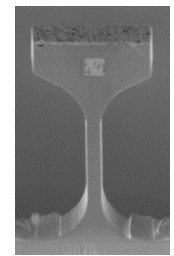
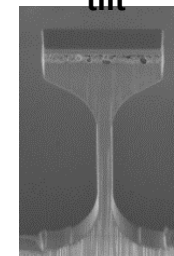
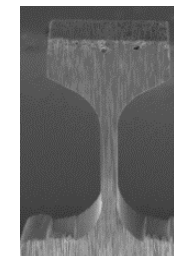
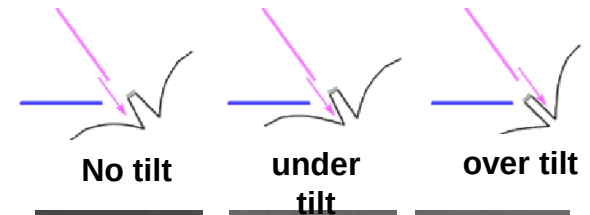
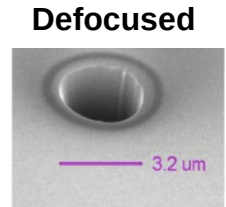
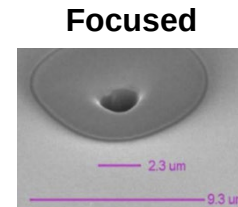
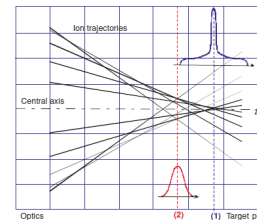
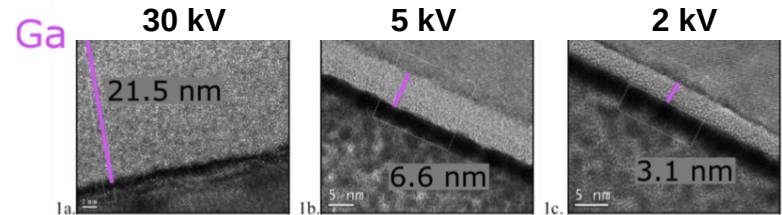


You can also attach the lamella on top of the grid instead of the side

Final tricks and tips

General tips:

- Small currents for high precision
- Large currents for speed
- Polishing for faster milling rate
- Defocus on high currents
- Tilt sample into beam for perpendicular cut
- Short dwell time for high control of shape/depth
- Long dwell time for hard materials /speed
- Several passes for nanopatterning to avoid redeposition
- Well tuned beam (e.g. dose and dwell time for GIS)



Normal

Pt cap

Rocking

9mm x2 50k SE(U) 9mm x2 50k SE(U) 9mm x2 50k SE(U)

Time necessary to produce a sample

Pitfalls and possible solutions:

- **Damaged layer and ions implantation** → low kV
- **Tapering** → overtilting, reduce current
- **Curtaining** → protection cap, stage rocking
- **Redeposition** → Several milling steps, reactive gas

Brief History of LASER

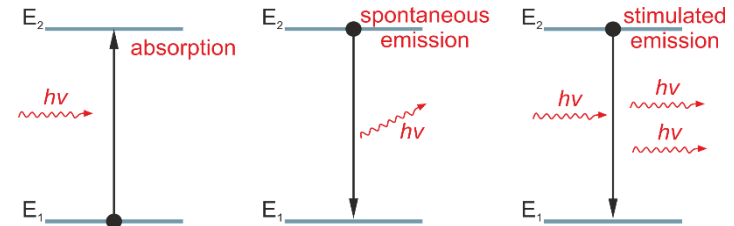
1917 Zur Quantentheorie der Strahlung (*Albert Einstein*)
→ stimulated emission of electromagnetic radiation

1928 Rudolf Ladenburg first observed stimulated emission

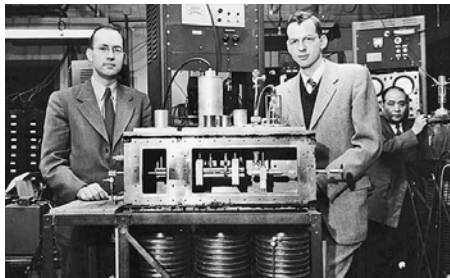
1950s Charles Townes (Columbia University) → MASER:
“microwave amplification by the stimulated emission of radiation.”

Gordon Gould (PhD @ CU) → LASER

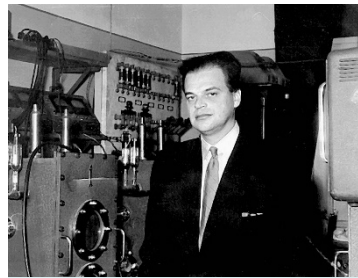
1964 Nobel Prize in Physics



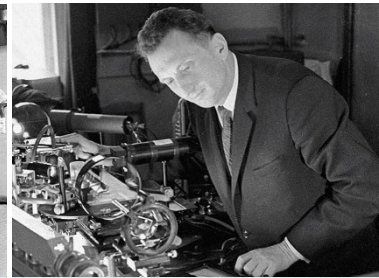
Albert Einstein and Rudolf Ladenburg
(Princeton Symposium, 1950)



Charles Townes and Gordon Gould



Nikolay Basov



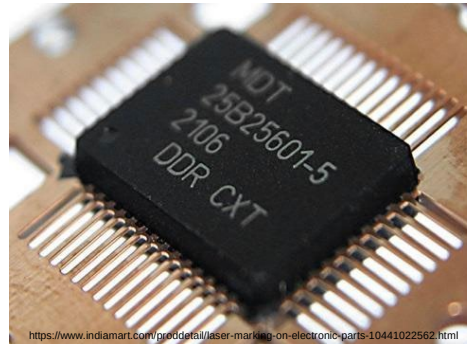
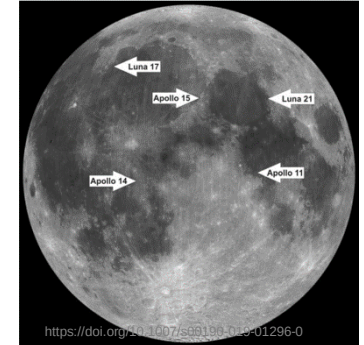
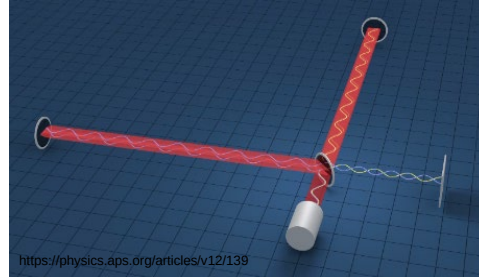
Aleksandr Prokhorov

1960s Hughes Research Laboratories in Malibu/ Bell Labs (New Jersey)/ General Electric Research and Development Center in Schenectady (New York) / ...

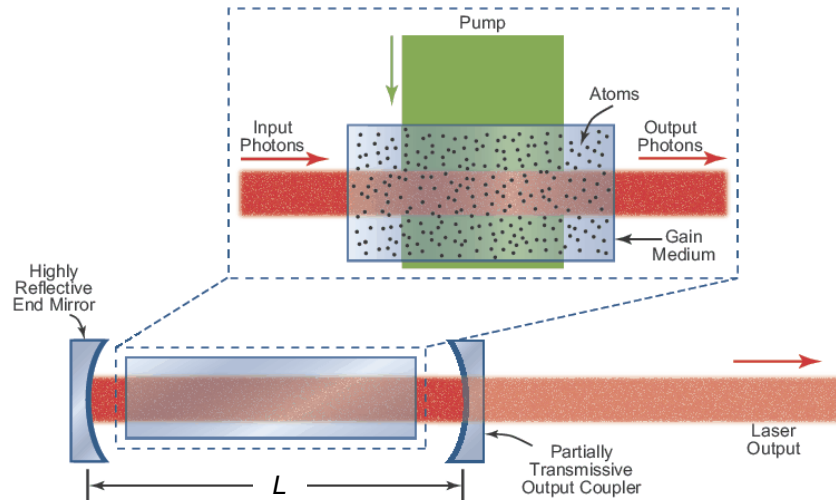
“... a solution looking for a problem”

Laser Applications

- Scientific
- Industrial
- Medical
- Military
- Commercial



Laser Physics



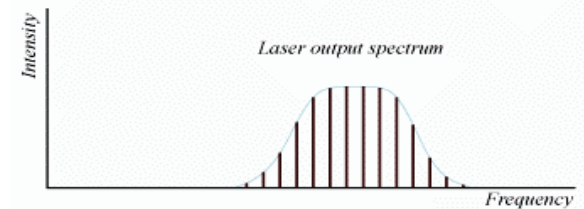
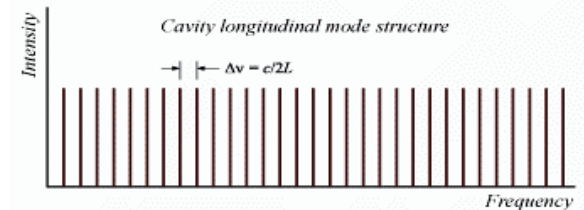
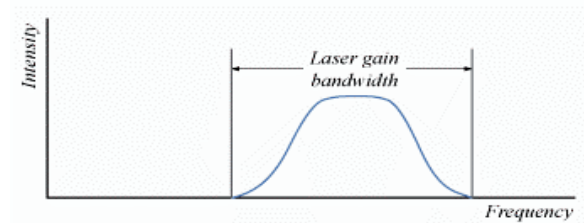
- **Optical resonator**
- **Pump** (optical/electrical/gas)
- **Gain medium**

Solid: doped crystals (Nd:YAG, $\text{Ti:Al}_2\text{O}_3$),
semi-conductors (InGaAs)

Gas: HeNe, N, Ar, CO_2

Liquid: dye solutions (rhodamine 6G)

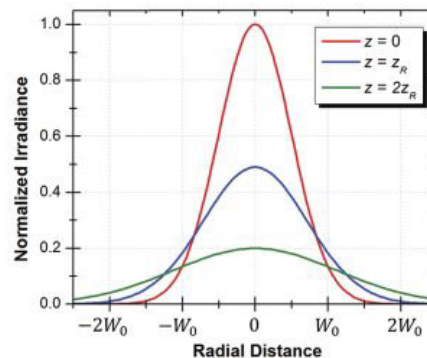
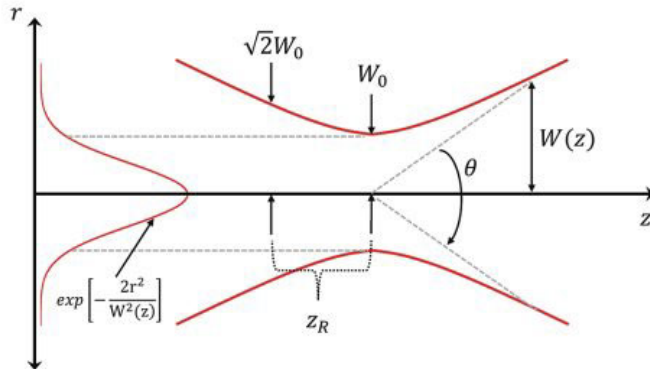
- Wavelength, λ
- Gain Bandwidth, B
- Output Power, P



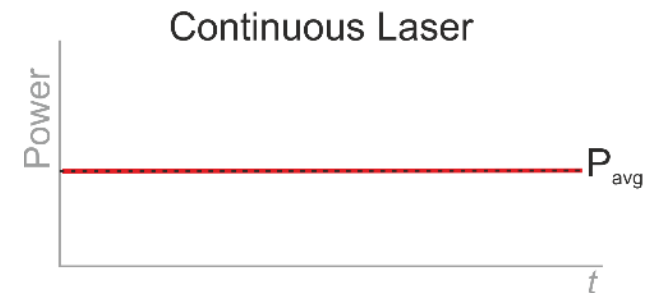
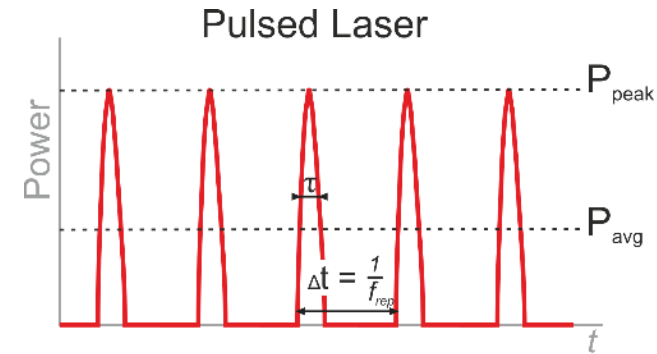
Laser Physics

- Continuous laser
- Pulsed laser (0.5 to 500 ns)
- Ultrashort pulsed laser (5 fs to 100 ps)

Gaussian laser beam profile



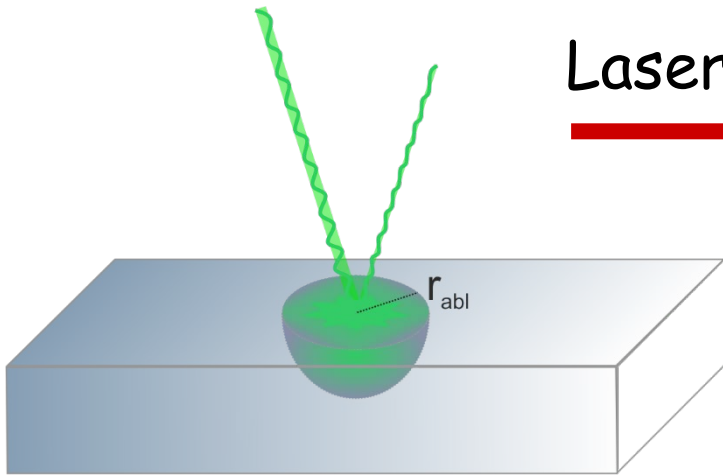
w_0 – beam waist radius



$$E_{pulse} = \frac{P_{avg}}{f_{rep}} [J]$$

$$P_{peak} = \frac{E_{pulse}}{\tau} [W]$$

Laser Ablation Principles



Laser-Induced Damage $\leftrightarrow$ **Fluence** [J/cm^2]

$$F_0^{peak} = 2 \frac{E_{pulse}}{\pi \omega_0^2}$$

$$F(r) = F_0^{peak} \exp\left(-\frac{2r^2}{\omega_0^2}\right)$$

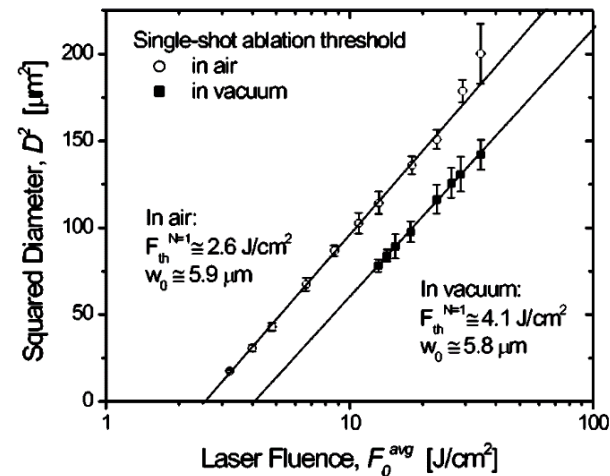
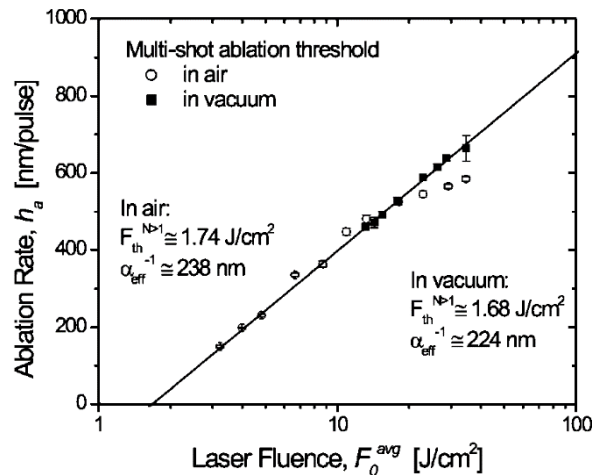
$$F_{th} = F_0^{peak} \exp\left(-\frac{2r_{th}^2}{\omega_0^2}\right)$$

Ablation rate [nm/pulse]: $h_a = \alpha_{eff}^{-1} \ln\left(\frac{F_0^{av}}{F_{th}^{N \geq 1}}\right)$ [1]

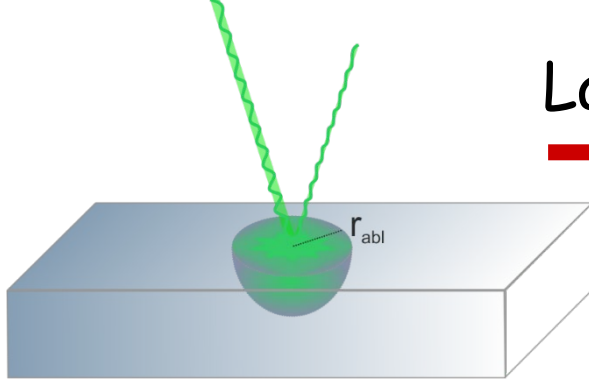
$F_0^{avg} = \frac{1}{2} F_0^{peak}$, α_{eff}^{-1} – effective optical penetration depth

Ablation "crater" diameter: $D^2 = 2w_0^2 \ln\left(\frac{F_0^{peak}}{F_{th}}\right)$

Fs-laser ablation properties of borosilicate glass [2]



Laser Ablation Principles



Interaction mechanisms x fs-laser ablation [3]

- 1) absorption of laser energy through photon-electron coupling (~ fs)
- 2) energy distribution to the lattice through electron-phonon coupling (~10 ps)
- 3) normal energy diffusion into the material through phonon-phonon collision

Laser-Induced Heat accumulation: **Two-temperature model (TTM)** [4]

$$C_e \frac{\partial T_e}{\partial t} = \nabla \cdot (k_e \nabla T_e) - g(T_e - T_p) + Q^*(x, y, z, t),$$

$$C_p \frac{\partial T_p}{\partial t} = \nabla \cdot (k_p \nabla T_p) + g(T_e - T_p)$$

[5] ablated volume $\leftrightarrow$ isolated mechanism
($T_e = T_p = T$)

$$(C_e + C_p) \frac{\partial T}{\partial t} = \nabla \cdot (k_e + k_p) \nabla T + Q(x, y, z, t)$$

[5] Bulk heat capacity: $(C_e + C_p) = \rho c$
Bulk thermal conductivity $(k_e + k_p) = k$

$$\rho c \frac{\partial T}{\partial t} = \nabla \cdot k \nabla T + Q(x, y, z, t)$$

e – electron / p – phonon

C, k – heat capacity and thermal conductivity

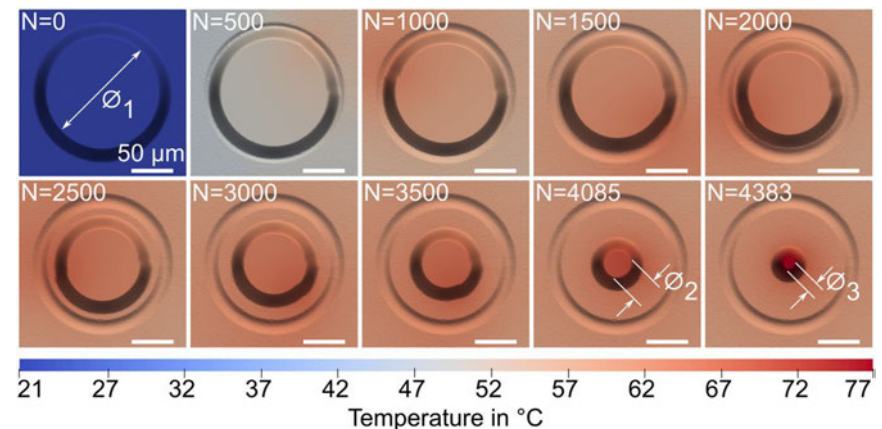
g – electron – phonon coupling

$Q(x, y, z, t)$ – energy absorption rate (spatial and temporal):

$Q(x, y, z, t) = S(x, y, z) \cdot T(t)$

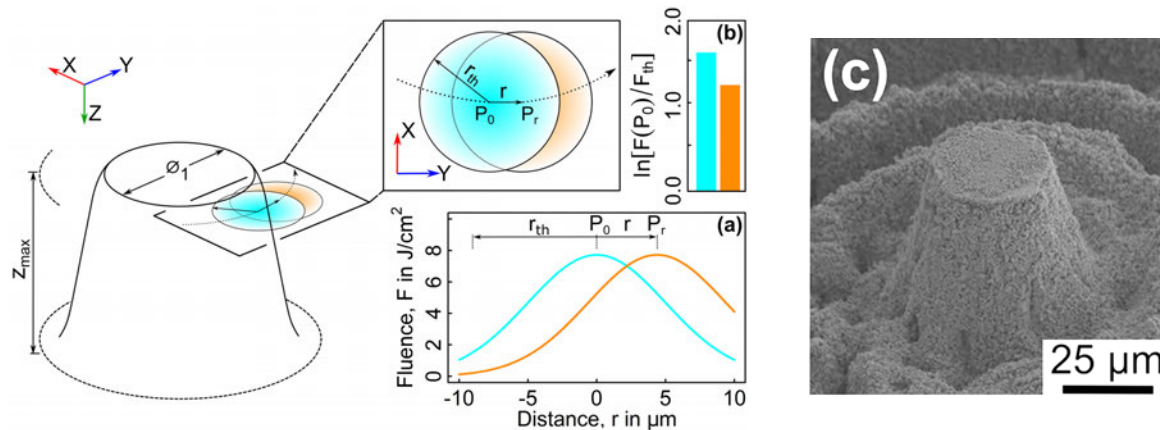
* – terms that vary between dielectrics and Me

FEM of temperature distribution during laser ablation extraction of mineralized tissue micropillar (final diameter ~12 μm) [5]

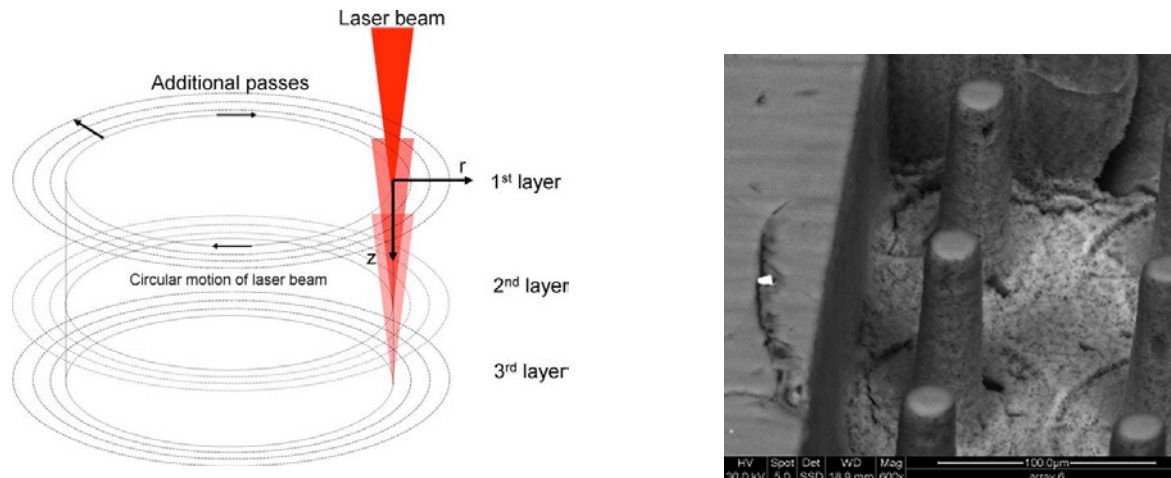


Laser Ablation for micropillar fabrication

Heat impact during laser ablation extraction of mineralised tissue micropillars [5]
(anticlockwise inward spiral pattern)

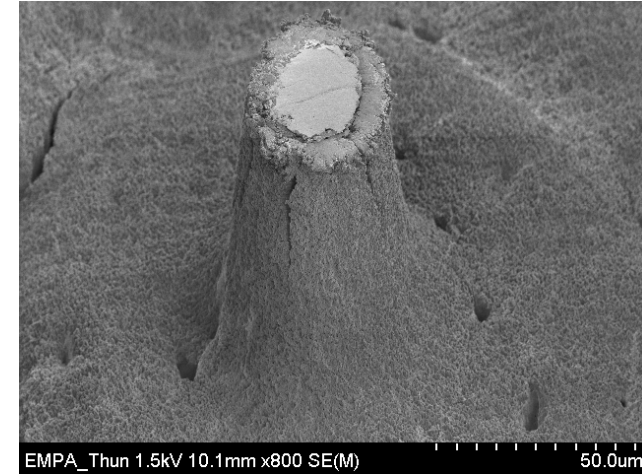
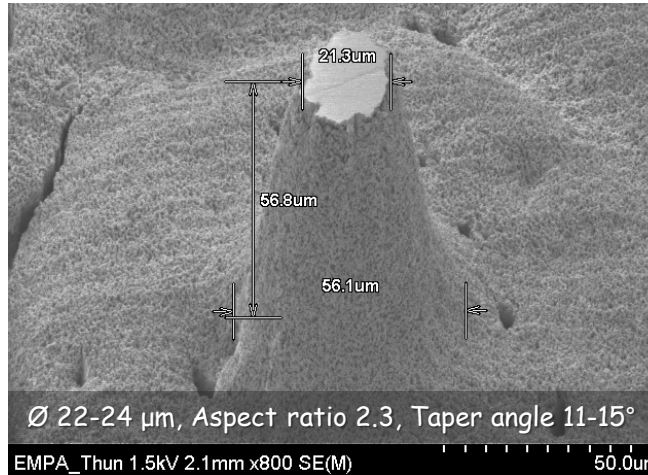


Micropillar fabrication on bovine cortical bone by direct-write femtosecond laser ablation [6]



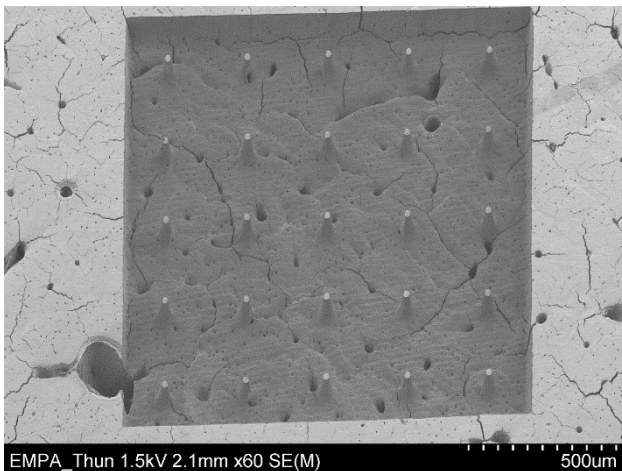
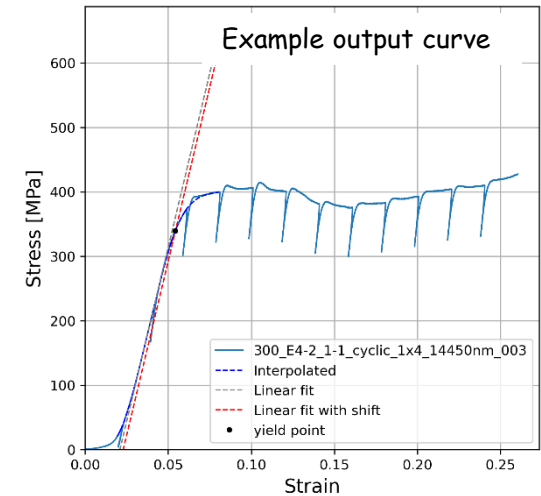
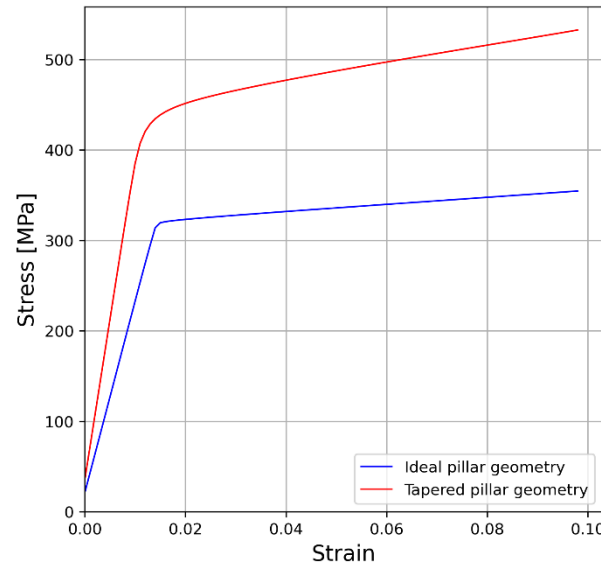
Micropillar compression

Scanning ablation @ALPS BFH :



- $\lambda = 515 \text{ nm}$
- $f_{\text{rep}} = 3 \text{ kHz}$
- $F_{\text{peak}} = 5.14 \text{ J/cm}^2$

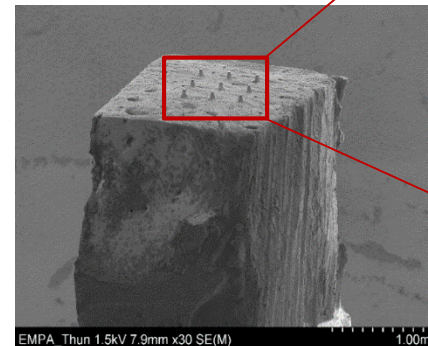
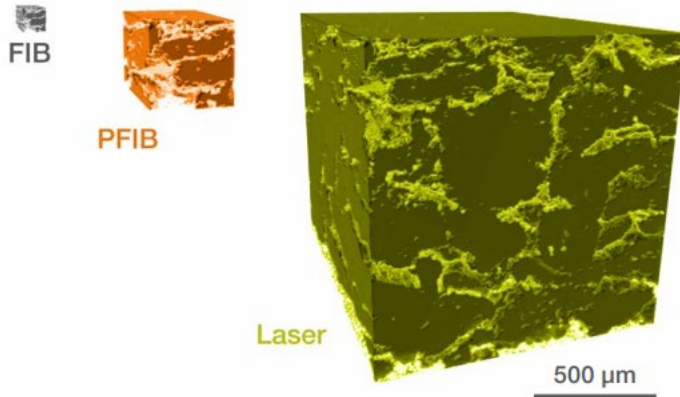
FEM of micropillar compression with different geometries



Laser Ablation for micropillar fabrication

	Ga ⁺ FIB	PFIB	Fs-Laser
Removal rate (Si)	~18 $\mu\text{m}^3/\text{s}$ 1x	~675 $\mu\text{m}^3/\text{s}$ 38x faster	~265000 $\mu\text{m}^3/\text{s}$ 15000x faster
Spot size	50nm	100nm-10 μm	10-20 μm

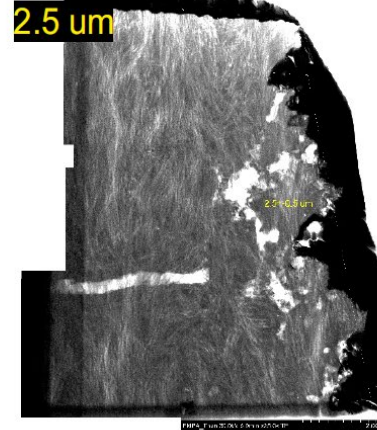
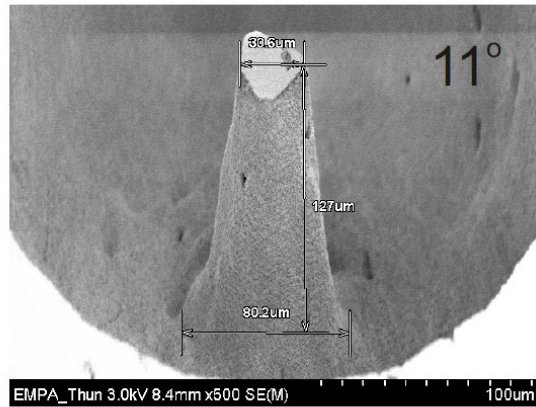
Comparison of 3D volumes milled within the same amount of time with FIB, Plasma FIB, and femtosecond laser



Surface damage

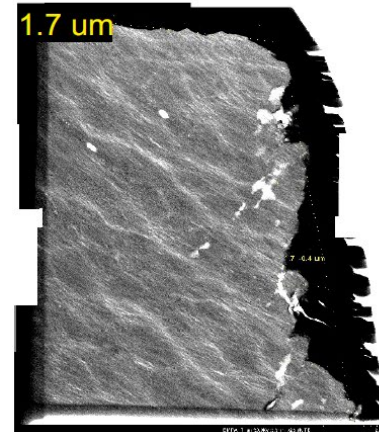
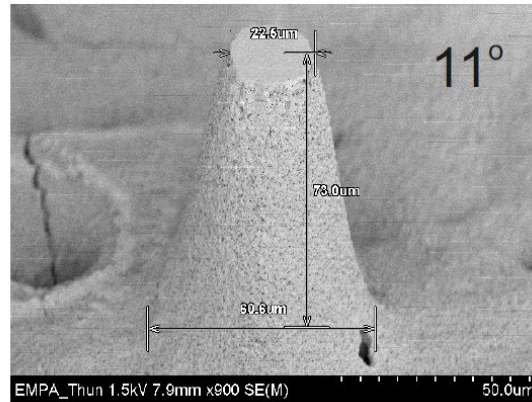
Spiral :

1W@5kHz



Bitmap:

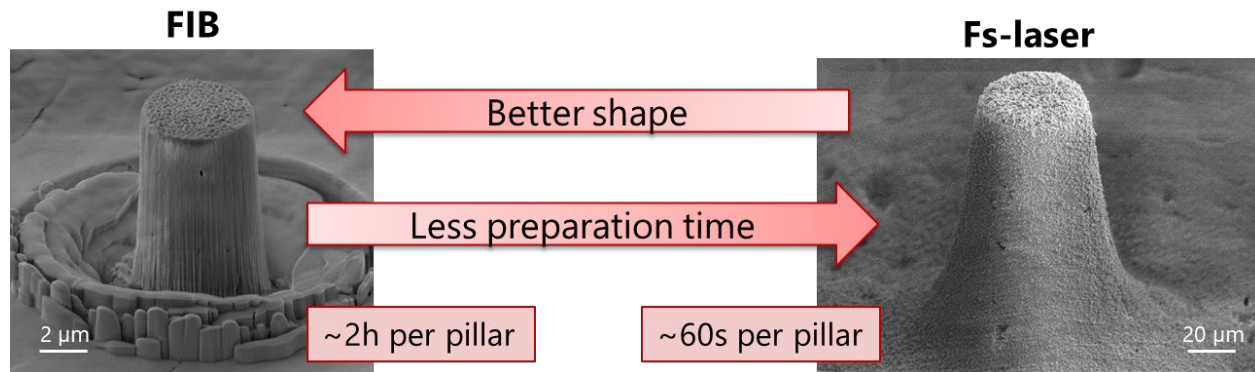
2W@3kHz



Laser Ablation for micropillar fabrication

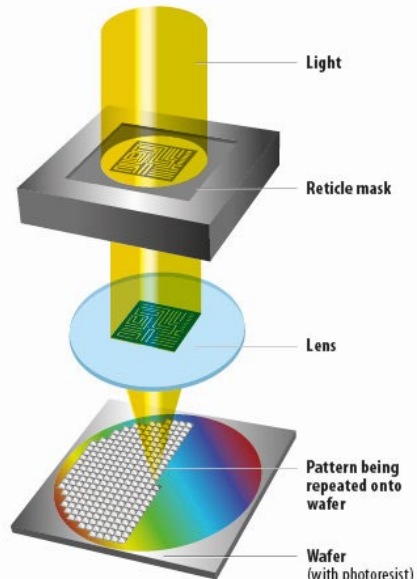
take-home message:

- Choosing laser system for ablation (CW/pulsed)
- ★ Ultrashort pulsed laser (<100 ps)
- Choosing laser parameters for ablation (λ , τ , f_{rep} , F^{pulse} , N)
- Ways to improve micropillar geometry (focal height adjustment, beam waist radius, beam profile)



Lithography for 3D nanoscale metamaterials

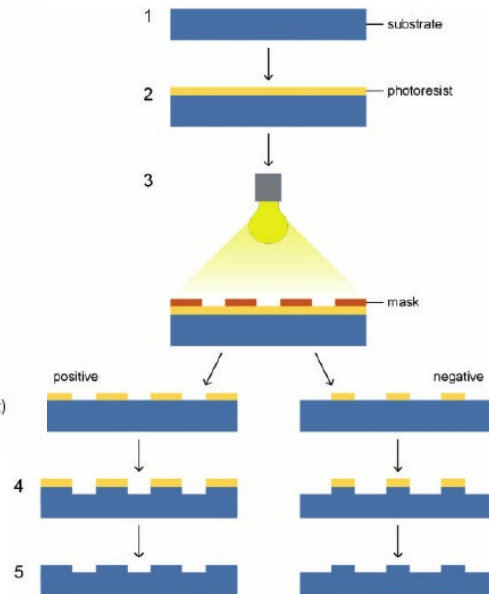
Basic idea



3 basic ingredients:

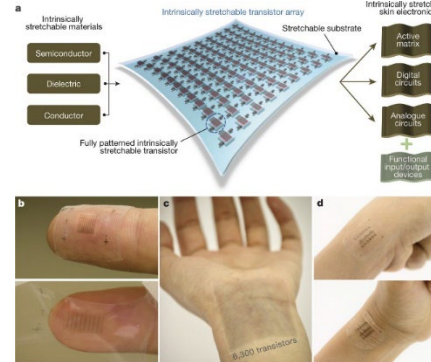
- light
- mask
- resist

Categories

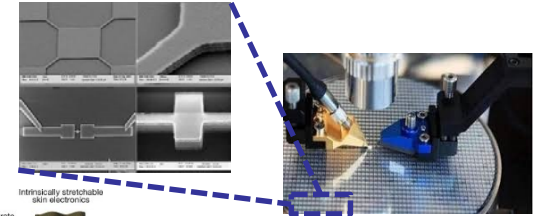


Applications

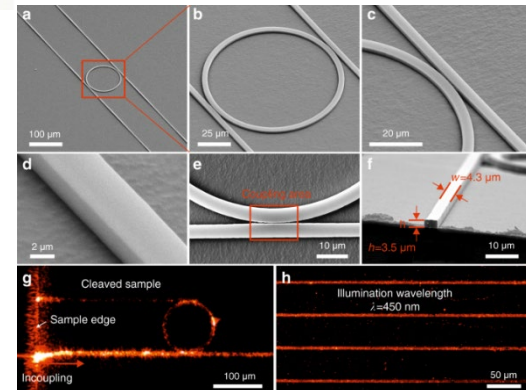
Bio-electronics



All about integrated electronic circuits

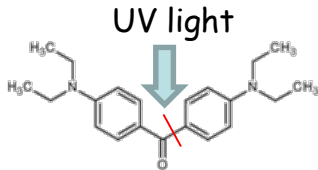


Photonic structures
Devices that guide light instead of electrons

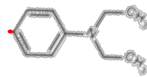


How it works

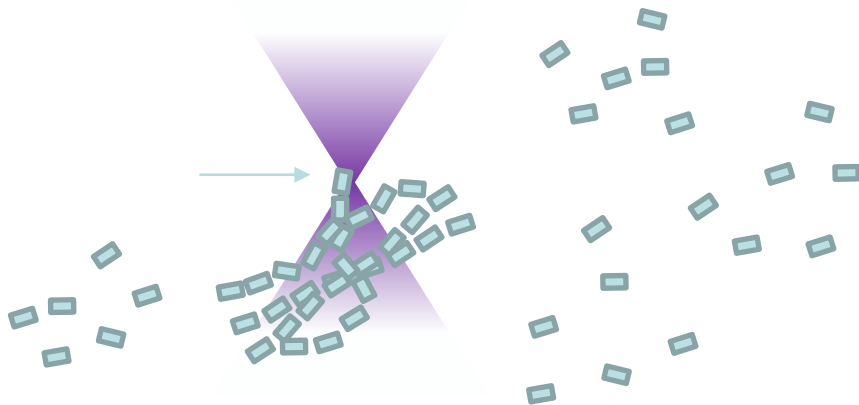
Chemistry
Photo-initiator



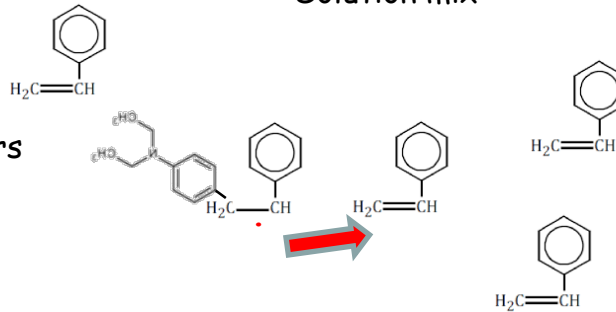
Free radicals attack monomers



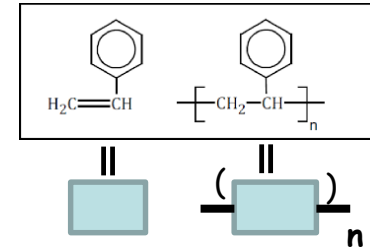
UV light



Solution mix



Monomer Polymer



Drawbacks

-2D patterns only

-Mask required for different patterns, increases the cost

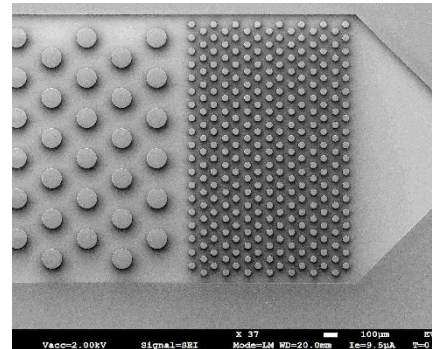
-Resolution: diffraction limited $d = \frac{\lambda}{2n \sin \theta} = \frac{\lambda}{2NA}$

$\lambda=500\text{nm}$ can be focused only down to 250nm

-Limited variety of designs

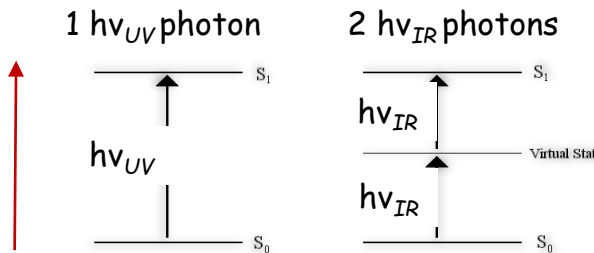
-Limited Opto-mechanics

High quality patterns

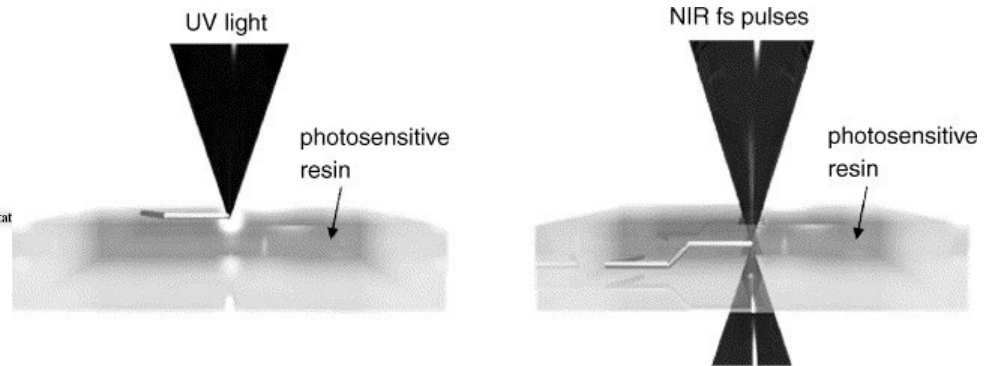


Single photon vs multiphoton

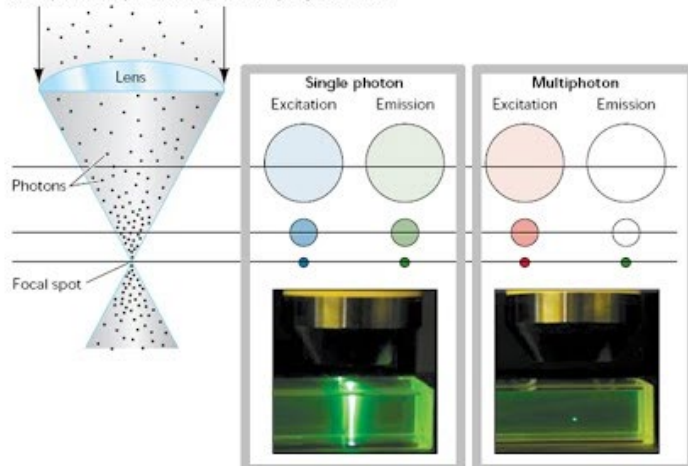
Energy needed for polymerization



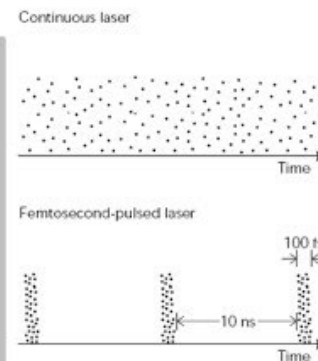
Volumetric Direct Laser Writing (DLW)



A Spatial compression of photons by objective lens



B Temporal compression of photons during femtosecond pulses



Essential and potential

-Ultrafast laser (pulses shorter than virtual state lifetime)

-3D patterns

-Resolution around 50nm

-Maskless

-Big variety of designs

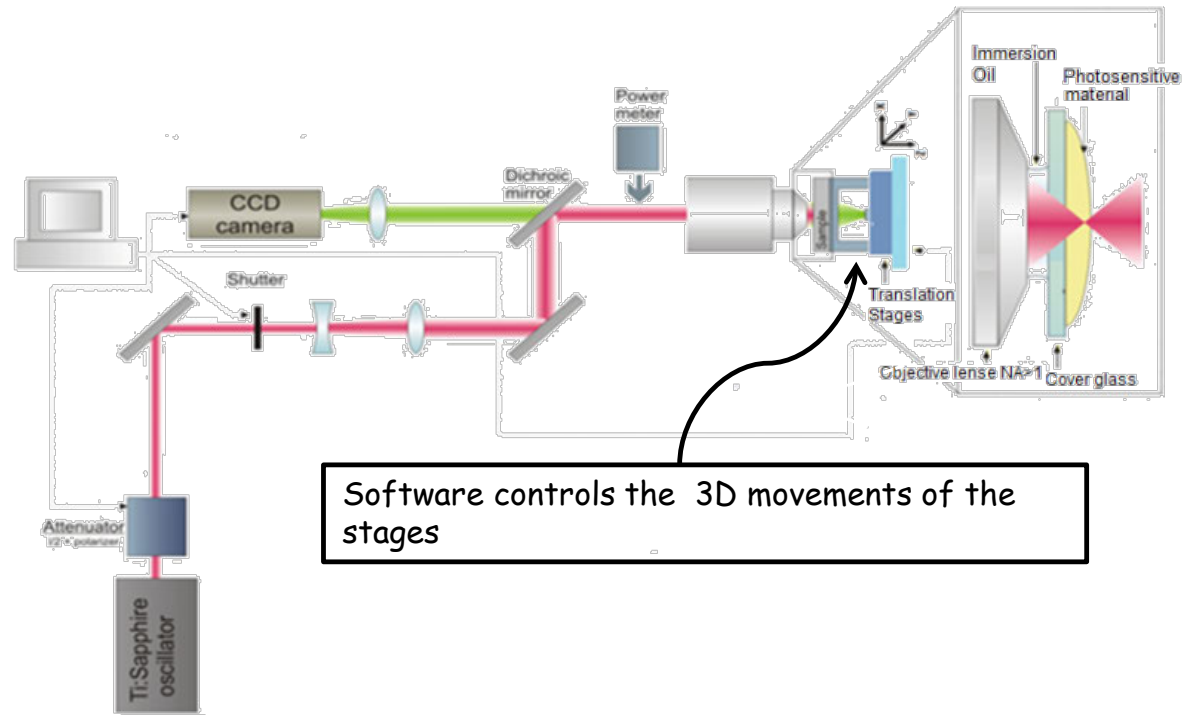
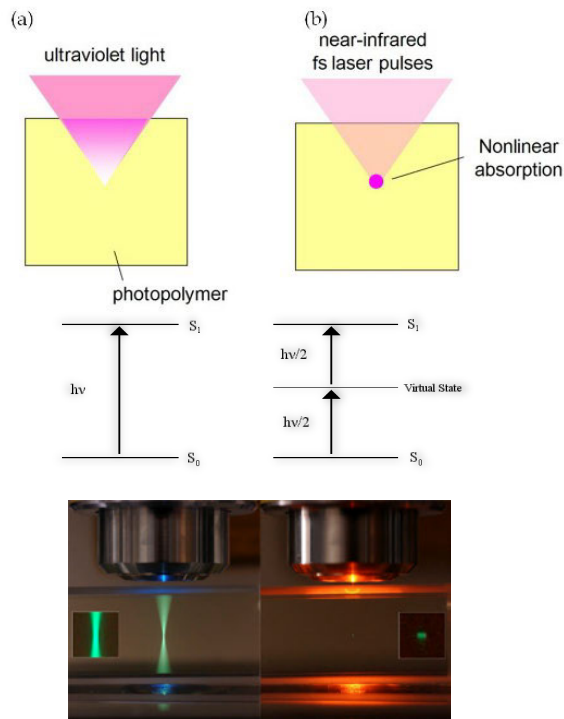
-Rich Opto-mechanics

Setup/instrumentation

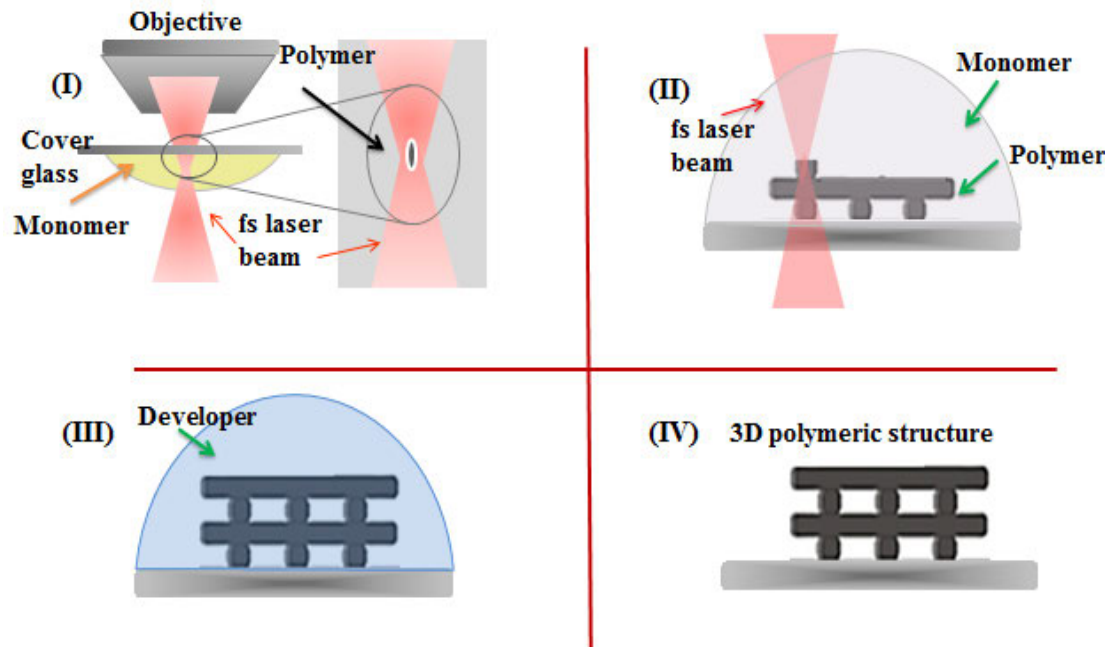
Setup

Ti: Sapphire Femtosecond Laser (800nm, 75MHz, <20fs)

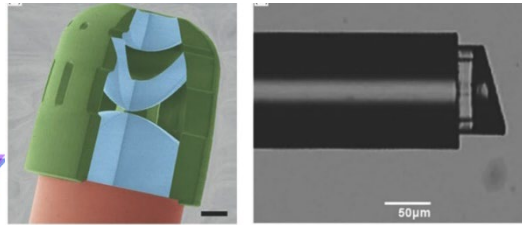
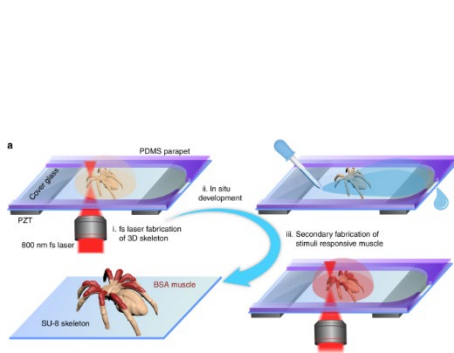
Direct Laser Writing



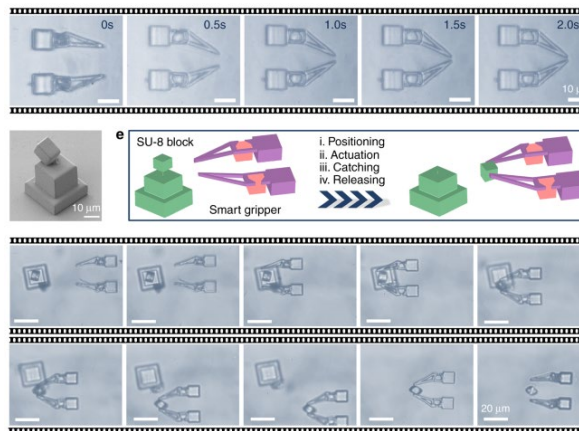
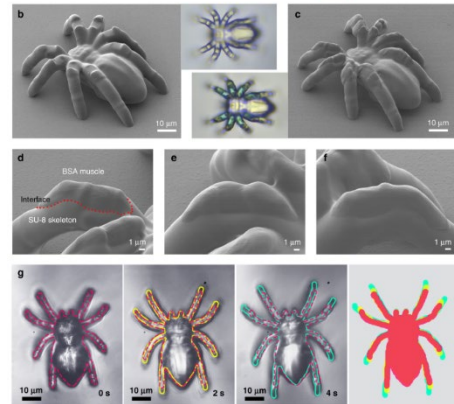
Fabrications steps



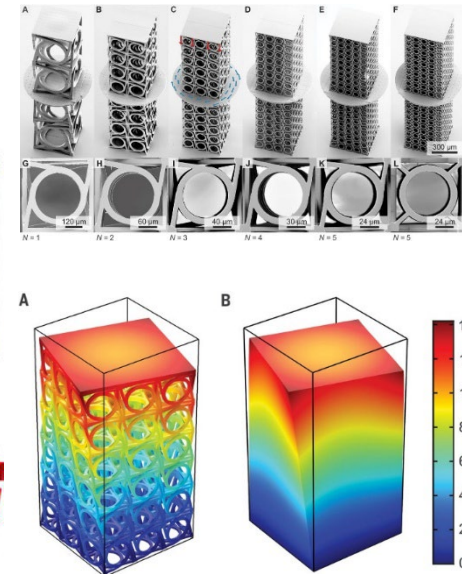
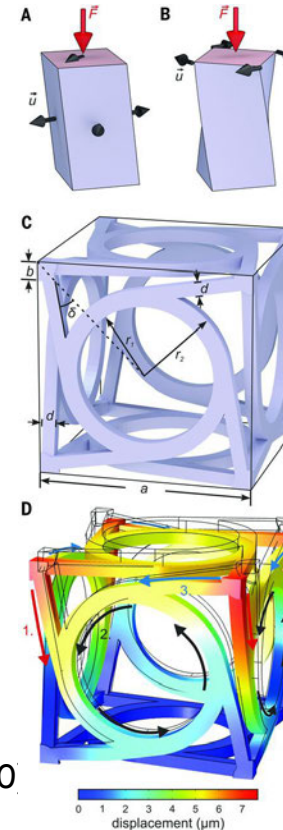
Possibilities



Adv. Opt. Mat. 7, 1800419 (2019)



Nature Commun. 11, 4536 (2020)

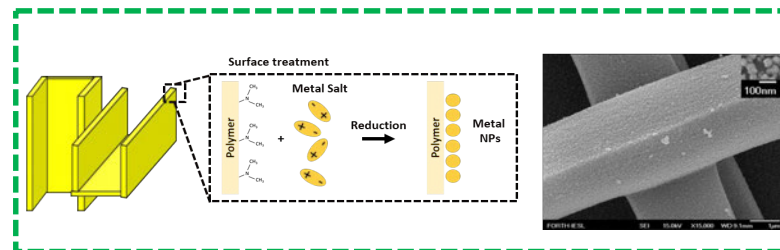
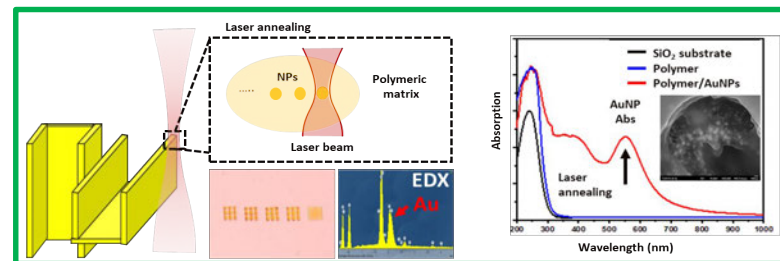
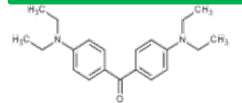
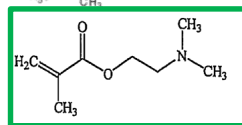
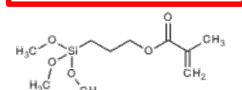
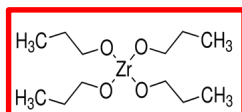
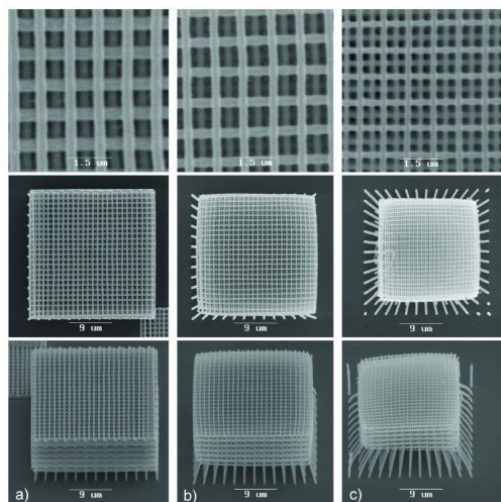


Actuation:
Photo, Thermal, pH, hydrophobic/ hydrophilic, abnormal mechanics

Science 358, 6366, 1072 (2017)

Improve/Advance materials

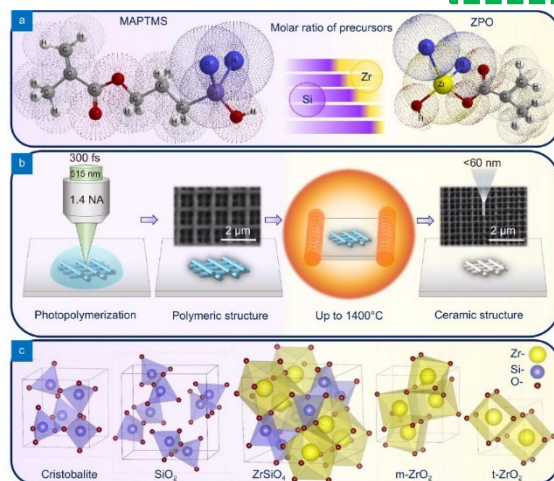
Selective plating of polymeric structures (binding of Au/Ag nanoparticles)



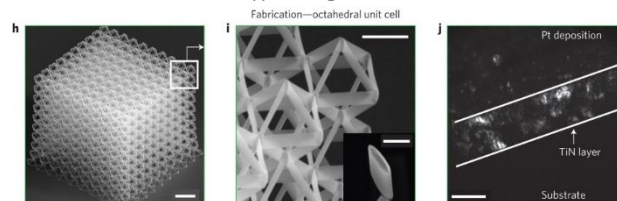
ACS Photonics 2, 287-294 (2015)
Adv. Opt. Mat. 5, 1700200 (2017)

Increasing % of inorganic material

Opt. Express 17, 2143 (2009)



Hollow ceramic 3D structures

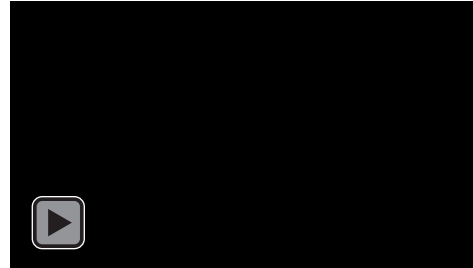


Nature Materials 12, 893 (2013)

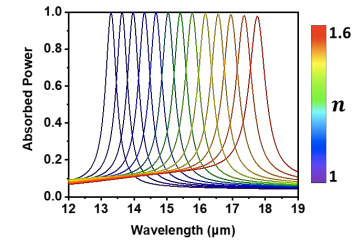
From photo resist to ceramic
Opto-Electron Adv X, 210077 (2022)

Equipment & possibilities at Empa

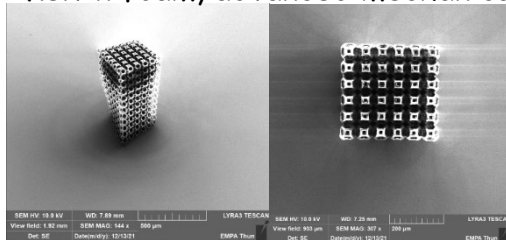
High resolution 3D printer from Nanoscribe



Metamaterials with enhanced light-matter interactions

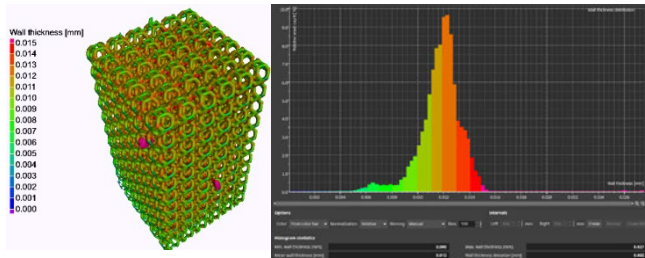


Kelvin foam, advanced mechanical properties

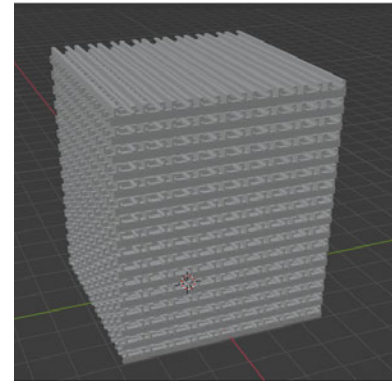


1mm tall
<1hr

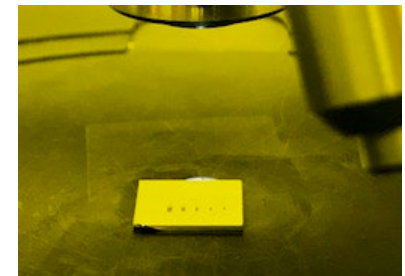
ALD deposition to increase opto-mechanics



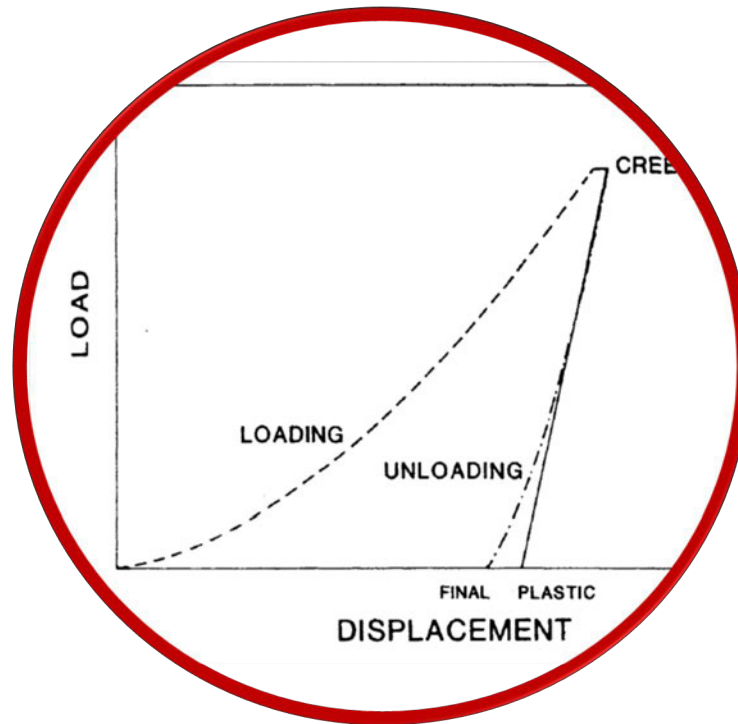
Nano-CT characterisation



Scaling



Nanoindentation



Nanoindentation

1. Definition of hardness
2. Principles of instrumented indentation
3. Load and displacement: actuation and measurement
4. What happens in the material?
5. Mechanical materials properties: beyond hardness and Youngs modulus

Hardness & Young's modulus

hardness: historical definition

Hardness	Mineral
1	Talc
2	Gypsum
3	Calcite
4	Fluorite
5	Apatite
6	Orthoclase
7	Quartz
8	Topaz
9	Corundum
10	Diamond

Mineralogist:
Metallurgist:
Machinist:

resistance to scratching
resistance to penetration
resistance to cutting



Gypsum
Calcite
Fluorite
Apatite
Orthoclase
Quartz
Topaz
Diamond

1812:

Mohs scale of mineral hardness

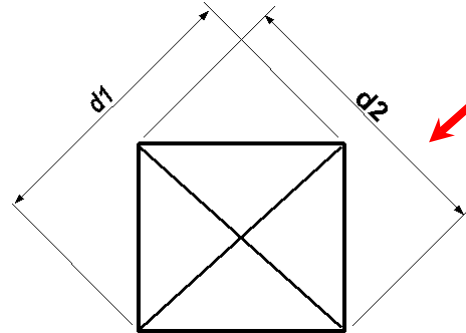
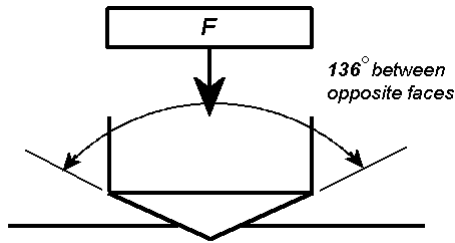
(German mineralogist Frederick Mohs (1773-1839))

Selected the ten minerals because they were common or readily available.

The scale is not a linear scale, but somewhat arbitrary.

Vickers Hardness Test

Diamond indenter body
(Vickers pyramid)



Residual impression
measured
by optical microscopy

$$HV = \frac{2F \sin \frac{136^\circ}{2}}{d^2} \approx 1.854 \cdot \frac{F}{d^2}$$

Load in kgf
d in mm

1 kgf = 9.81 N

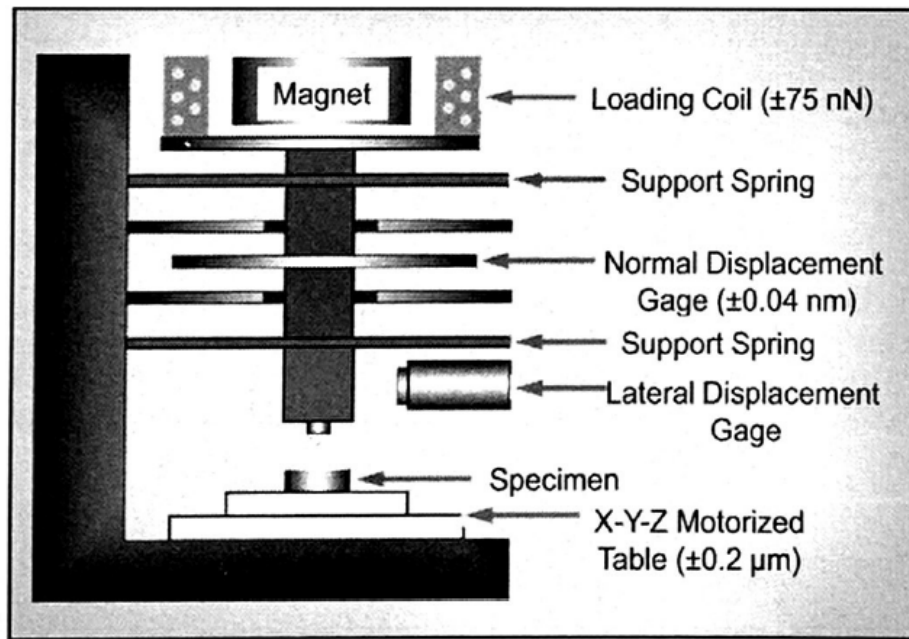
$$HV = 0.1891 \cdot \frac{F}{d^2}$$

Load in N
d in mm

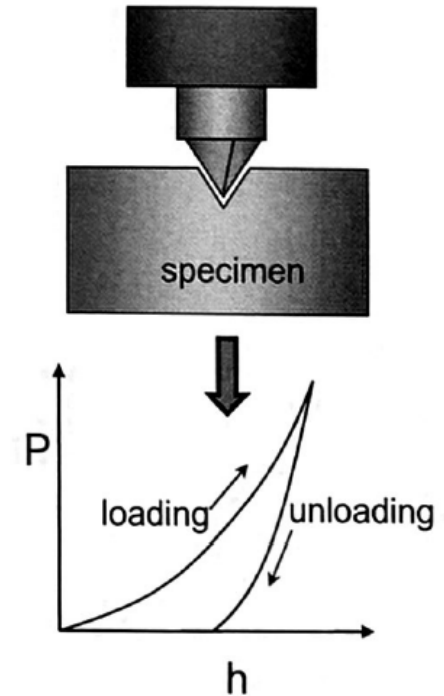
Advantage: „Easy“

Disadvantage: Operator needed for optical measurement
„NOT SUITED“ FOR SMALL OBJECTS OR THIN FILMS

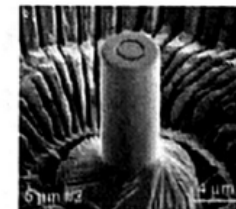
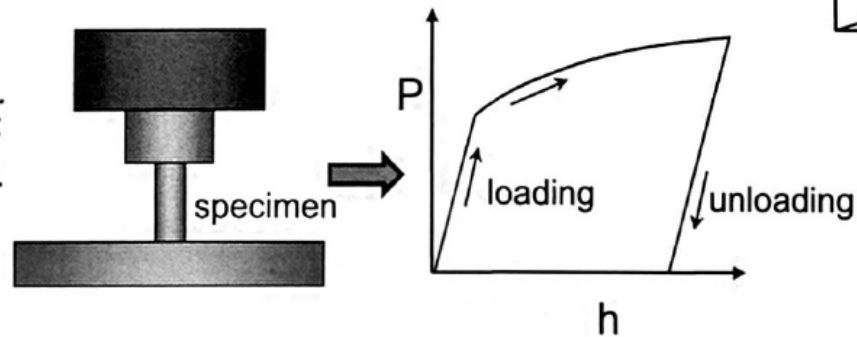
A nanoindenter



Indentation:

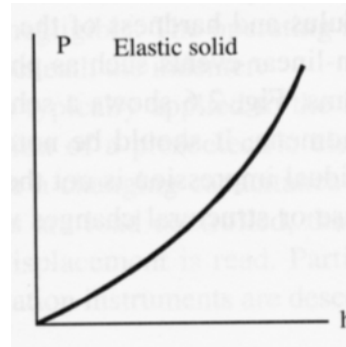


Pillar Testing

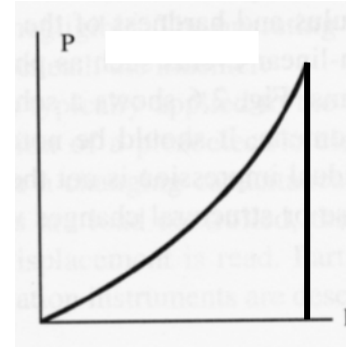


Load-Displacement curves: Typical shapes

Extreme cases:



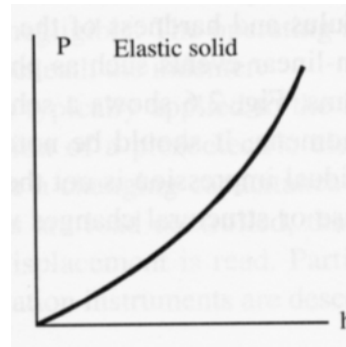
Elastic Solid



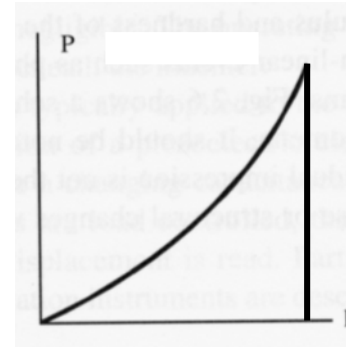
Fully plastic

Load-Displacement curves: Typical shapes

Extreme cases:

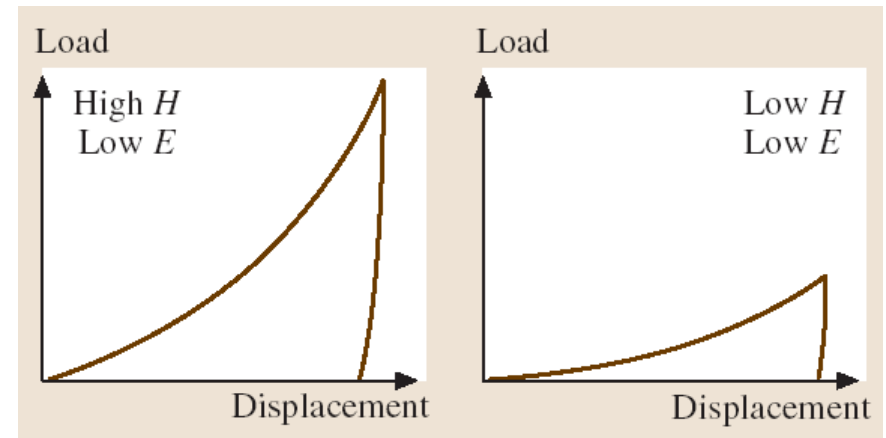
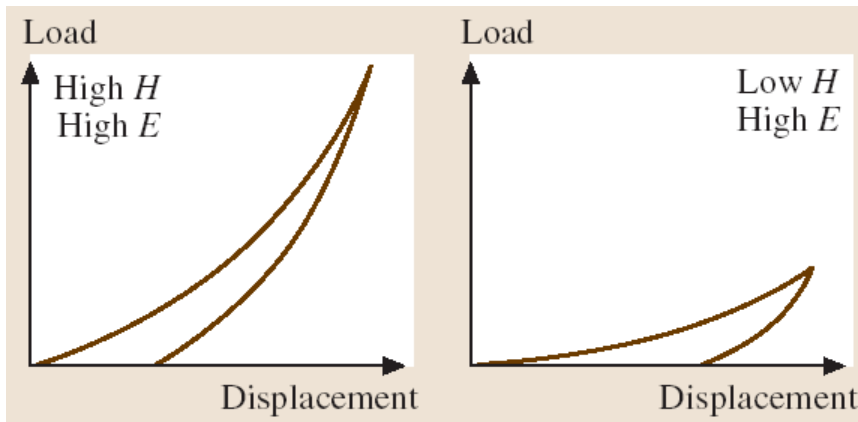


Elastic Solid



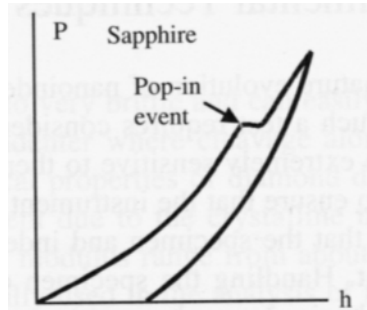
Fully plastic

Typical cases:

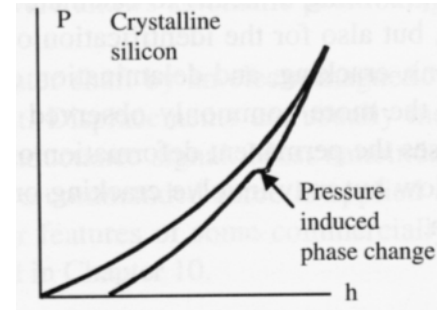


- High hardness $\Leftrightarrow$ High load needed for a given displacement
- Young's modulus depends on the shape of the unloading curve

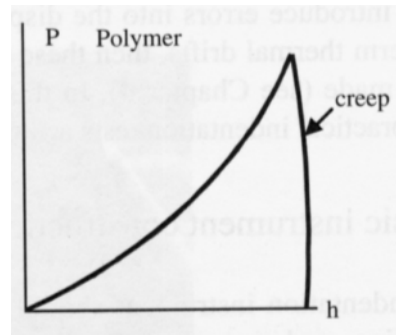
Load-Displacement curves: Typical shapes



Brittle Solid
Cracking during loading

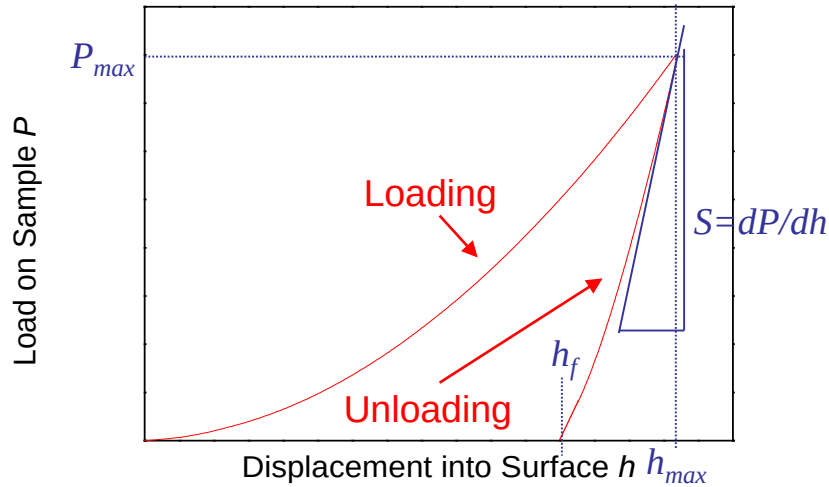


Pressure induced phase change
(Silicon)



Polymer exhibiting creep

Principle of nanoindentation



hardness:

Average contact pressure at maximum load
(projected area)

Young's modulus:

proportional to slope of unloading curve

Basic equations

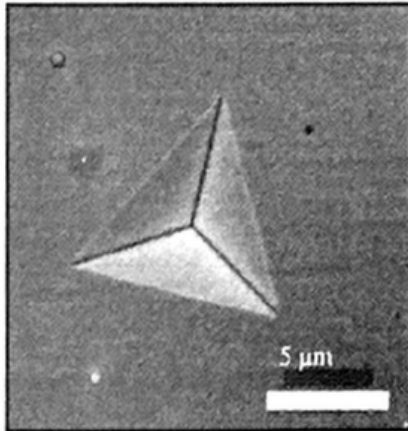
$$E_r = \frac{\sqrt{\pi} \cdot S}{2 \cdot \sqrt{A}}$$

$$\frac{1}{E_r} = \frac{(1-\nu^2)}{E_{\text{Indentation}}} + \frac{(1-\nu_i^2)}{E_i}$$

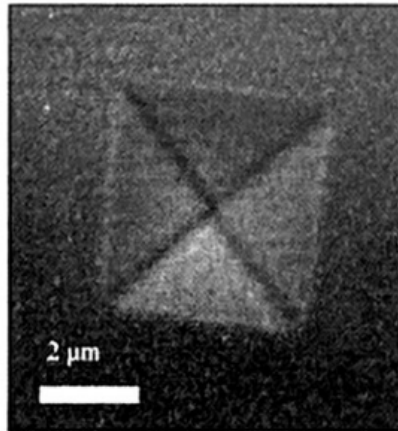
$$H = P/A$$

What determines the contact area?

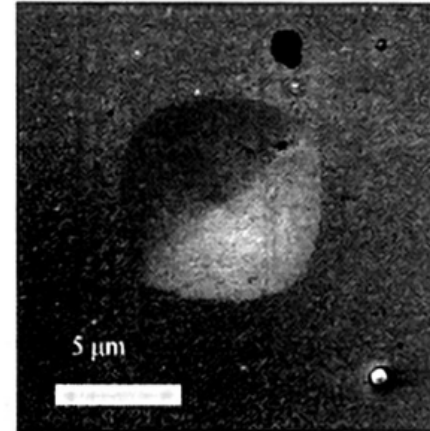
indenter geometries



Berkovich



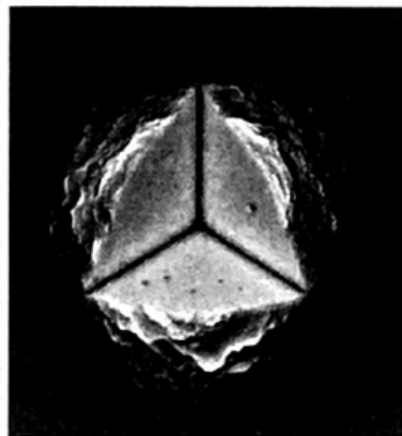
Vickers



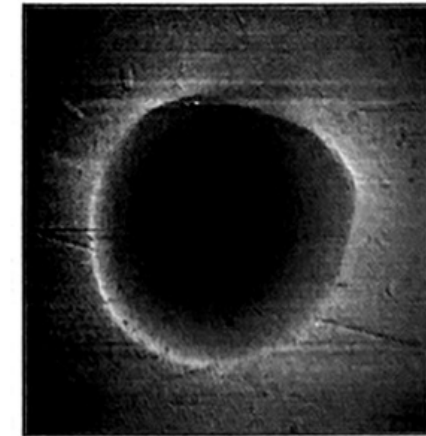
Conical



Berkovich
indenter

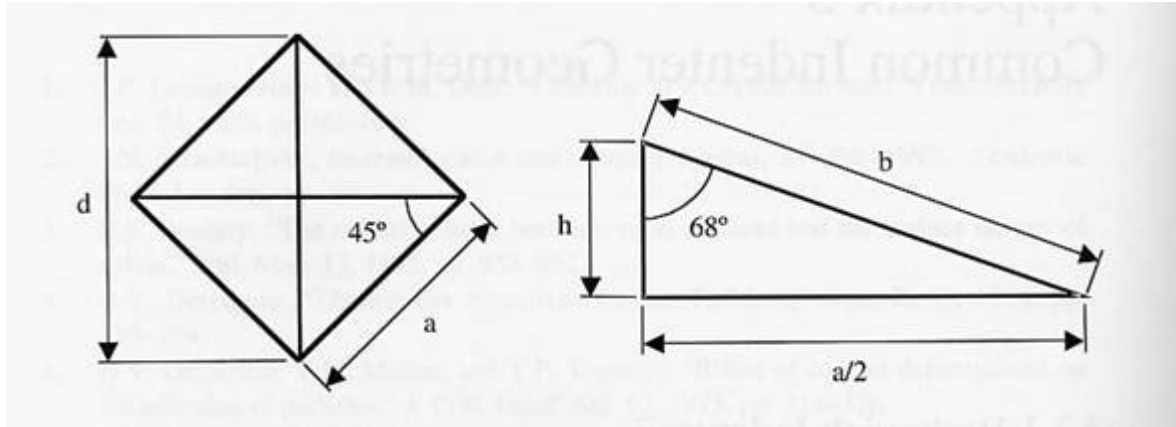


Cube-corner



Spherical

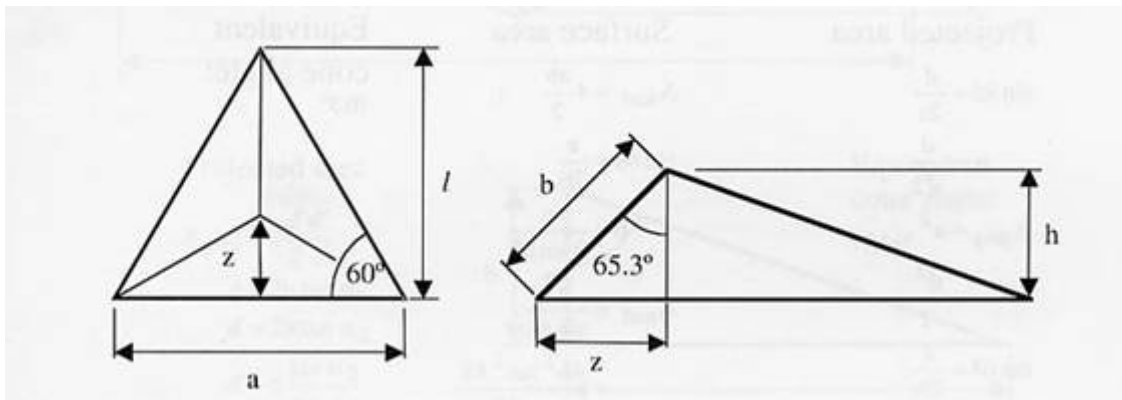
Tip area function assuming ideal geometries



Vickers:

$$A_{\text{proj}} = 24.504 h^2$$

$$A_{\text{surf}} = 26.429 h^2$$



Berkovich:

$$A_{\text{proj}} = 24.56 h^2$$

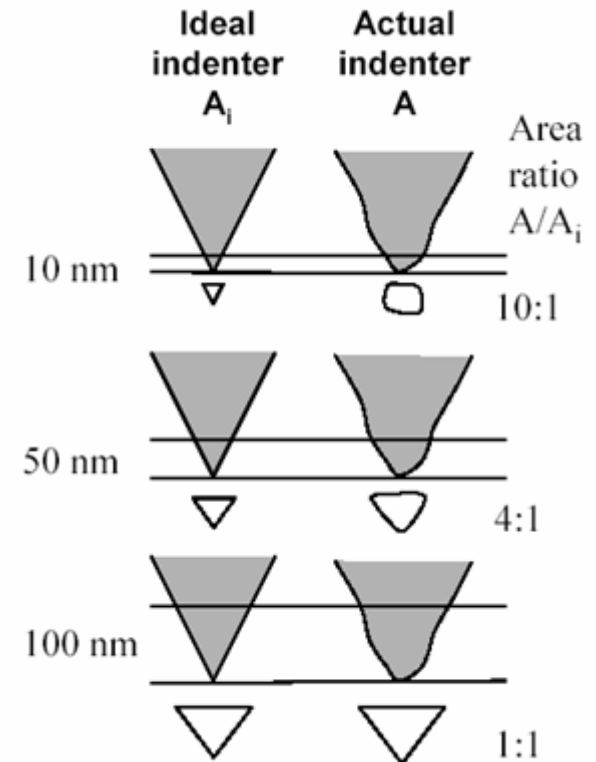
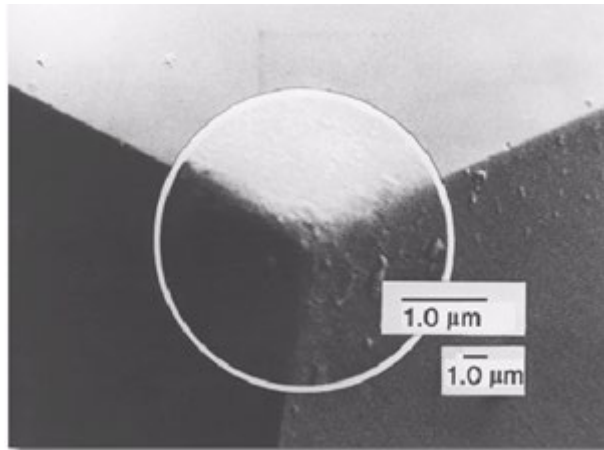
$$A_{\text{surf}} = 27.05 h^2$$

Determination of the tip area function $A(h_c)$

Projected contact area needed for the determination of H and $E_{\text{Indentation}}$ is calculated using the displacement into the surface
Crucial point: Exact tip geometry has to be known for this procedure!!

For small indentation depths ($<1\mu\text{m}$) the assumption of having an ideal tip is not valid.

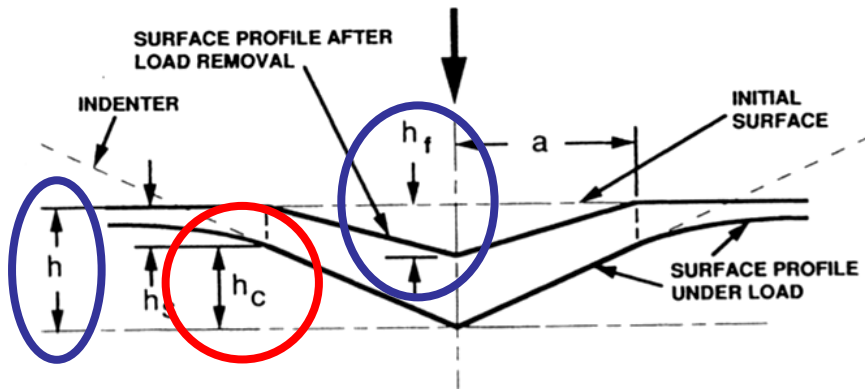
Berkovich: tip roundness between 20 and 100 nm



=> Tip area function

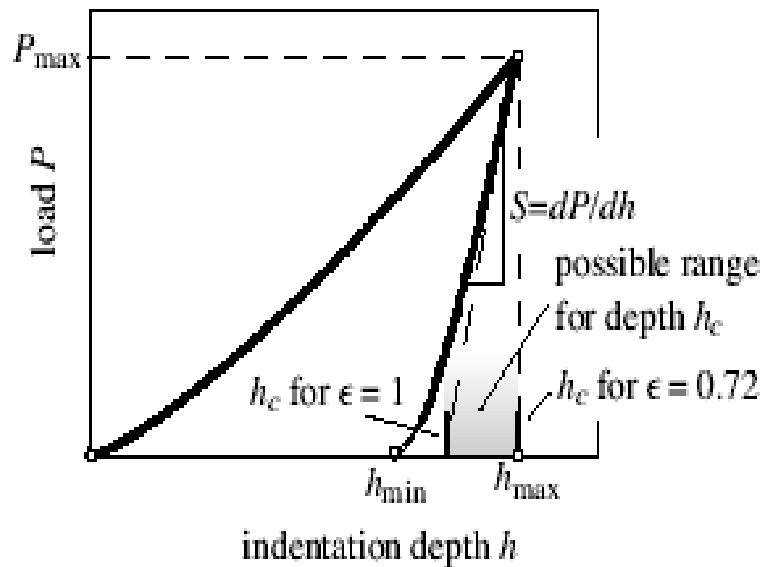
$$A(h_c) = a_0 \cdot h_c^2 + \sum_{i=0}^n a_{i+1} \cdot h_c^{\frac{1}{2^i}}$$

Contact depth



Take into account elastic sink-in!

h maximum depth
 h_f residual depth
 h_c contact depth

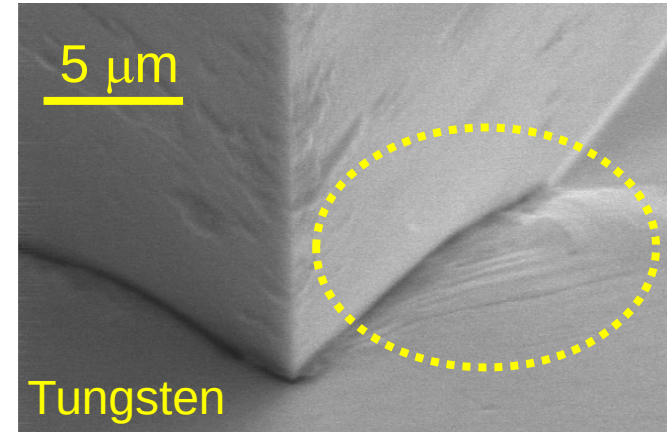
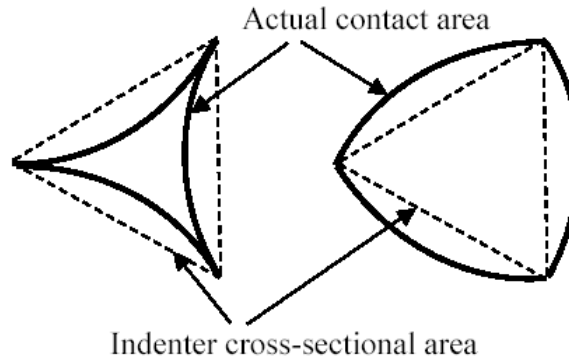
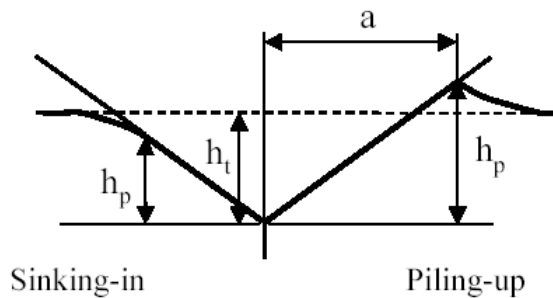


$$h_c = h - \epsilon \frac{P_{\max}}{dP / dh}$$

ϵ is geometry factor to adapt
 "Flat Punch" model to Berkovic indenters

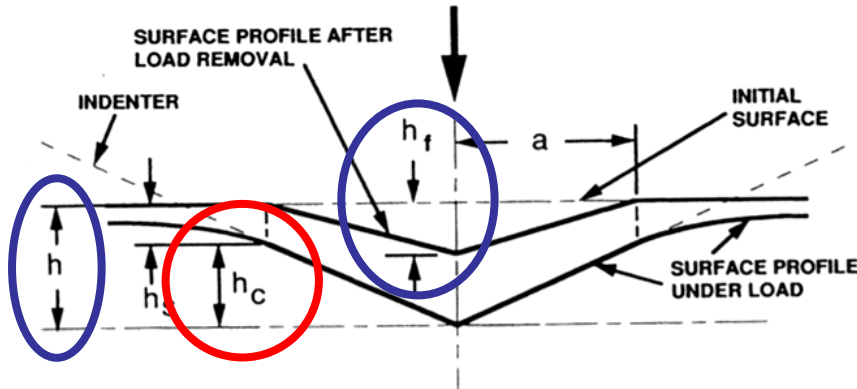
Limit of the model: Pile-up and Sink-in

Depending on strain hardening behavior,
pile-up or sink-in phenomena influence the contact depth value
=> errors in contact area => errors in hardness and modulus



SEM image of cube corner
indent into tungsten

Summary: evaluation of load displacement curves



Fit unload curve

$$P = B(h - h_f)^m$$

$$S = dP/dh \longrightarrow S = Bm(h_{\max} - h_f)^{m-1}$$

Projected contact area

$$h_c = h - \epsilon P/S$$

$$A(h_c) = a_0 \cdot h_c^2 + \sum_{i=0}^n a_i \cdot h_c^{1/2^i}$$

a_i is determined from measurements on reference materials (Fused Silica)

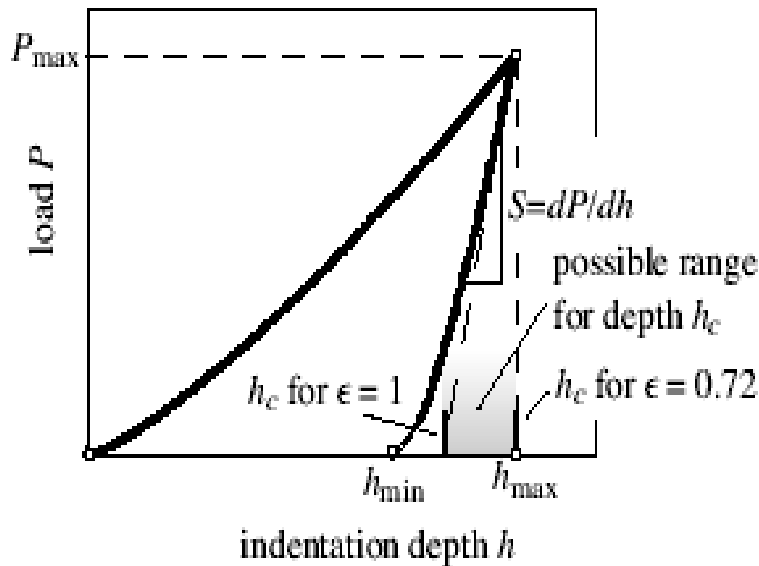
Ideal Berkovich tip: $a_0=24.5$ / $a_i=0$ für $i>0$

Summary H and E

$$E_r = \frac{\sqrt{\pi} \cdot S}{2\beta \cdot \sqrt{A(h_c)}}$$

$$\frac{1}{E_r} = \frac{(1-\nu^2)}{E_{\text{Indentation}}} + \frac{(1-\nu_i^2)}{E_i}$$

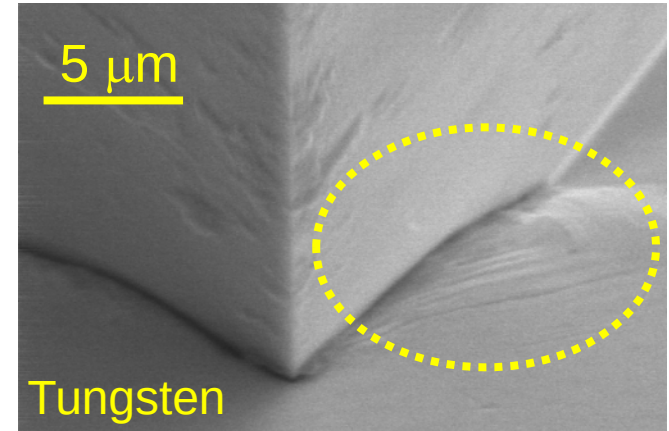
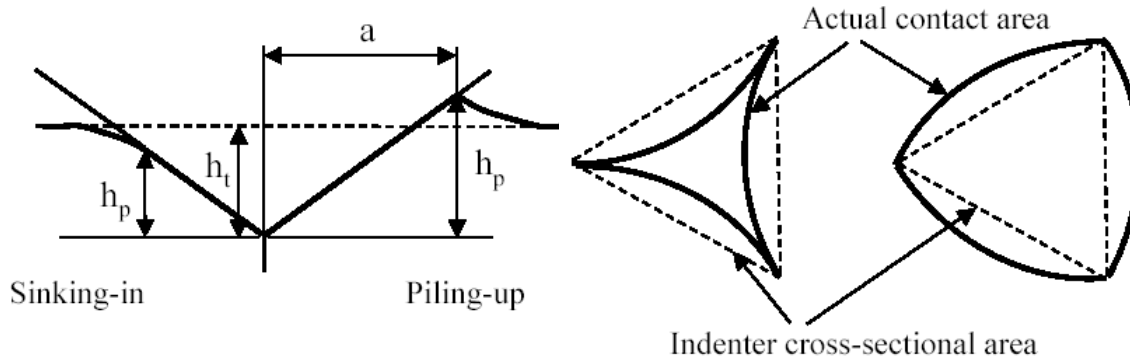
$$H = P/A(h_c)$$



ϵ, β are geometry factors to adapt flat punch model to Berkovic geometry

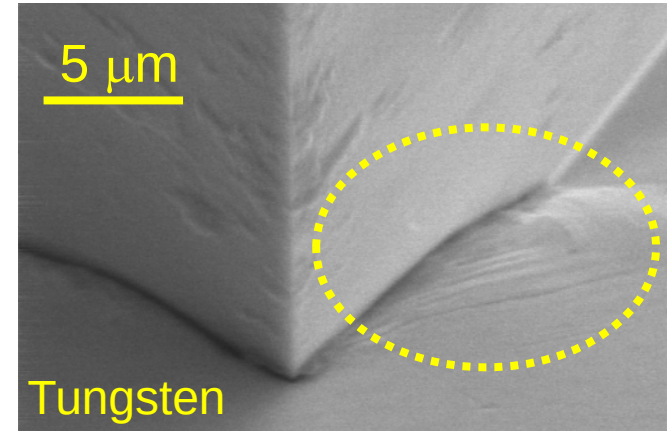
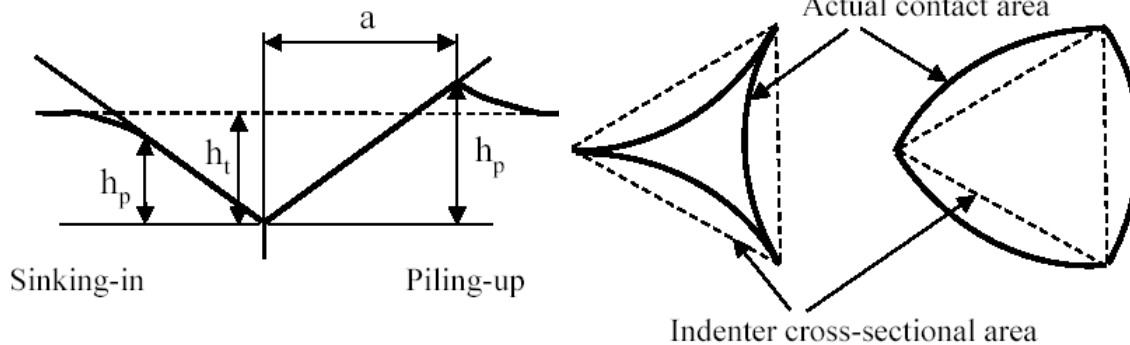
Limit of the model: Pile-up and Sink-in

Pile-up or sink-in phenomena influence the contact depth value
=> errors in contact area => errors in hardness and modulus

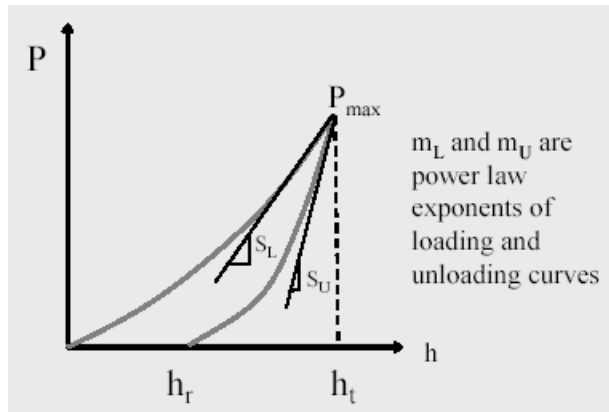


Limit of the model: Pile-up and Sink-in

Pile-up or sink-in phenomena influence the contact depth value
 $\Rightarrow$ errors in contact area $\Rightarrow$ errors in hardness and modulus



Correction factor: (from finite element simulations)



$$\frac{S_L}{S_U} = \frac{m_L}{m_U} \left(1 - \frac{h_r}{h_t} \right)^{1.35}$$

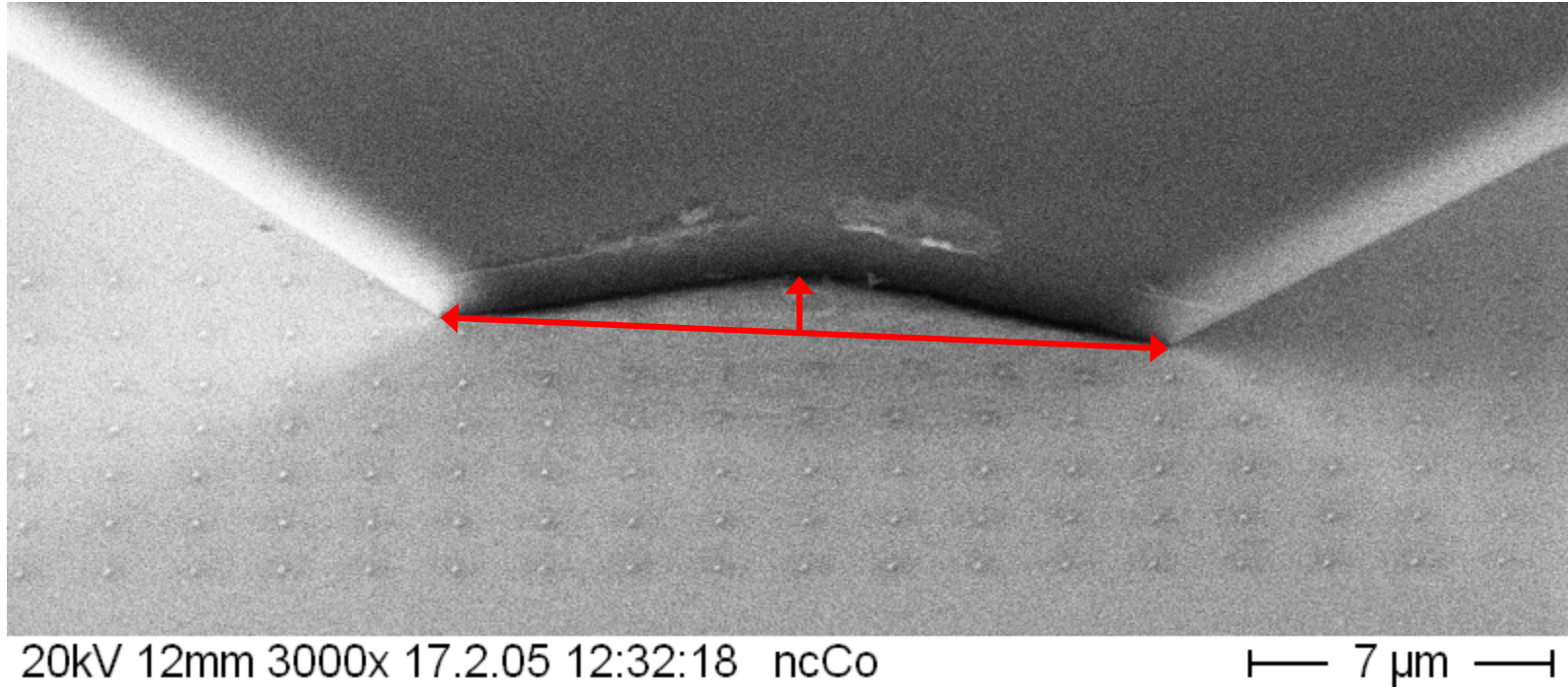
Residual depth

Total depth

1.35

Pile-up, Sink-in factor.
 Can be applied to
 calculated contact area to
 obtain true contact area.

in-situ measurement of contact area



contact area of PDMS

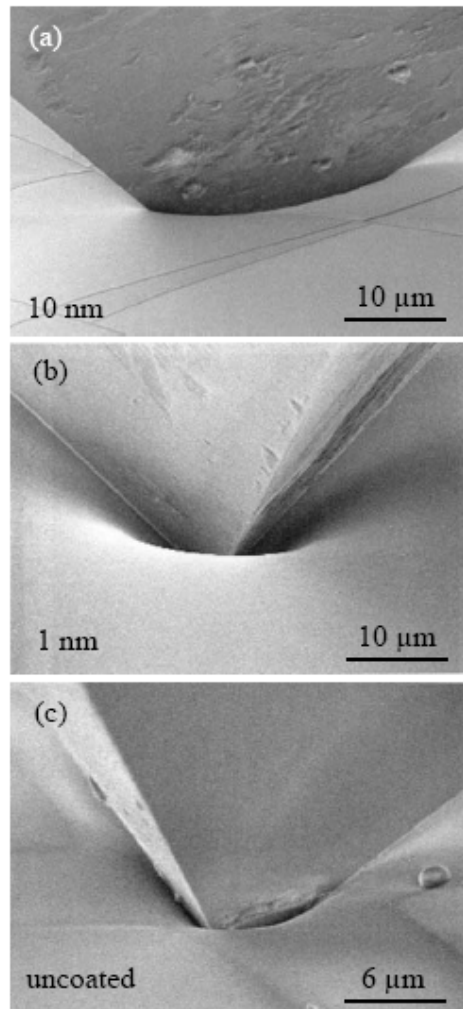
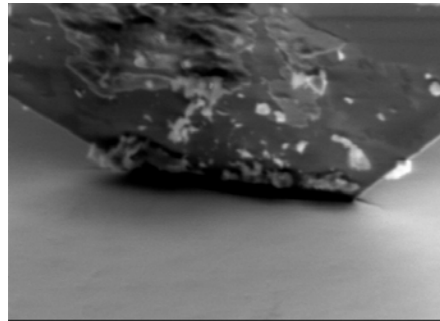


Figure 8

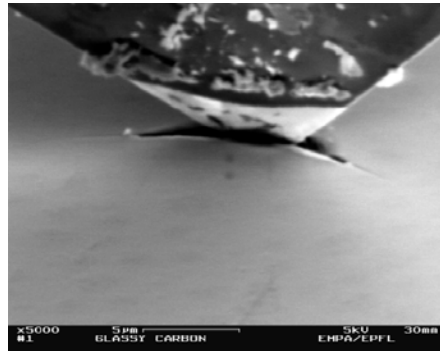
influence of gold layer

J. Deuschle (2008) J. Mater. Res.

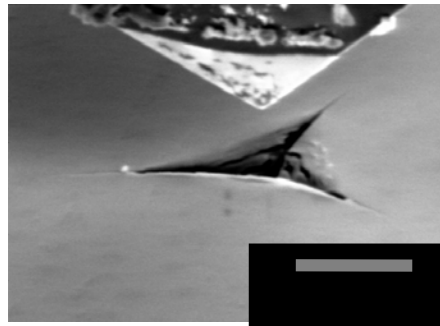
contact area of glassy carbon



max.load

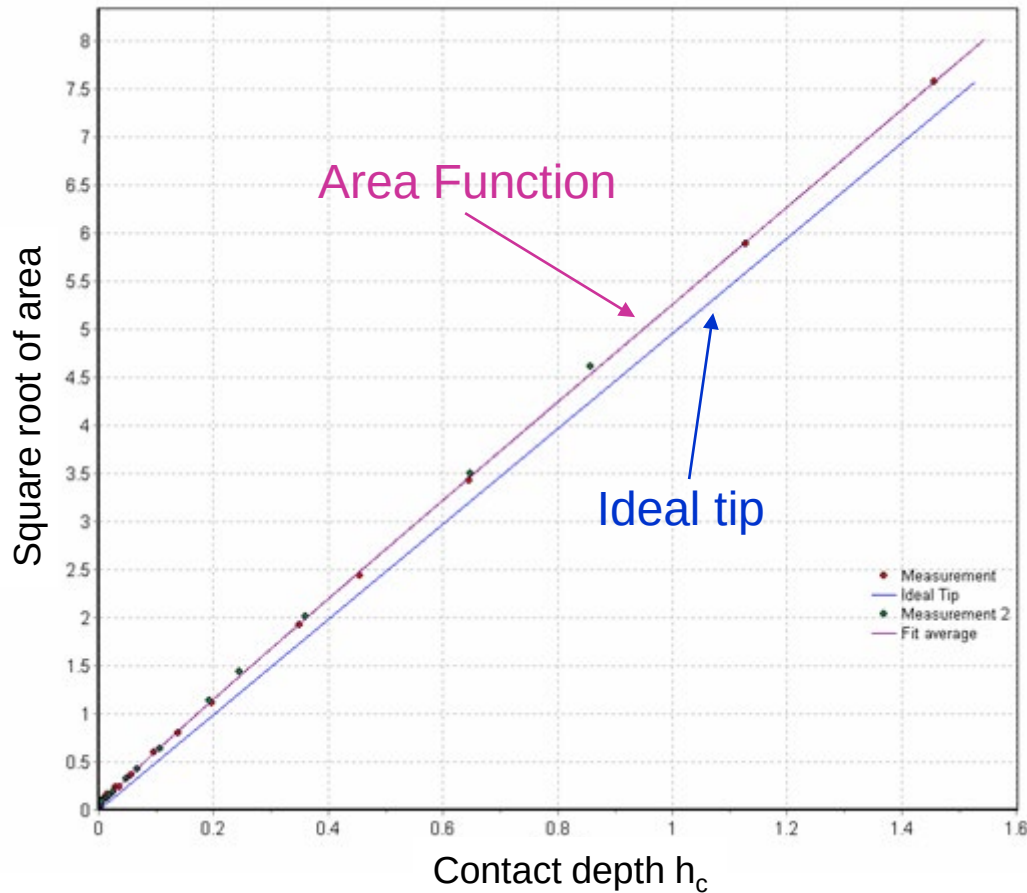


partial
unloading



complete
unloading

Determination of tip area function $A(h_c)$



Reference Materials (typical):

Quartz $E = 72 \text{ GPa}$

Sapphire $E = 420 \text{ GPa}$

Load-Displacement curves on both materials are measured at different loads (500mN - 300 μ N)

Coefficients are adjusted to obtain the best modulus values for both reference values

$$\sqrt{A(h_c)} = a_0 + a_1 \cdot h_c^{0.25} + a_2 \cdot h_c^{0.5} + a_3 \cdot h_c + a_4 \cdot h_c^{1.5}$$

$$a_1 = 0.0955987$$

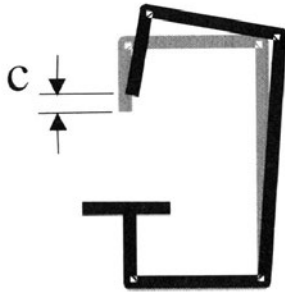
$$a_2 = -0.214813$$

$$a_3 = 0.462383$$

$$a_4 = 4.78958$$

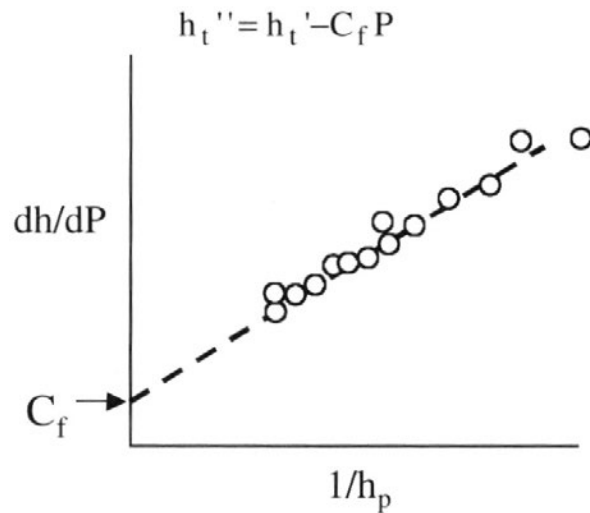
$$a_5 = 0.104144$$

Instrument stiffness



Problem: stiffness of the machine

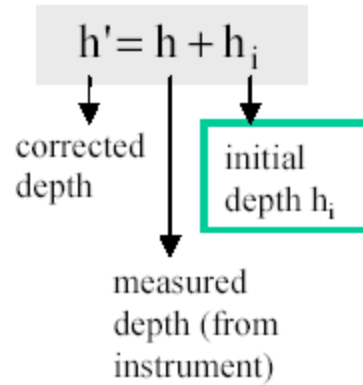
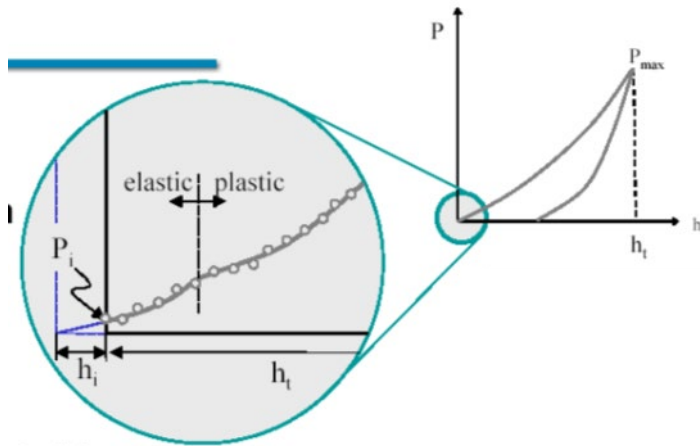
$$\frac{dh}{dP} = \frac{1}{S} + C_f$$



Use reference materials with known E

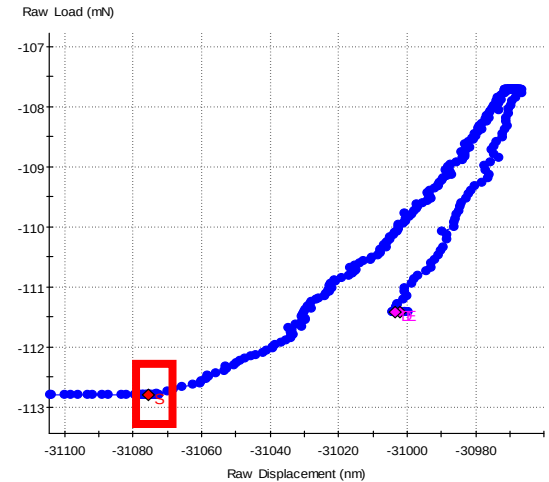
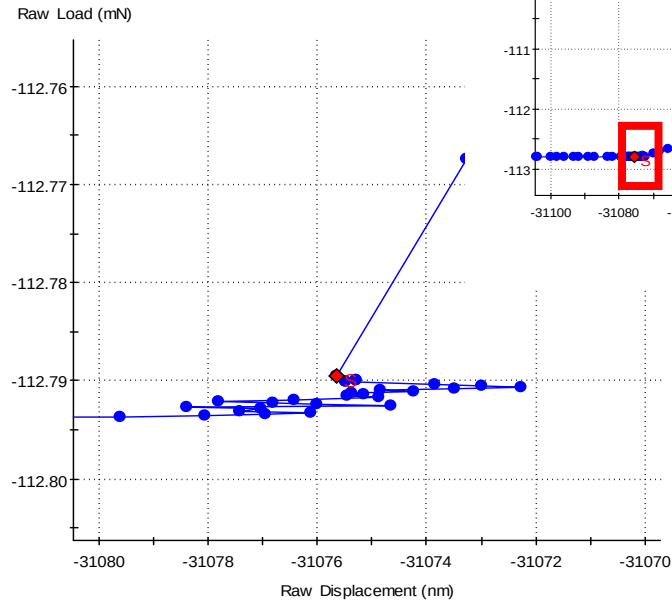
$$\frac{dh}{dP} = \sqrt{\frac{\pi}{24.5}} \frac{1}{2E^*} \frac{1}{h_p} + C_f$$

Surface Detection



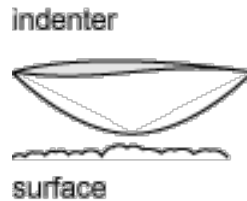
How to estimate h_i ?

1. Estimate by eye the intercept with the depth axis
2. Fit a polynomial by least squares method to the initial loading data and extrapolate back to zero load.
3. Fit the Hertz equations for elastic contact to the initial loading data and extrapolate back to zero load.



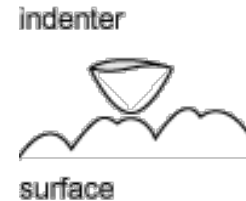
Surface Roughness

Low surface roughness



well-defined

High surface roughness

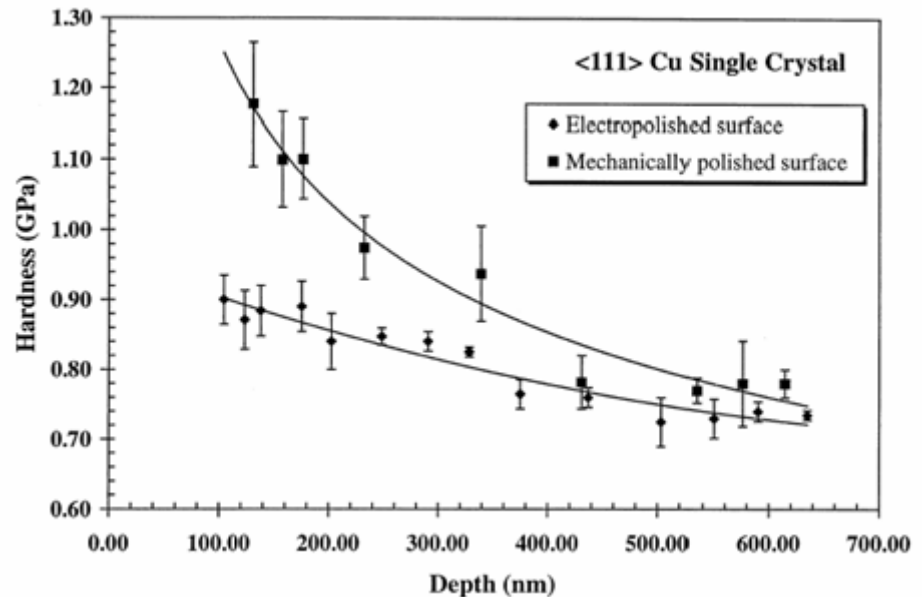


ill-defined

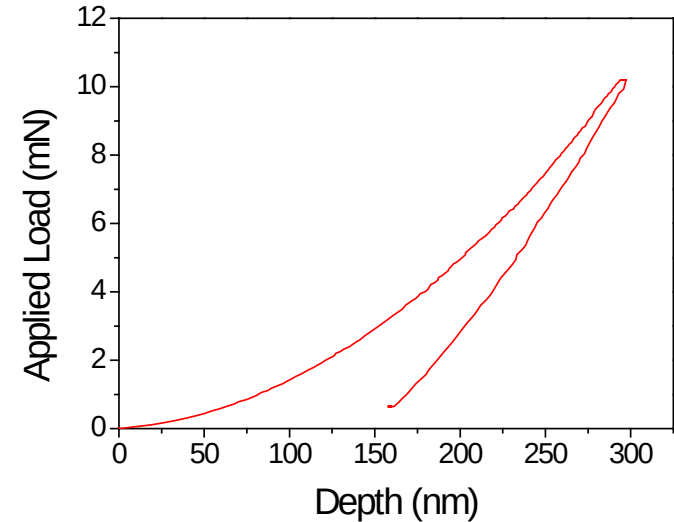
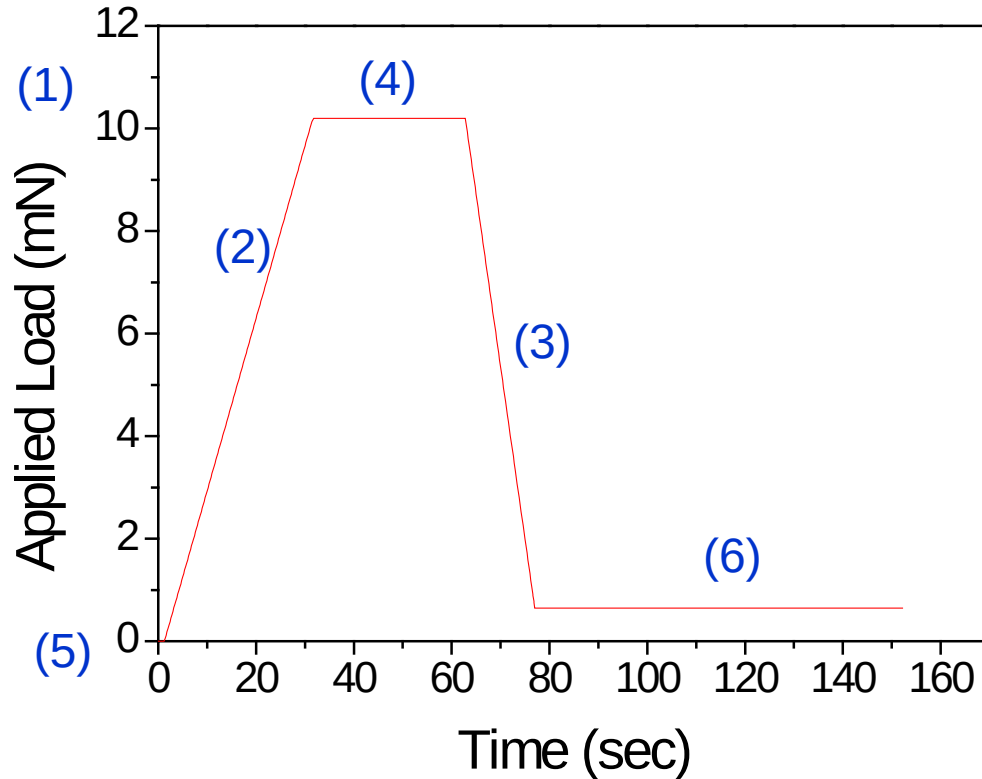
Contact Area

"Rule": $h_{\max} > 20 R_a$

Caution:
Polishing the sample surface results in a reduced roughness but considerable work hardening may occur



"A typical measurement"

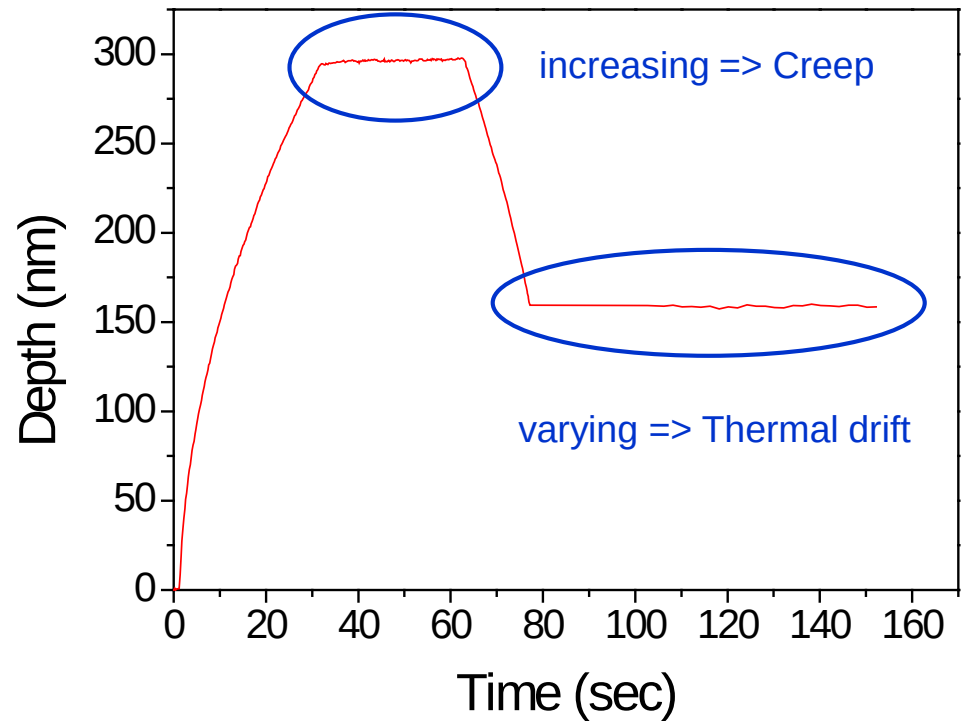
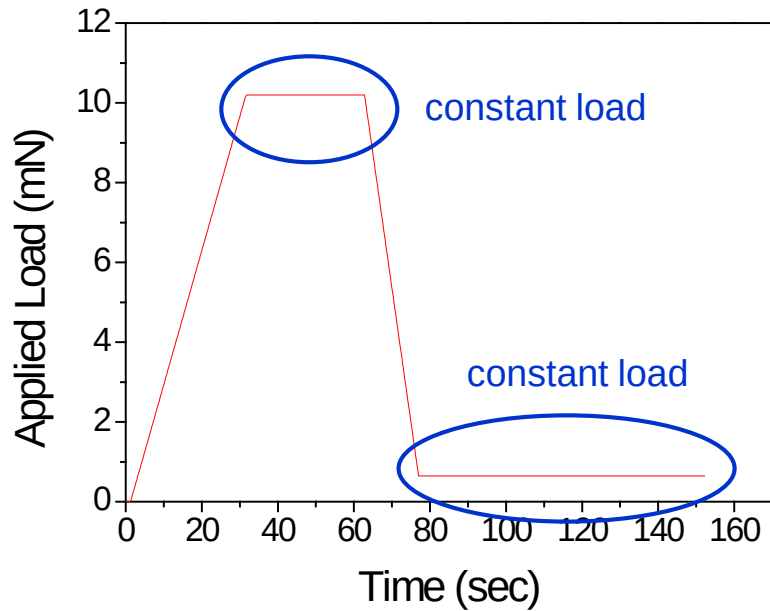


The loading - unloading cycle is **load-controlled**
Normally a **constant load rate** is used

Input Parameters:

- (1) $F_{\max}$
- (2) Time to load / loading rate
- (3) Time to unload / unloading rate
- (4) Hold period @ $F_{\max}$
- (5) Load for 2nd hold period after partial unloading
- (6) Period of 2nd hold period after partial unloading

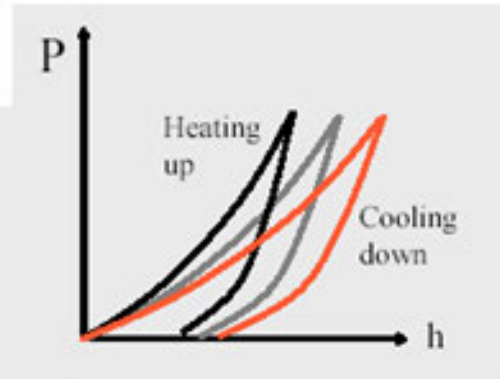
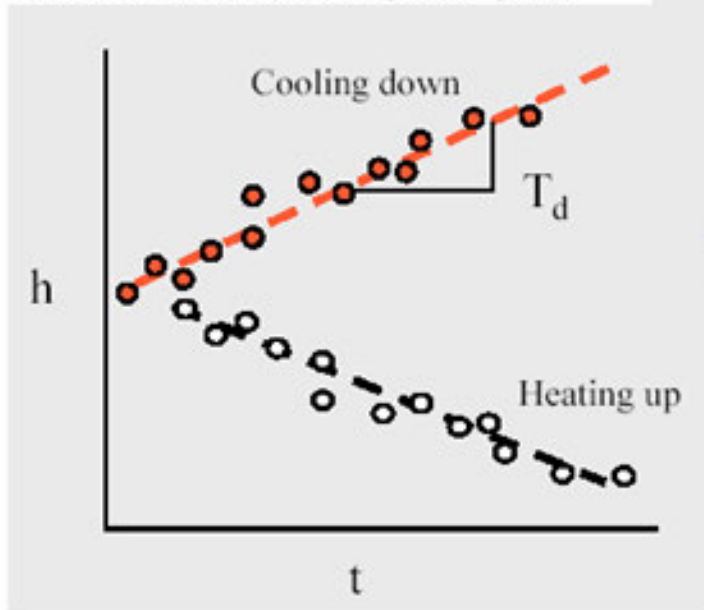
Hold periods



Thermal drift

How to estimate T_d ?

Thermal drift data taken during “hold” period



$$h' = h - T_d \cdot t$$

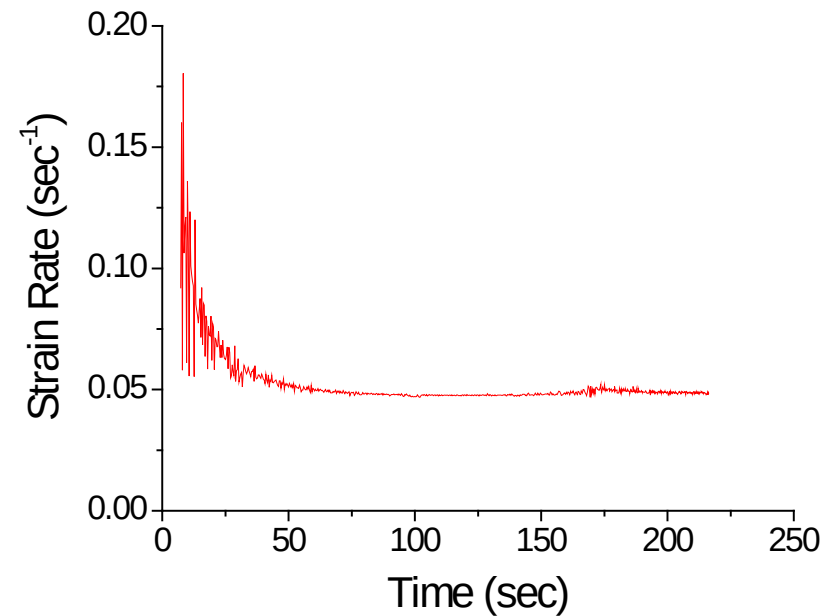
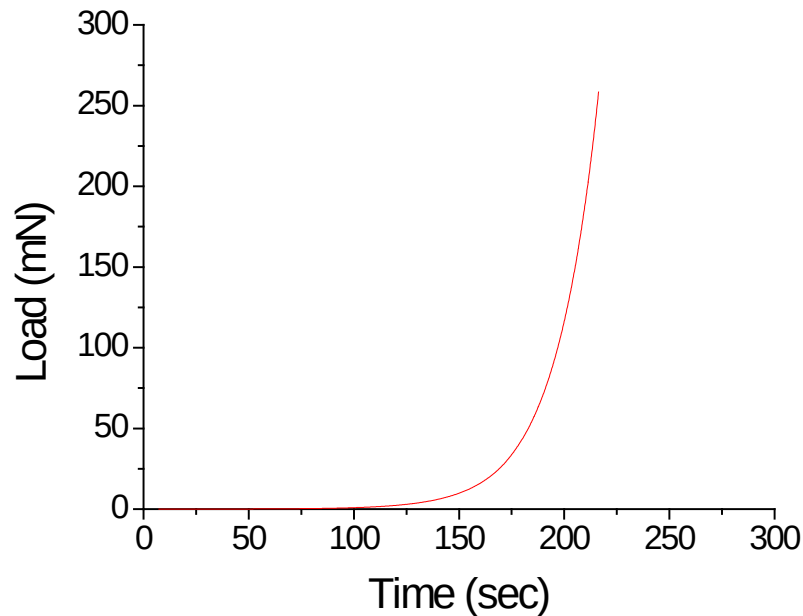
Typical drift values below 0.05 nm/sec
(for MTS Nanoindenter @ Empa Thun)

Strain rate in indentation tests

Tensile are normally performed with displacement-controlled machines at constant strain rate

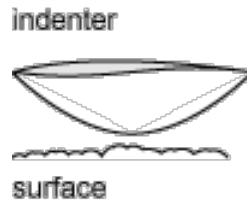
With pyramidal indenters it is possible to perform constant strain rate experiments with load-controlled nanoindenters

$$\dot{\varepsilon} = \frac{\dot{P}}{P} = \frac{\dot{h}}{h} = \text{const}$$



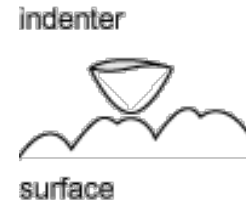
Surface Roughness

Low surface roughness



well-defined

High surface roughness

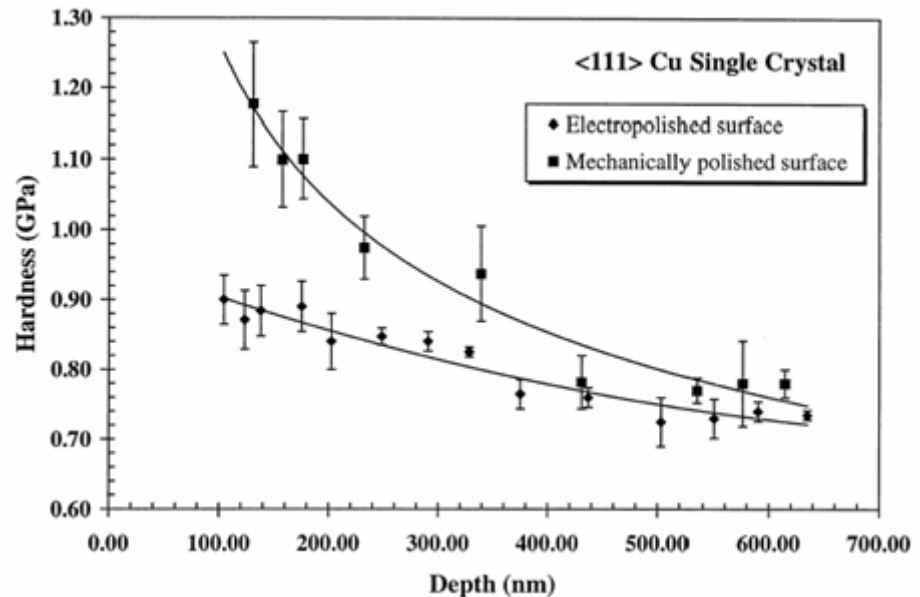


ill-defined

Contact Area

"Rule": $h_{\max} > 20 R_a$

Caution:
Polishing the sample surface results in a reduced roughness but considerable work hardening may occur

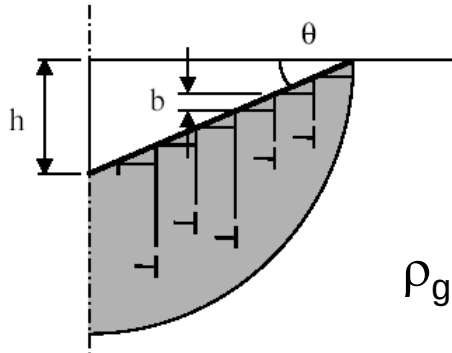


Indentation Size Effects (ISE)

Soft materials (Fe, Al, Cu) with surface contaminant layers (oxides, carbides)

=> dislocations pinned

=> higher hardness values @ small indentation depths



$$\rho_g = \frac{3}{2bh} \tan^2 \Theta$$

ρ_g : dislocation density

circular dislocation loops serve to increase the effective yield strength

Nix & Gao, J. Mech. Phys. Solids 46(3) 1998, pp. 411-425

Other ISE effects:

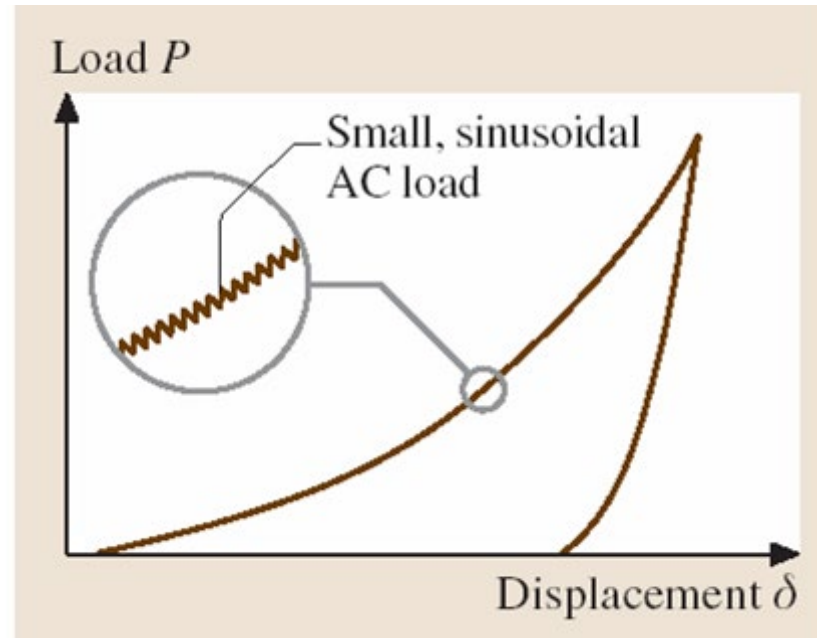
- Real shape of indentation pyramid
- Sample surface roughness, surface polishing

Dynamic Contact Models

Principle:

A small AC load is superimposed to the DC load.

The contact stiffness S can be calculated throughout the complete indentation cycle.



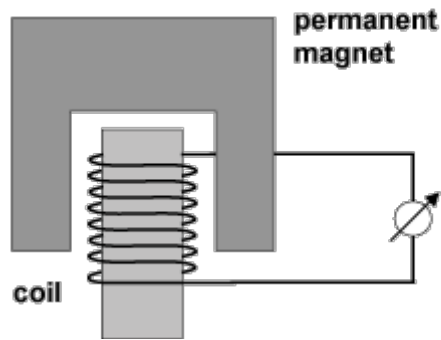
Typical frequency ≈ 60 Hz

The AC load creates a dynamic system with the sample acting as a spring with stiffness S (contact or unloading stiffness) and the nanoindentation system as a series of springs and dampers

Nanoindentation equipment: load actuation & displacement measurement

Load actuation

Electromagnetic actuation:



Advantages:

- long displacement range (up to mm)
- linear current-load behavior
- wide load range (mN to N)
- can be used to pick up the indenter as well as to push it down

Disadvantages:

- large ($\approx 10\text{cm}$) and heavy (order of kg)
- current in the coil $\Rightarrow$ heat $\Rightarrow$ thermal drift

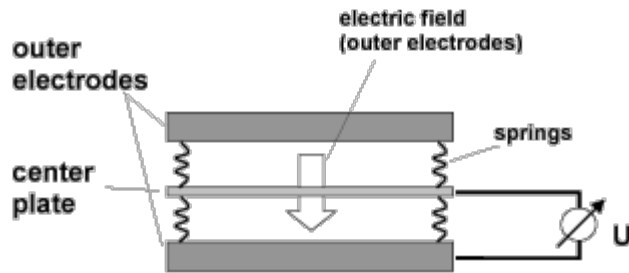
By varying the current, I , through the coil, a magnetic field is generated that interacts with the magnetic field of the permanent magnet.

Calibration:

Hanging a series of weights to the indenter shaft and recording the load current to lift the shaft to the same position for each weight

Load actuation

Electrostatic actuation:



Advantages:

- small size of the system (in the order of tenths of mm)
- good temperature stability

Disadvantages:

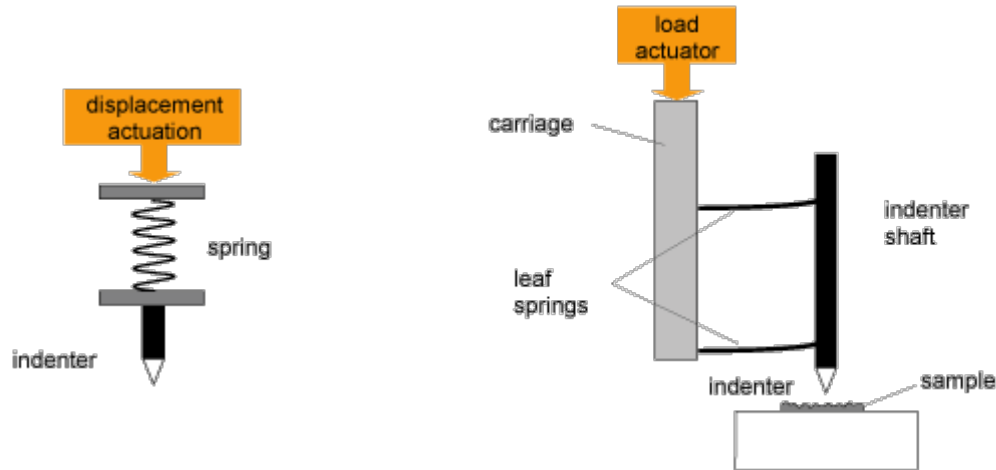
- limited load range (in the order of tenths of mN)
- limited displacement range (in the order of tens of μm)
- usually only one possible direction of tip movement

The load is applied by an electrostatic force generated between the center plate and the upper or lower plate of a three-plate transducer system.

The applied load is proportional to the square of the voltage.

Load actuation

Actuation through springs:



Range vs. resolution: In principle, very high force resolutions are possible. Cantilever based devices commonly report force resolutions in the pN range, or better. However, as resolution goes up, range goes down.

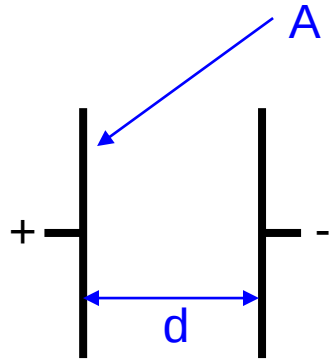
Geometric stability: One of the main disadvantages of using a cantilever is that the tip rotates as the load on it is increased.

Force response: The higher the force resolution, the greater are the displacements needed to change that force. The rate at which the force can be changed is limited in such machines.

Calibrations: Force calibration depends on accurate knowledge of the spring constant and the relative displacements.

Displacement measurement

Capacitive:



Parallel plate capacitor:

$$C = \frac{\epsilon\epsilon_0 A}{d}$$

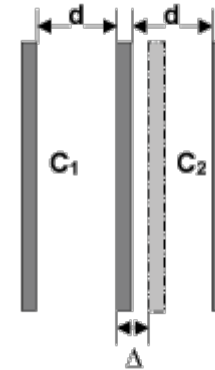
Advantages:

- can be of very high precision (resolution below $1\text{\AA}$)
- small size

Disadvantages:

- total displacement range is relatively small

Differential capacitor:



Difference between C_1 and C_2 is measured

Displacement measurement

Linear Variable Differential Transducer (LVDT):



Advantages:

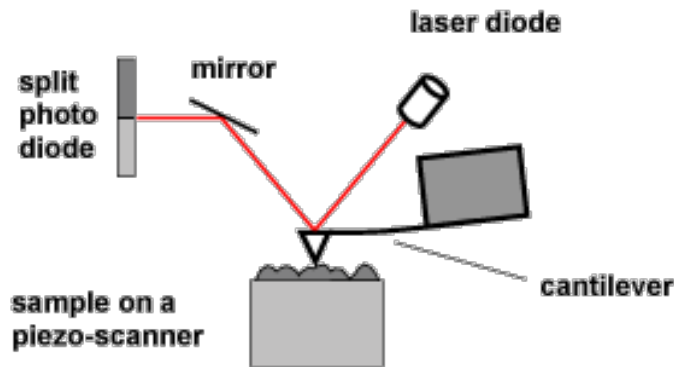
- relatively low cost due to its popularity
- solid and robust, capable of working in a wide variety of environments
- high signal to noise ratio
- negligible hysteresis
- no permanent damage to the LVDT if measurements exceed the designed range

Disadvantages:

- lower resolution compared to a capacitive displacement measurement
- core must be in contact (directly or indirectly) with the measured surface

Displacement measurement

Optical lever methods:



Used for example to measure the deflection of beams
Most of the Atomic Force Microscopes (AFM) use this principle

Very high sensitivity (below $1\text{\AA}$) is possible

Nanoindentation other experimental aspects

Nanoindentation experiments on thin films

Advantage:

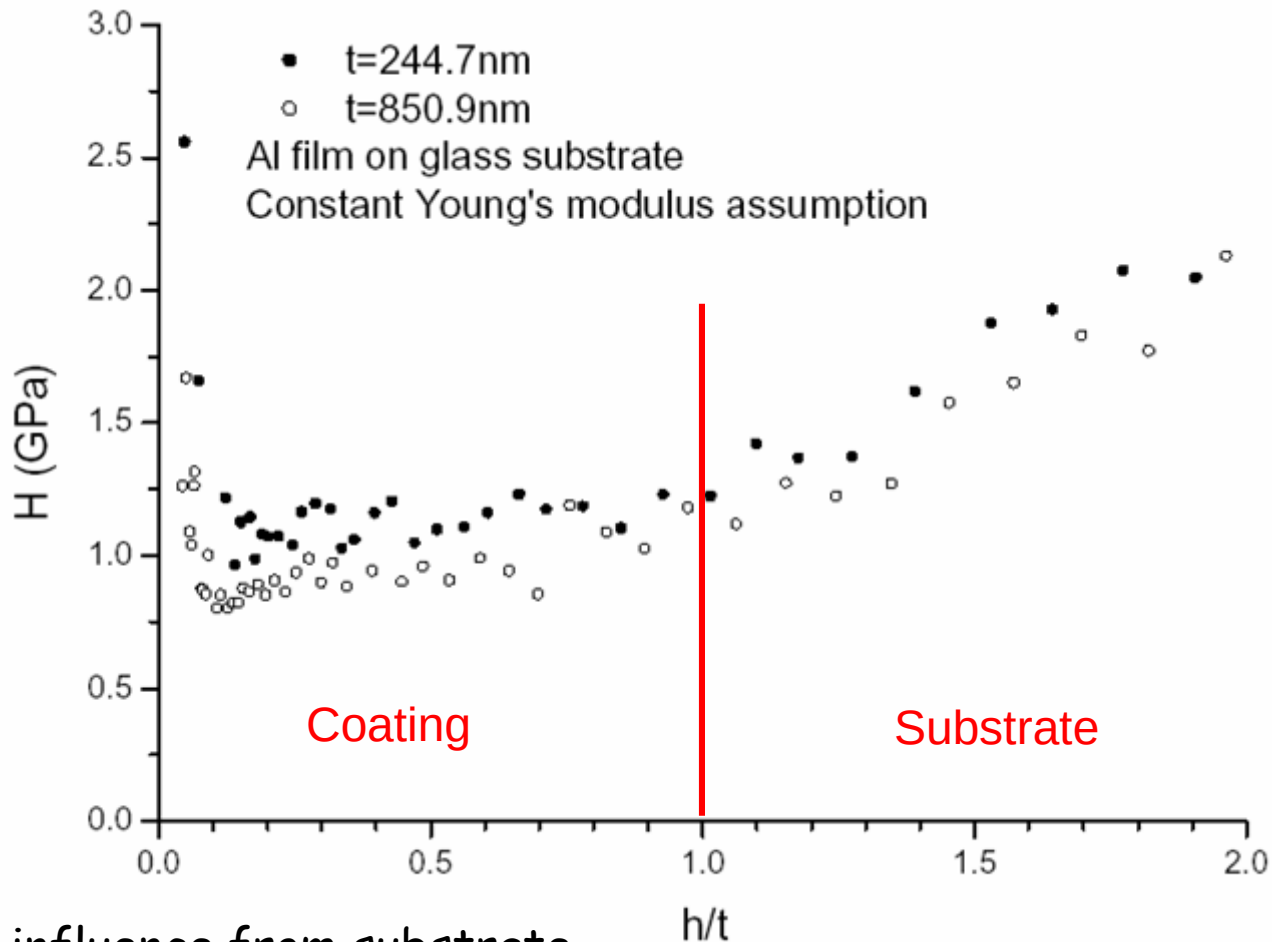
Film can be measured without removing it from the substrate
Spatial distribution in lateral & vertical direction



Chief difficulty:

Avoiding unintentional probing of substrate properties

$1\mu\text{m}$ Al on glass (soft coating on hard substrate)



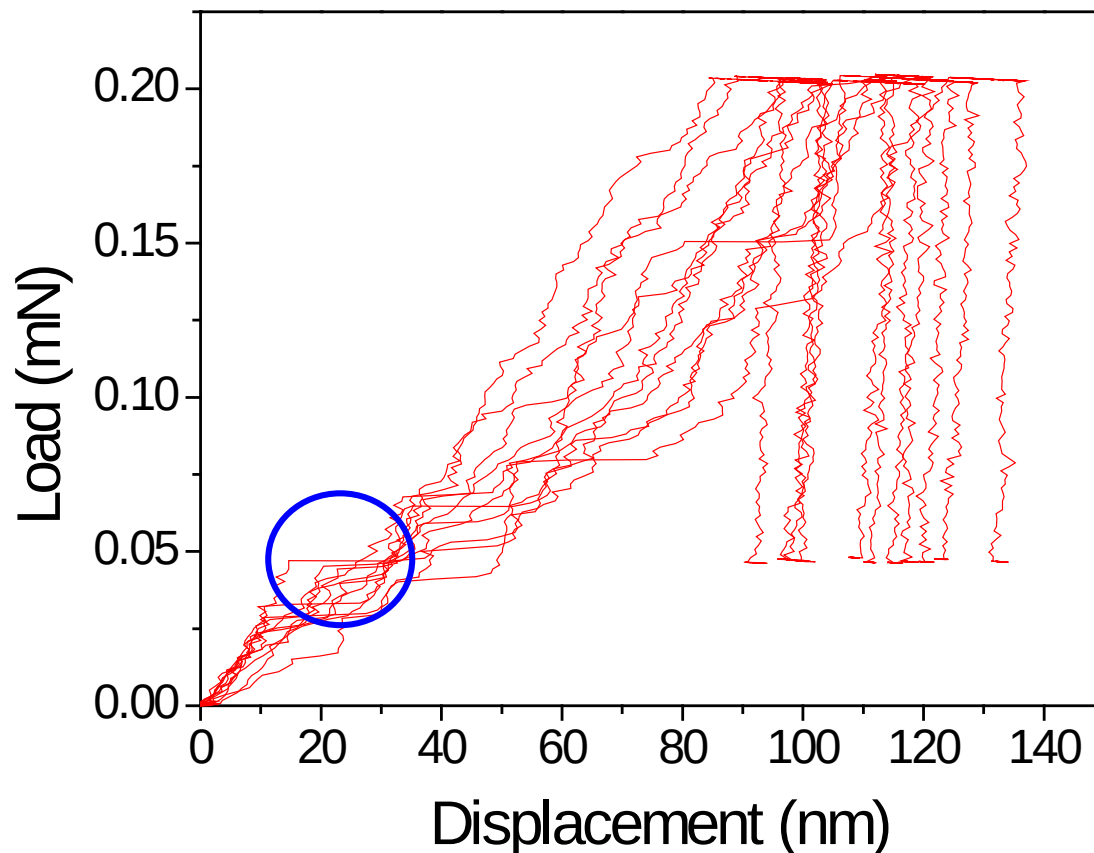
- almost no influence from substrate
- ISE observable

S. Chen, L. Liu, T. Wang, *Acta Mater.* 52 (2004), p. 1089

1 μm Al on glass: effects of surface oxide layer

Surface oxide layer breaks under load resulting in "pop-in" features in the load-displacement curve

=> Evaluation of H and E is not possible at small penetration depths



Considering the substrate properties

Soft film on hard substrate:

$$H_{eff} = H_s + (H_f - H_s) \cdot \exp \left\{ -\frac{Y_f}{Y_s} \frac{E_s}{E_f} \left(\frac{h}{t} \right)^2 \right\}$$

Hard film on soft substrate:

$$H_{eff} = H_s + (H_f - H_s) \cdot \exp \left\{ -\frac{H_f}{H_s} \frac{Y_s}{Y_f} \sqrt{\frac{E_s}{E_f}} \frac{h}{t} \right\}$$

H_{eff} : hardness of film-substrate combination

Y : Yield stress

h : penetration

t : film thickness

„Finite element simulation of indentation experiments“

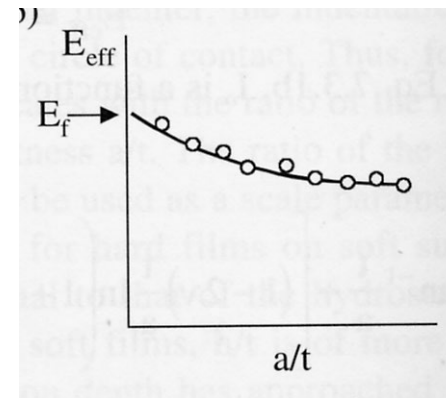
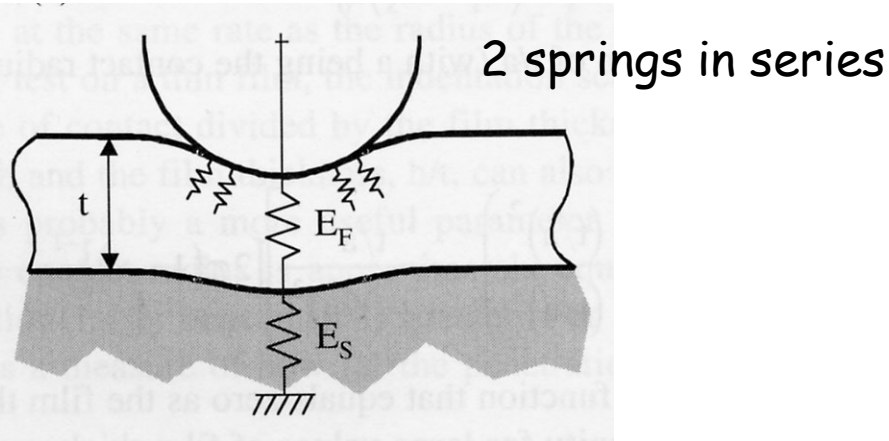
Bhattacharya and Nix, Int. J. Solids Structures 24, 1988, 1287-1298

BUT:

There is no one relationship which covers a wide range of materials behaviour

Young's modulus

Evaluating E for different a/t values
 $\Rightarrow$ extrapolating to E_f



$$\frac{dP}{dh} = \beta \frac{2}{\sqrt{\pi}} E_{eff} \sqrt{A} \left[\frac{\frac{(1-\nu_s^2)}{E_s} + \frac{(1-\nu_i^2)}{E_i}}{\frac{(1-\nu_f^2)}{E_f} (1-e^{-\alpha t \sqrt{A}}) + \frac{(1-\nu_s^2)}{E_s} (1-e^{-\alpha t \sqrt{A}}) + \frac{(1-\nu_i^2)}{E_i}} \right]$$

a : penetration depth
 β : depends on the indentation tip geometry

t : coating thickness
 α : empirical constant, determined from a series of experiments

R.B. King, Int. J. Solids Structures 23(12), 1987, pp. 1657-1664

"1/10-rule of thumb"

Rule of thumb by H. Bückle:

($h_{\max}$ = maximal depth; d_{Film} = film thickness)

$$h_{\max} \leq 0.1 \cdot d_{\text{Film}}$$

For the "extreme" cases of a hard film on a soft substrate (Nanocomposite coatings)
or for a soft coating on a hard substrate (Al on glass)

this rule may be too lax or too strict

H. Bückle, VDI Berichte, Vol. 41, p. 14, 1961

Choice of applied maximal load / maximal displacement

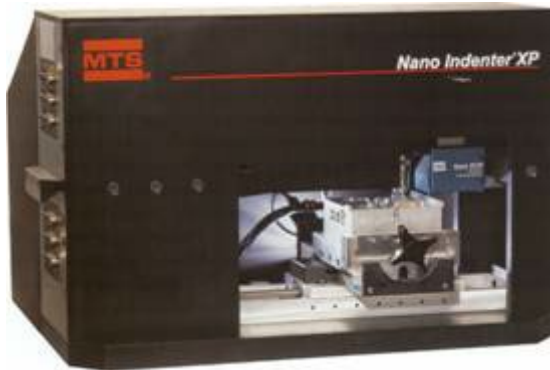
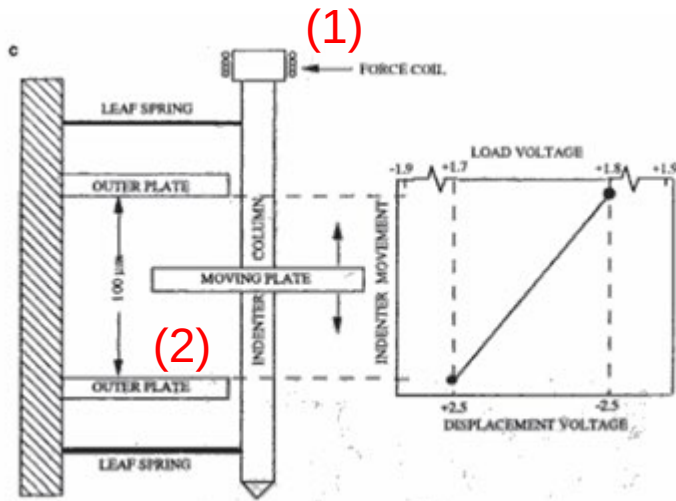
Rules:

- Displacement $> 20 R_a$
- Displacement $\leq 10\%$ of coating thickness

Nanoindentation equipment: Commercial Nanoindenters

MTS Nanoindenter XP / KLA Tencor NanoIndenter G200

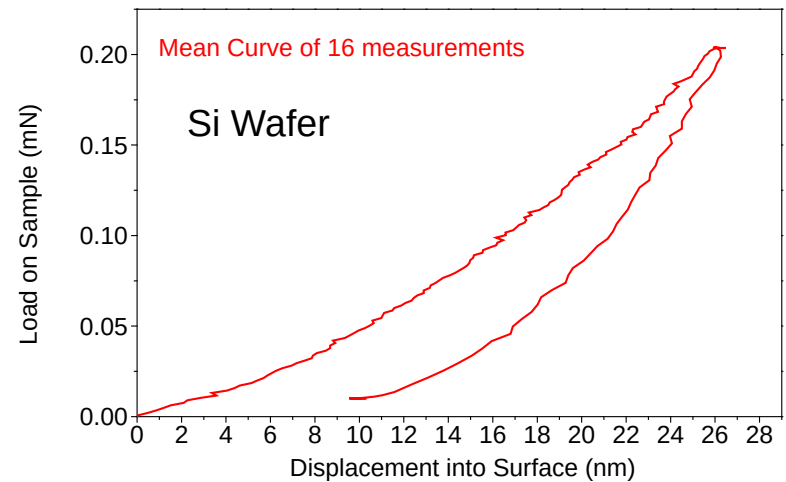
- (1) Inductive Force Generation
- (2) Capacitive Displacement Measurement



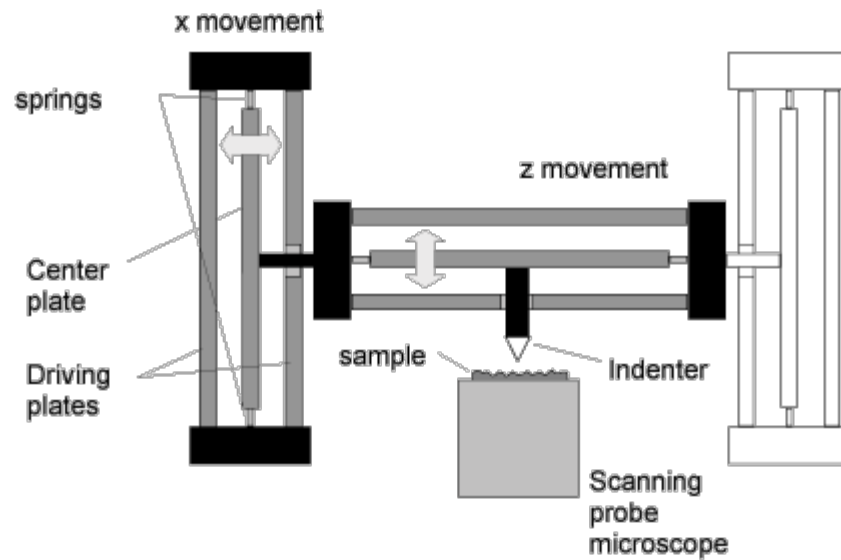
MTS Nanoindenter XP installed @ Empa in Thun:

Displacement resolution	< 1 nm
Maximum indentation depth	500 μm
Minimal peak load	100 μN
Maximum load	500 mN
Load resolution	50 nN
Lateral position accuracy	$\pm 1 \mu\text{m}$

Scratch option with lateral force measurement
(Measurement of Friction Coefficient)



Hysitron Tribo-Scope / Ubi



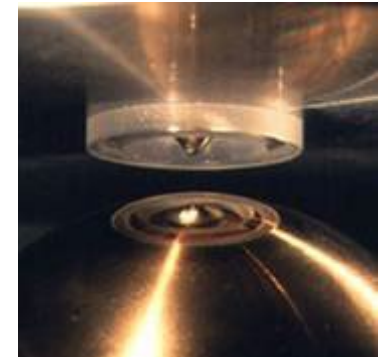
Transducer Specifications

- Load
 - Resolution: $<1\text{nN}$
 - Noise Floor: 100nN
- Displacement
 - Resolution: 0.0002nm
 - Noise Floor: 0.2nm
 - Drift: $<0.05\text{nm/sec}$

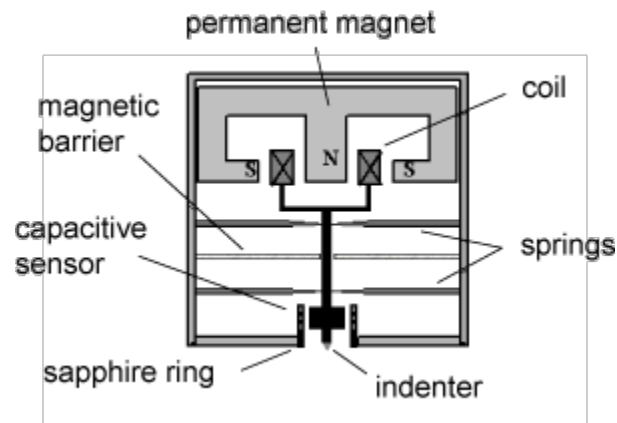
CSM Instruments Nano-Hardness Tester

Indentation Testers Specifications

	Micro	Nano
Maximum Load	10 N (30 N optional)	500 mN
Load Resolution	100 μ N	0.04 μ N
Maximum Depth	0-20 & 0-200 μ m (1 mm optional)	0-20 & 0-200 μ m
Depth Resolution	0.04 & 0.3 nm	
XY stages (*)	120 mm x 20 mm	
XY resolution	0.25 μ m	

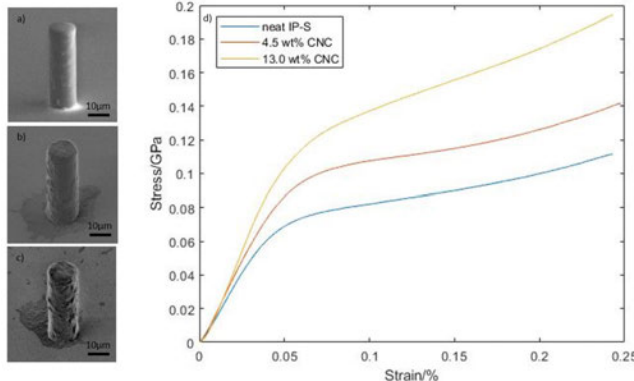
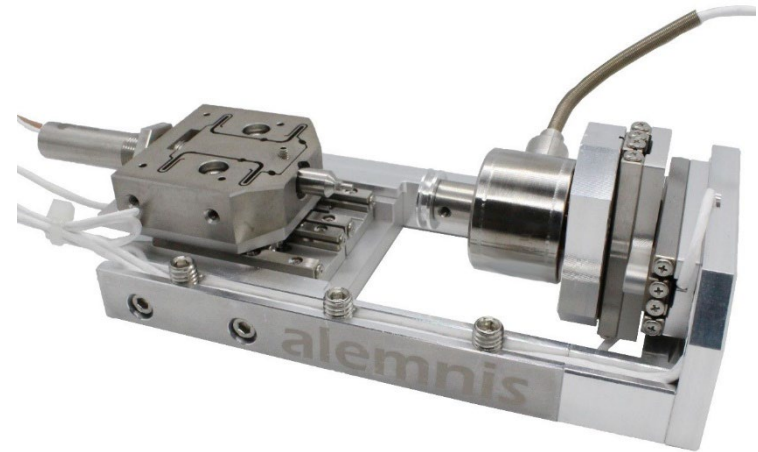


Surface reference by contact with a ring



Alemnis in situ indenter

- In situ experiments inside the SEM
- Actuation: Piezo
- Load, displacement measurement: Strain gauges
- Load range: Up to 2.5N
- Load noise: 4 μ N
- Displacement range: 40 μ m
- Displacement noise: 0.2 nm

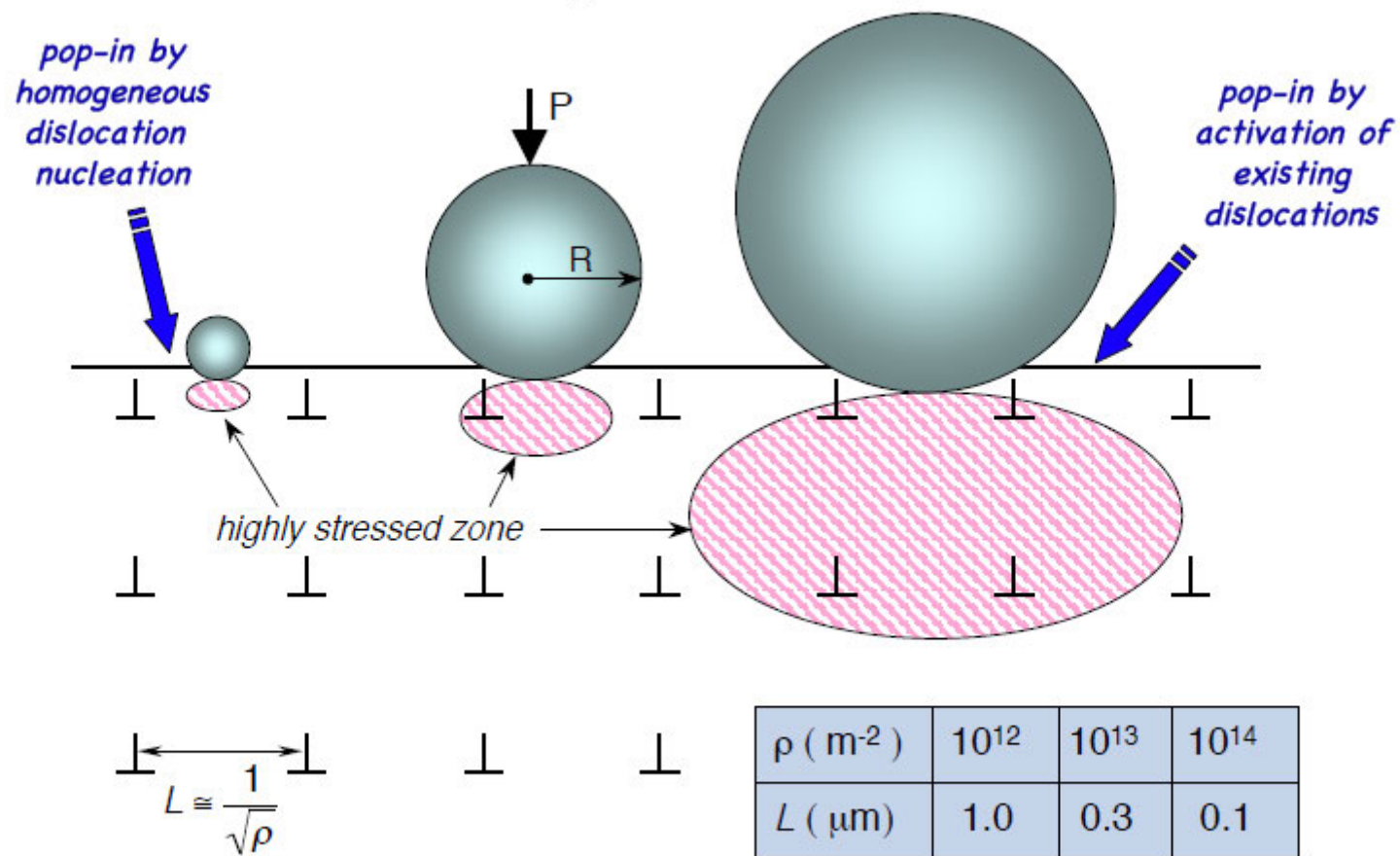


- Variable temperature modules (-150°C to 1000°C)
- High strain rate module (up to 1000/s)

What happens in the material?

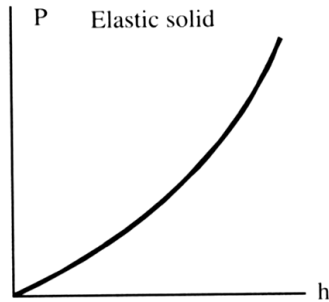
- Sink-in and pile-up around the tip (α -Me)
- Densification and phase transformation (Remy)
- Dislocation nucleation and grain boundary sliding (Sid etc.)
- Creep
- Crack propagation

Pop-in and defect microstructure

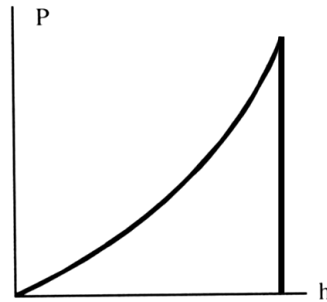


40

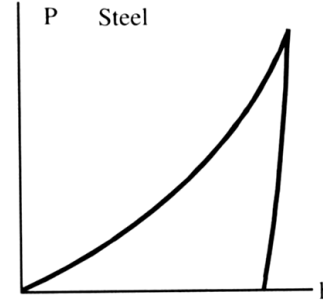
Typical load displacement curves



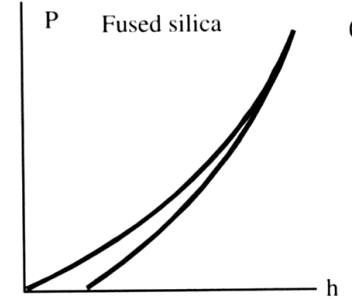
Elastic Solid



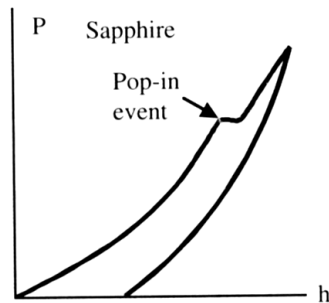
Fully plastic



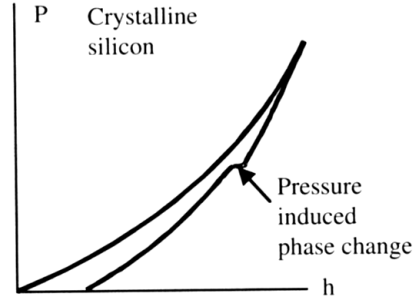
Ductile Solid
(Steel)



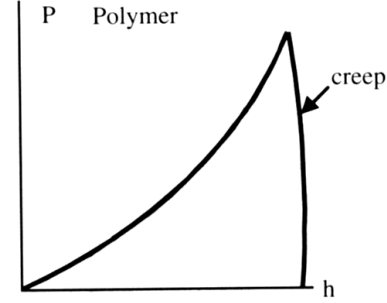
Brittle Solid
(Fused Silica)



Brittle Solid
Cracking during
loading



Pressure induced
phase change
(Silicon)



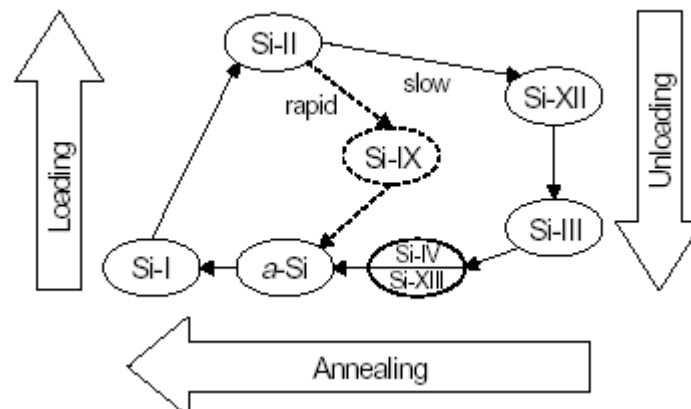
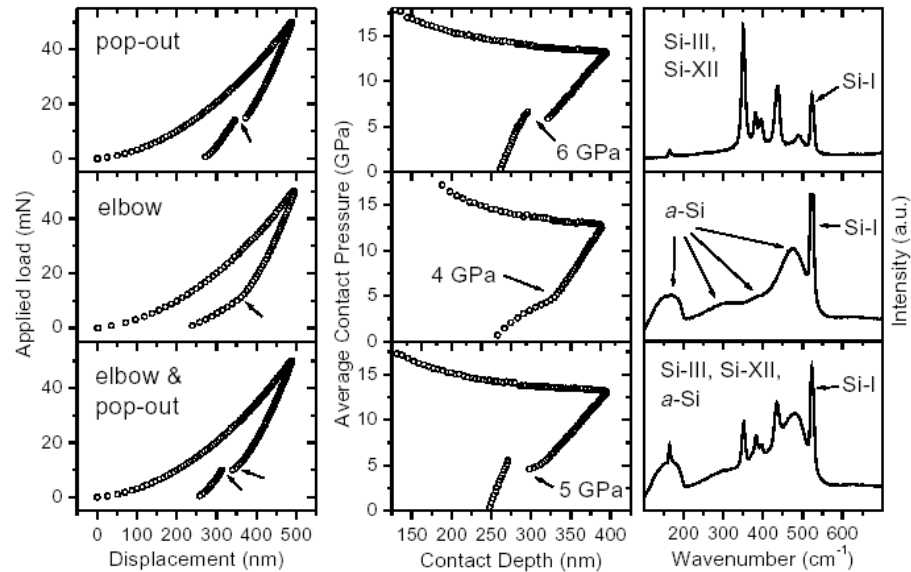
Polymer exhibiting
creep

phase transformations in silicon

slow ($<1\mu\text{m/s}$)

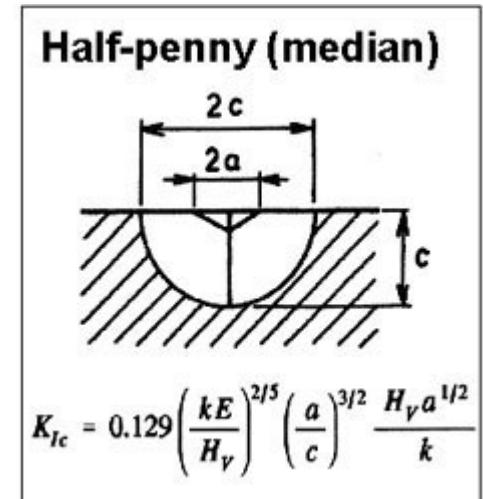
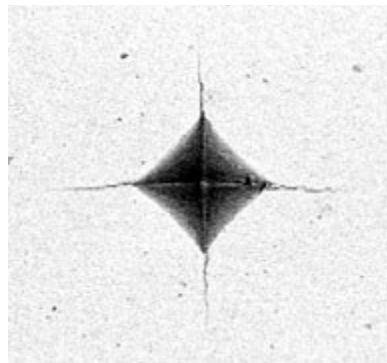
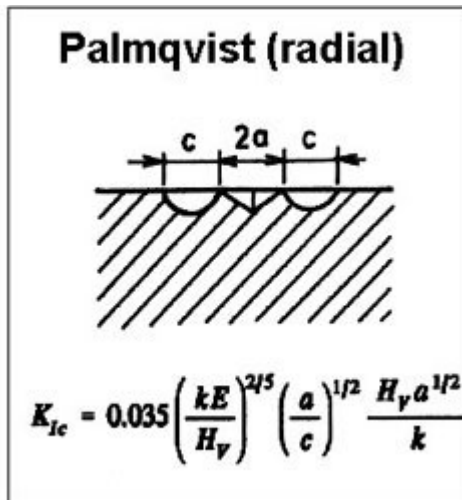
fast ($>100\mu\text{m/s}$)

intermediate



Fracture toughness

Determine K_{Ic} : measure size of residual impression a and crack length c

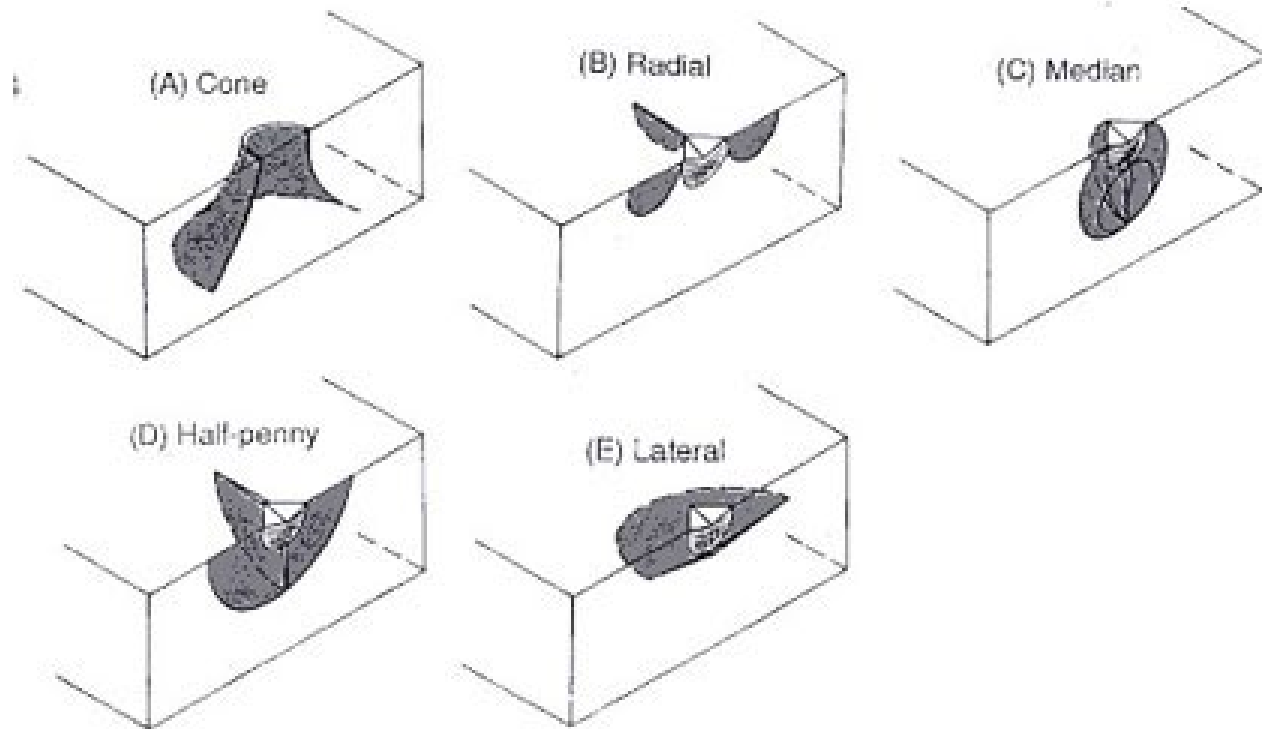


Probleme:

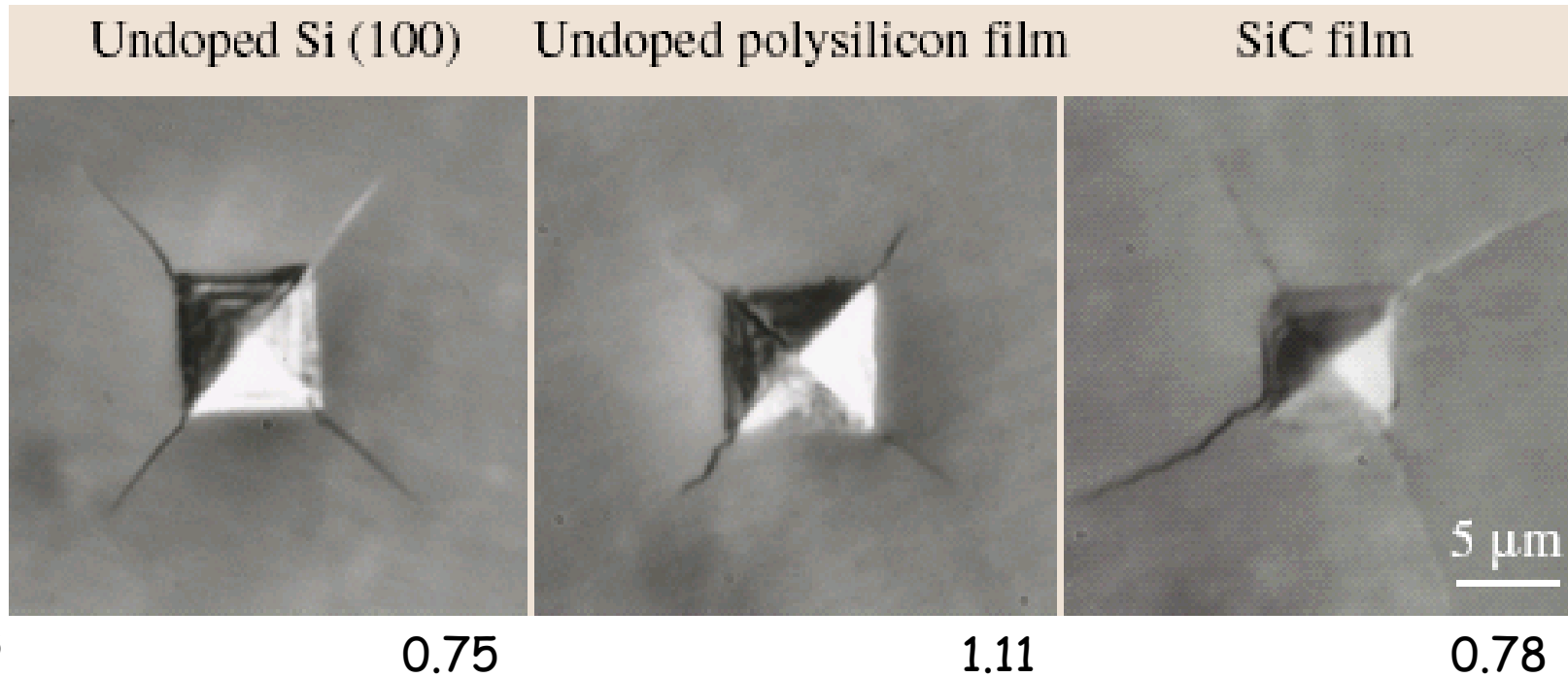
- precision of length measurement
- Crack morphology
- When is crack generated?
- Model is material specific

Fracture toughness

Possible crack modes



Example: fracture toughness



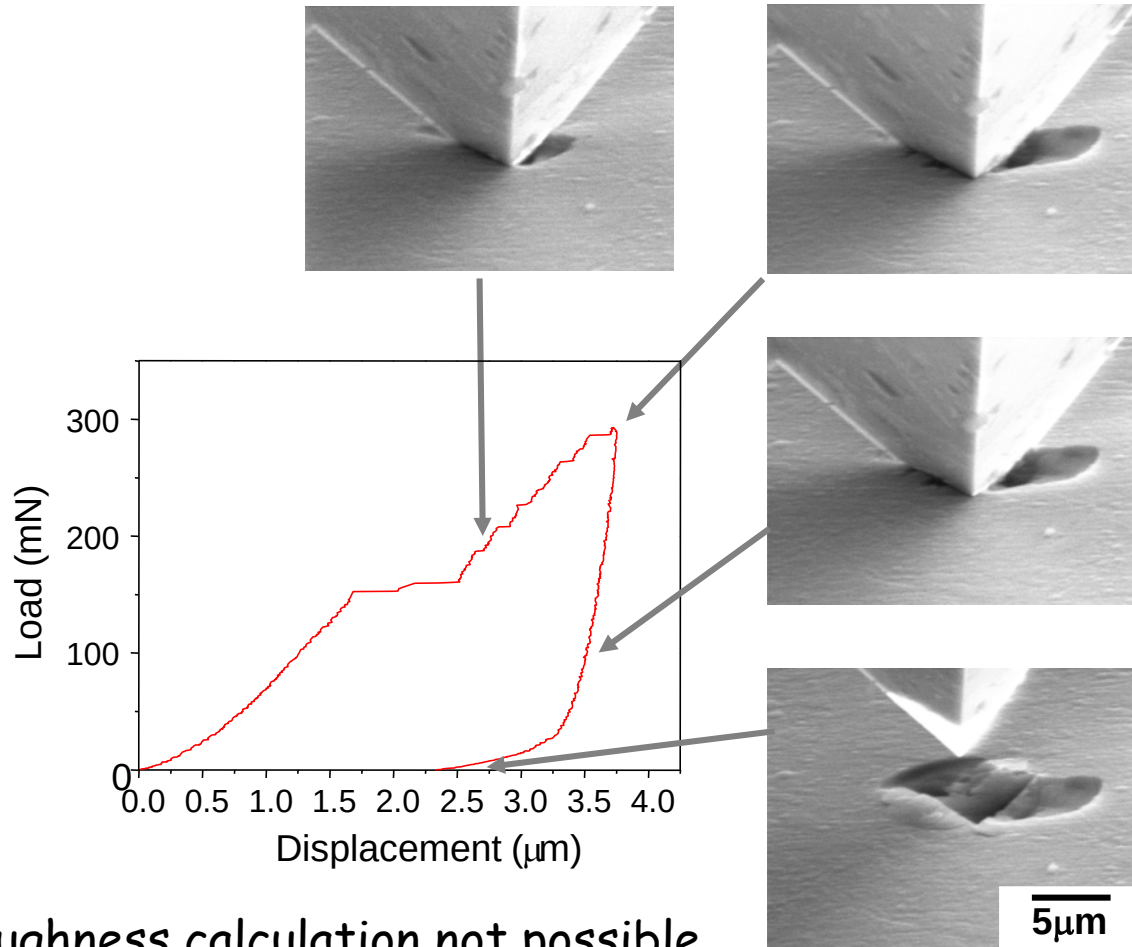
(Half- penny crack model)

Example: fracture toughness

Indenter:
cube corner

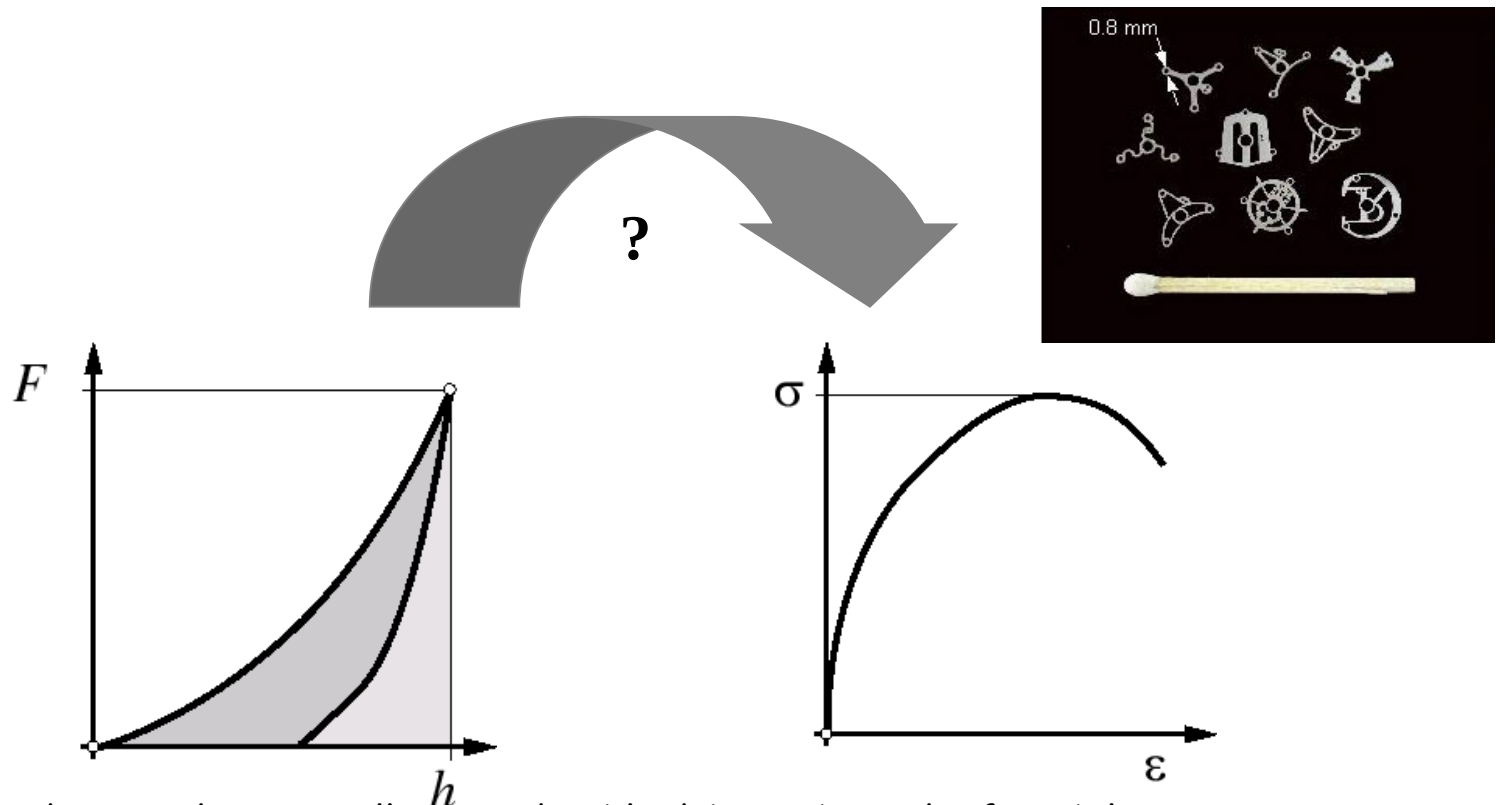
coating:
a-C:H mit 20at% Si
3.5 μm thickness
H=8GPa

Substrate:
(X155CrMoV121)



Lateral cracks form: toughness calculation not possible

Stress-strain curves from indentation

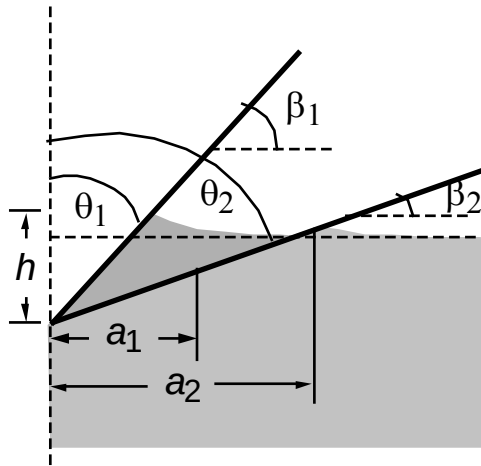


For conical type indenters, there is still a considerable debate about the feasibility:
Cheng YT, Cheng CM (1999) J Mater Res 19, 3493.
Venkatesh TA, Van Vliet KJ, Giannakopoulos AE, Suresh S. (2000) Scripta Mater 42, 833

Can we at least develop a robust practical method by pure numerical methods?

idea: combination of experiments

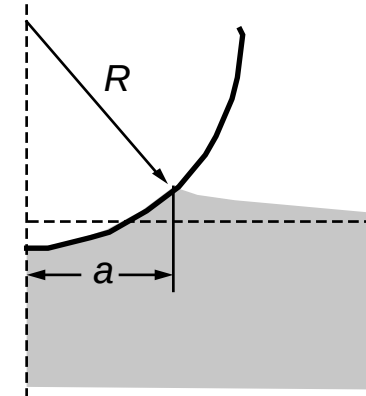
Conical tips



$$\varepsilon \sim \frac{h}{a} \sim \cot \Theta$$

Johnson, K.L.: Contact Mechanics, 1985.

Spherical tip

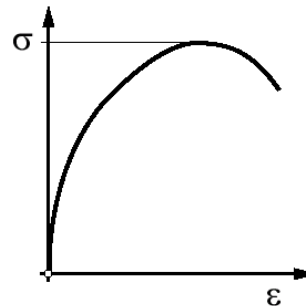


$$\varepsilon \sim \frac{a}{R}$$

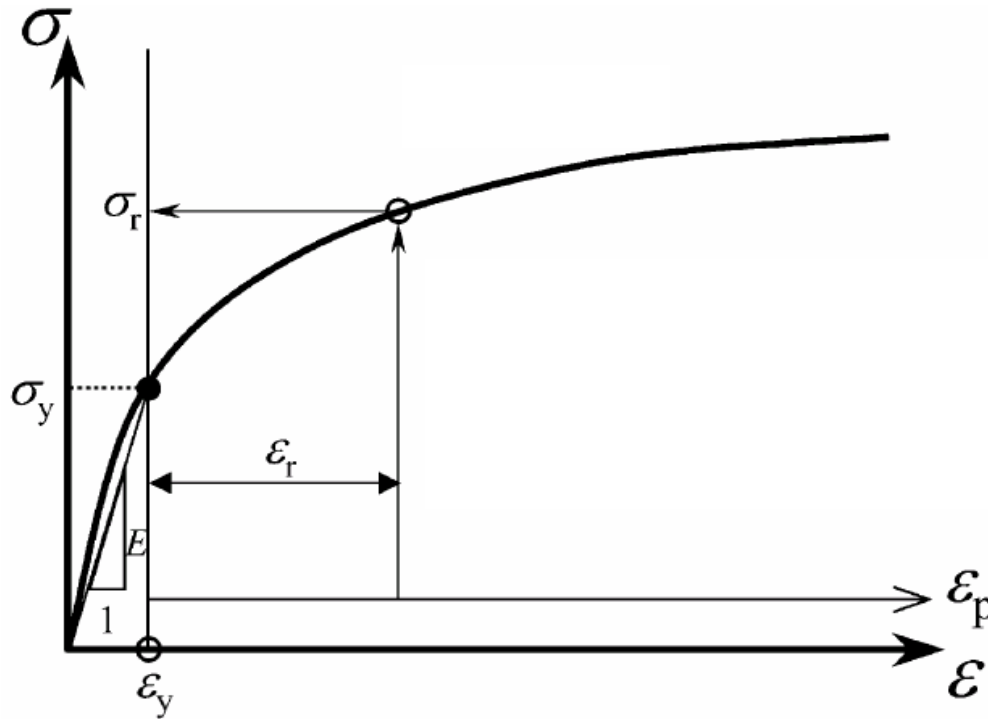
Tabor, D.: The Hardness of Metals, 1951

combine several
experiments
with varying cone angle

combine
load displacement data
with residual profile



some definitions



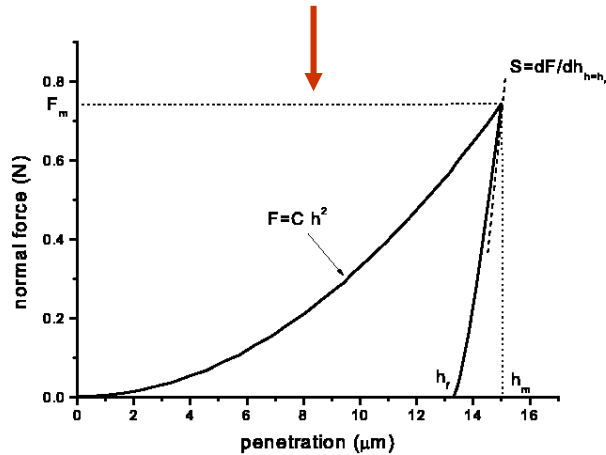
$$\sigma = \begin{cases} E\varepsilon & \varepsilon < \varepsilon_y \\ \sigma_y \left(1 + \frac{E}{\sigma_y} \varepsilon_{pl} \right)^n & \varepsilon > \varepsilon_y \end{cases}$$

ε = true strain, σ = true stress

We can describe the elastic behavior by E (ν)
and the plastic behavior by σ_y and n

conical tips: algorithm I

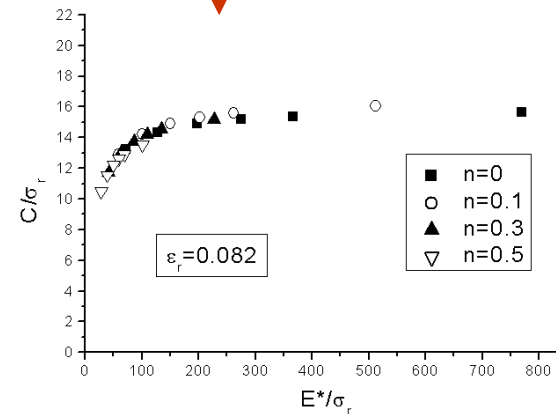
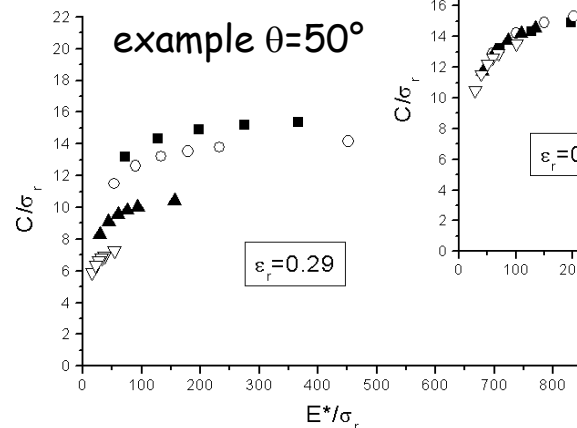
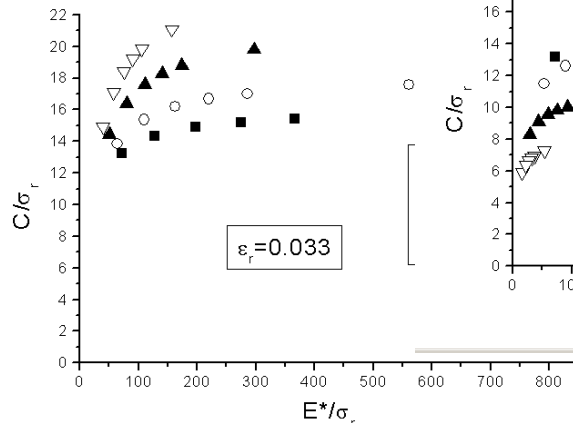
parametric finite element calculations of a large set of typical E , σ_y , n and θ



modeling of loading: $F = Ch^2$

for a given θ find representative ε_r for that all C/σ_r and E^*/σ_r are superimposed on one curve (Dao, Acta Mater. (2001),
→ average total strain independent on strain hardening

F-h for a large number of combinations of σ_y , n , θ

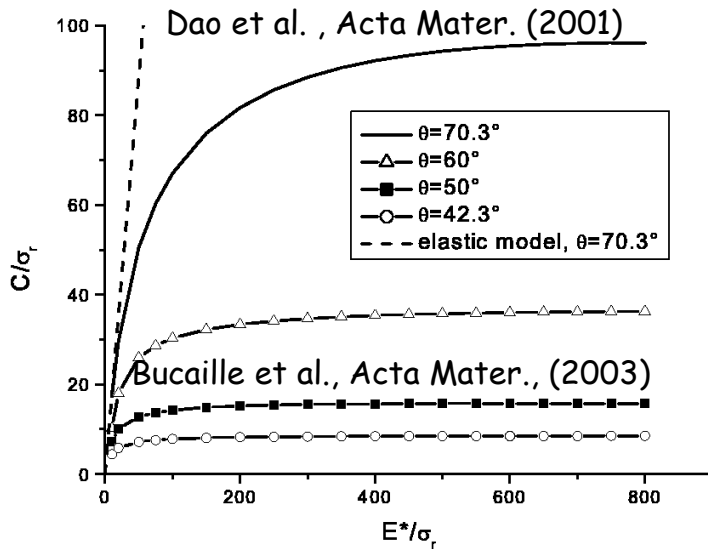


calculate back σ_y , n

Dao, Acta Mater. (2001)

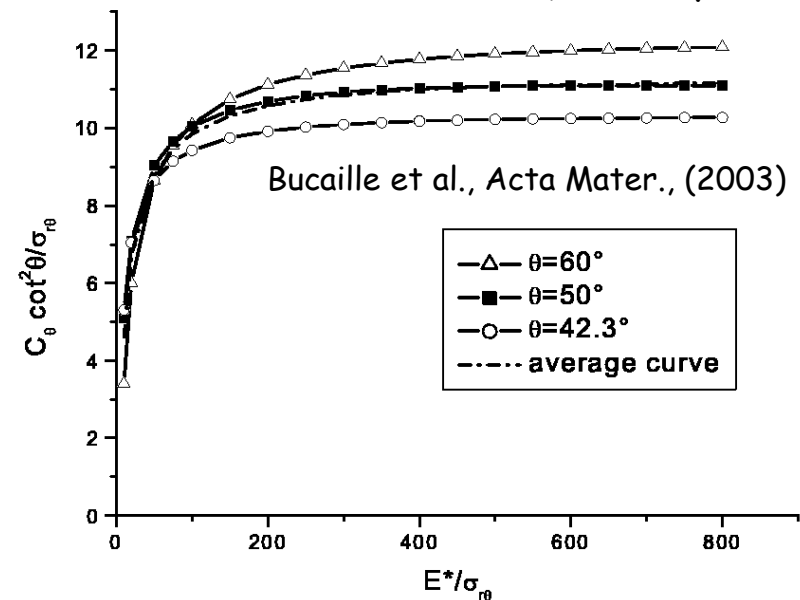
conical indenters: algorithm II

normalized dimensionless functions



master curve:

relation between C and E , σ_r for any value of θ



representative **strain**

$$\varepsilon_r = 0.105 \cot \theta$$

and the corresponding **stress** computed with the Π_1 function below:

$$\Pi_{1\theta} = \frac{C_\theta}{\sigma_{r\theta}} = \tan^2 \theta \left\{ 0.02552 \left[\ln \left(\frac{E^*}{\sigma_{r\theta}} \right) \right]^3 - 0.72526 \left[\ln \left(\frac{E^*}{\sigma_{r\theta}} \right) \right]^2 + 6.34493 \left[\ln \left(\frac{E^*}{\sigma_{r\theta}} \right) \right] - 6.47458 \right\}$$

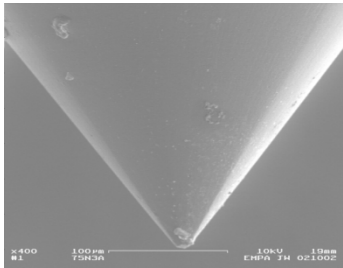
-> two simple formula based on E^* , C_θ from experimental load-displacement data

conical indenters: experiment

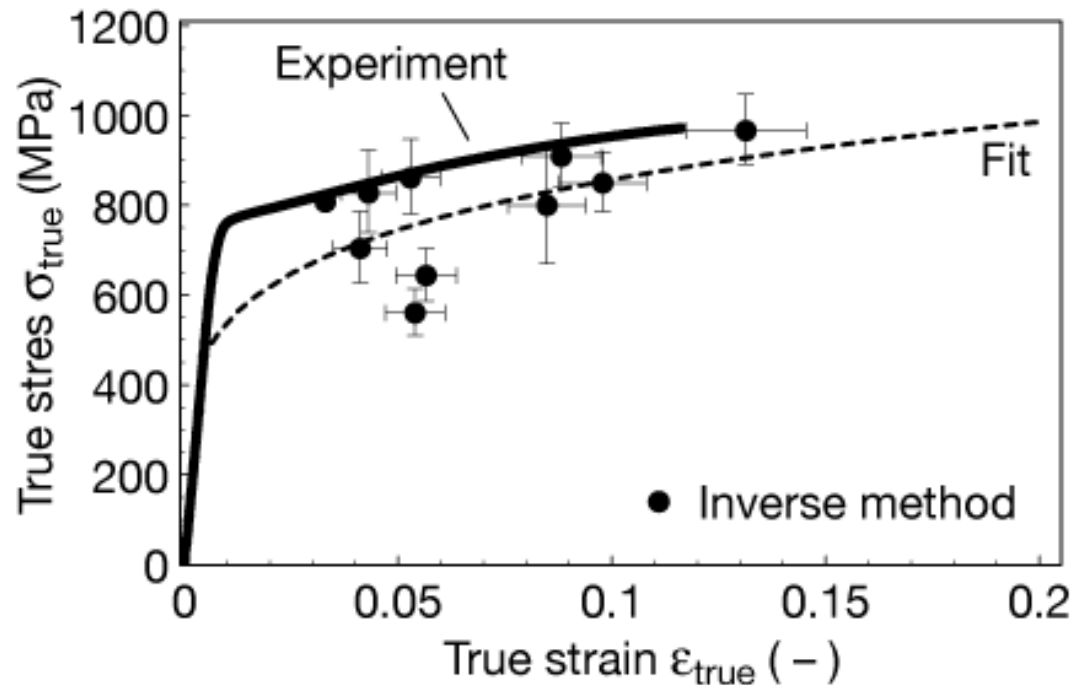
Material:
CuCo2Be

Indentation tests:
Zwick Universal
hardness tester

Diamond tip geometries
38.6°, 47.0°, 50.0°, 51.0°, 61.7°
62.8°, 63.3°, 67.7°, 68.6°

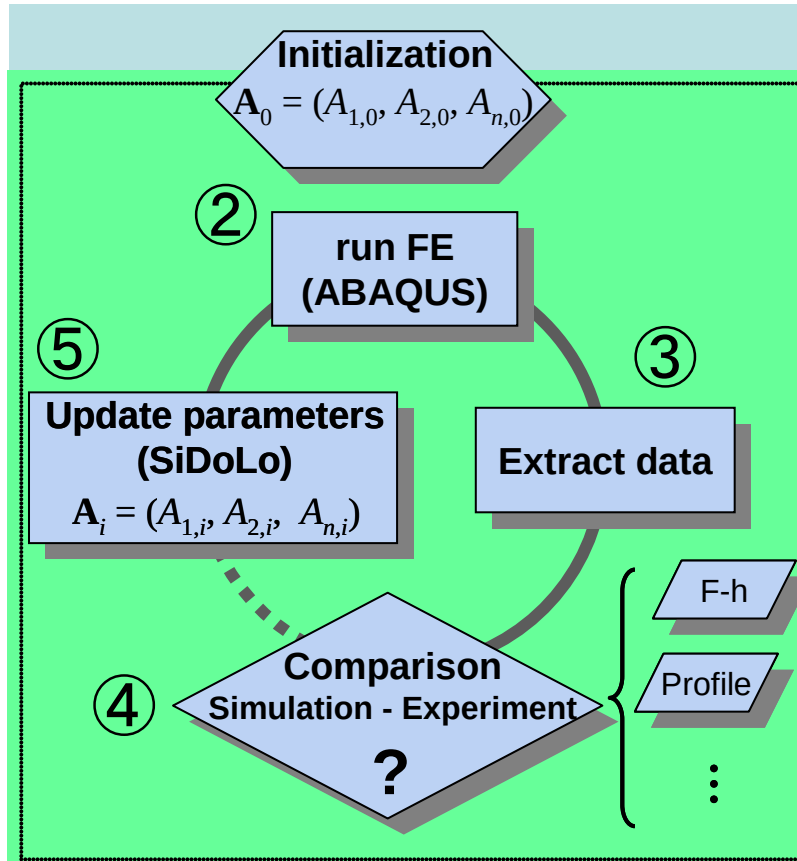


& Vickers (70.3°)

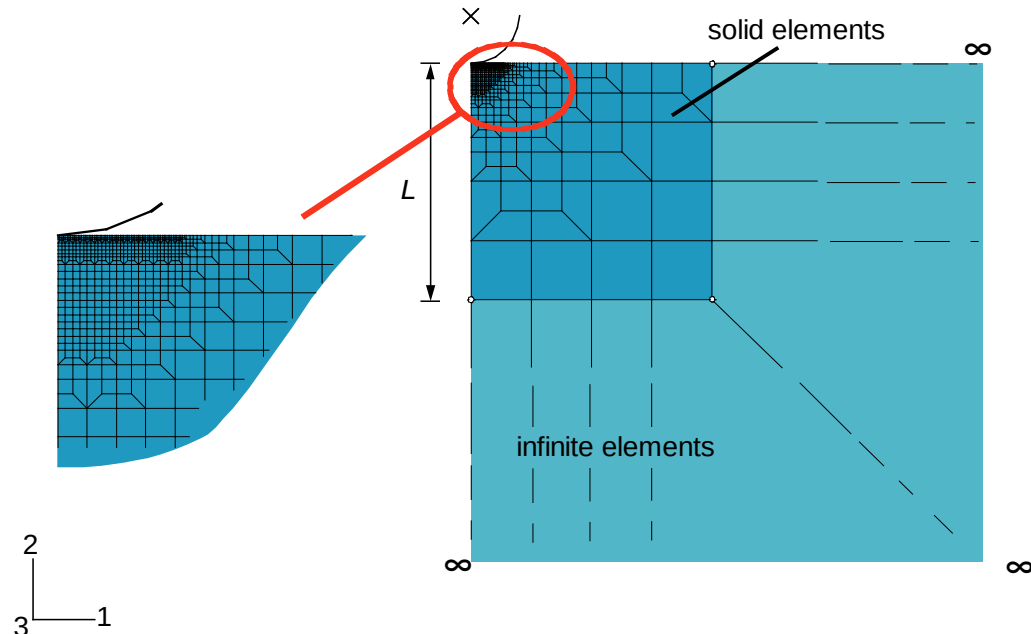


spherical indentation: algorithm I

idea: optimize FE calculation until calculated data fit experimental topography and load-displacement data

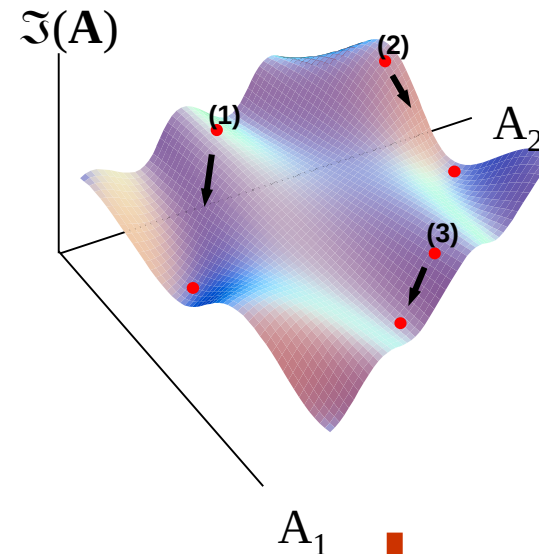
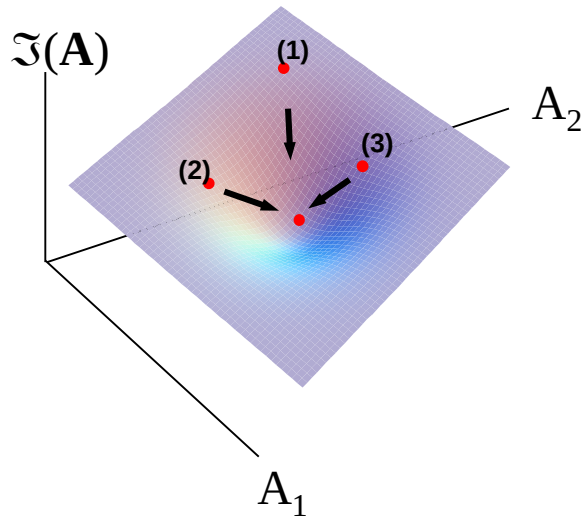


FE meshing scheme optimized for minimizing computing time; combination of finite and infinite axisymmetric elements (to eliminate boundary effects (i.e. $u_i = 0$) on numerical solution)



spherical indentation: algorithm II

But: Ill conditioned problem?



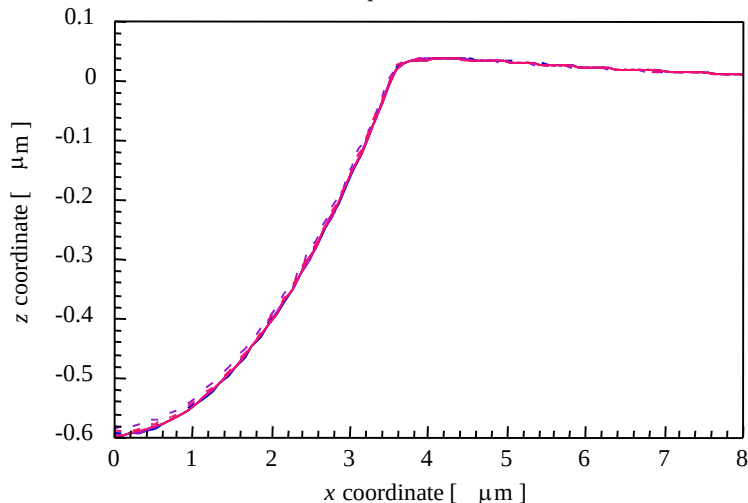
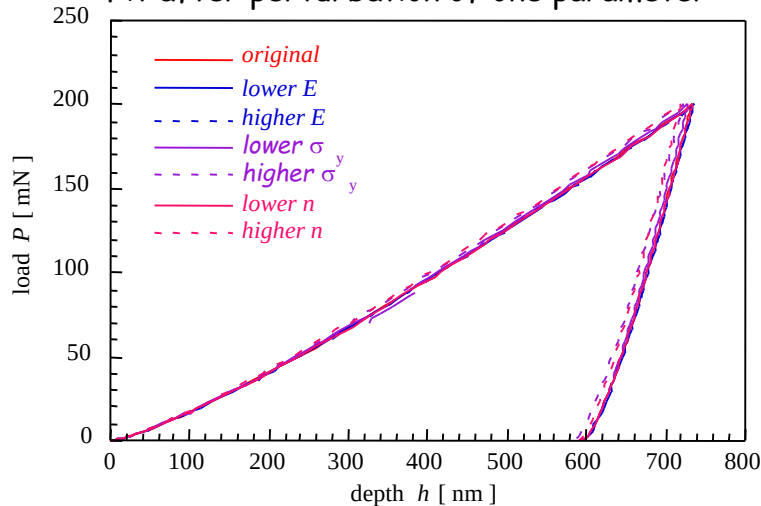
Fitting: Vary systematically parameters around starting point and “go a step in direction of the deepest gradient” to minimize the difference $J(\mathbf{A})$ between simulated and experimental data

Practical guideline: Good estimation of initial values and stabilization of the solution by increasing the number of fitted parameters

spherical indentation: model calculation

Validation: Fit back a finite element calculation after starting from 10% perturbation

Fit after perturbation of one parameter



Material model:

$$\sigma = \begin{cases} E\varepsilon \\ \sigma_y \left(1 + \frac{E}{\sigma_y} \varepsilon_{pl} \right)^n \end{cases}$$

Example calculation (perturbation of all param.):

	E [GPa]	σ_y [MPa]	n []
Original	210	500	0.3
Start	189	450	0.27
Fit	208	494	0.30

spherical indenters: experiment

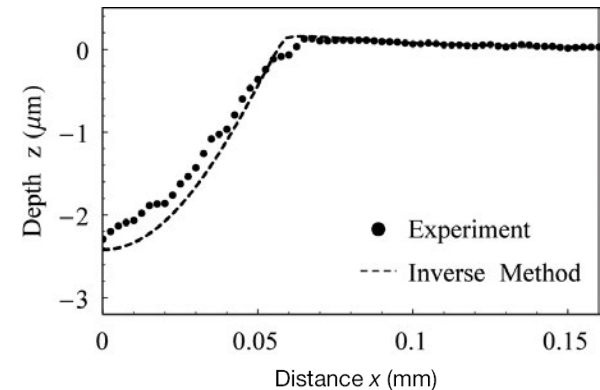
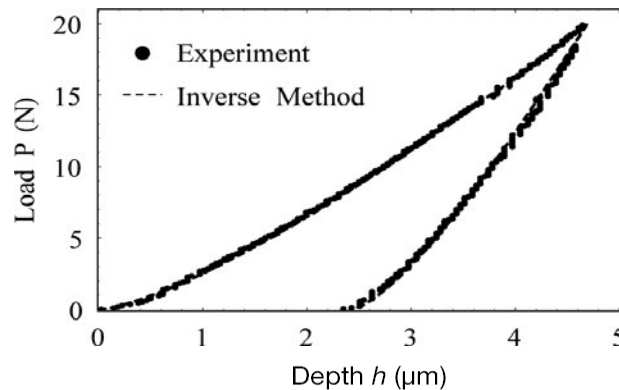
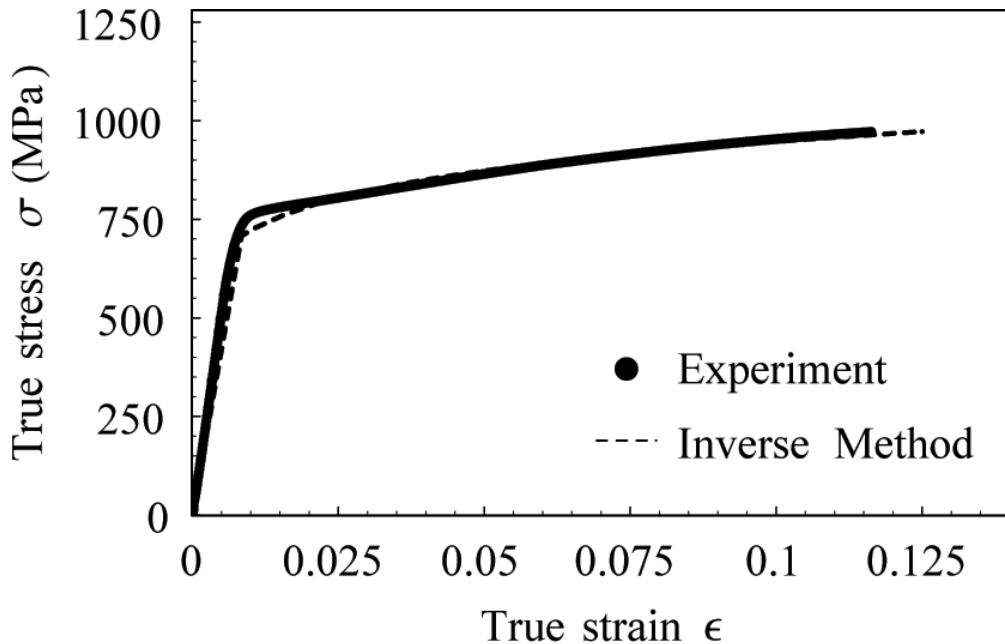
material:
CuCo2Be

indentation tests:
universal
hardness tester

topography measurements:
laser profilometer

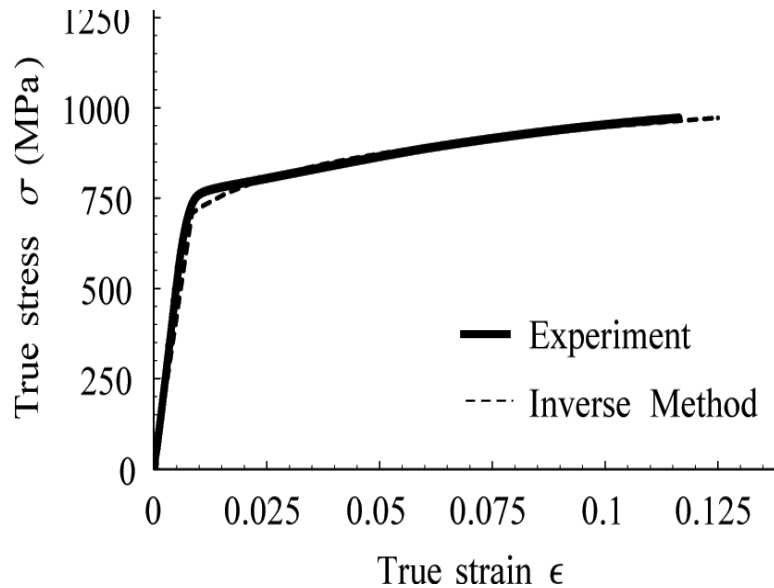
tip geometry:
WC sphere $R=0.5\text{mm}$

fit:
perturbation of
all parameters
by 10%

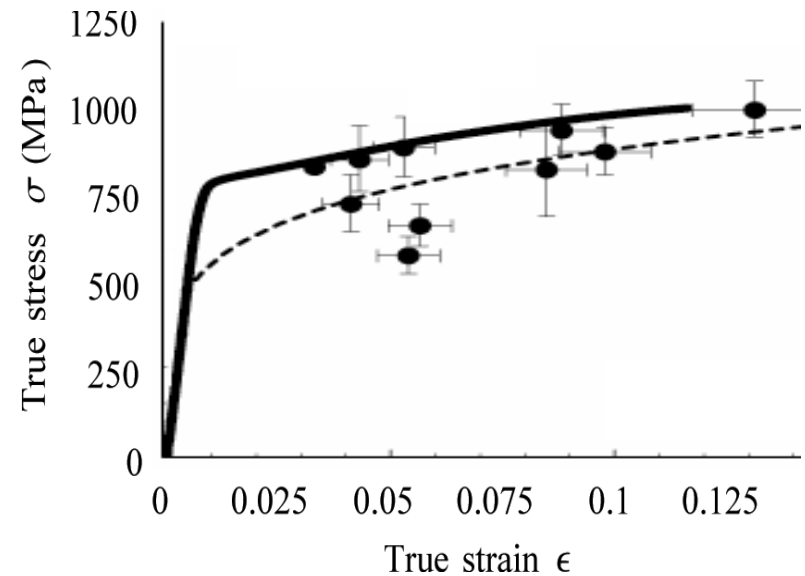


comparison of "conical" and "spherical" indentation methods

sphere & residual imprint



multiple cones



outlook: application to coatings

material:

NiCo electrodeposited coating

tensile tests:

UV-Liga tensile test bars

indentation tests:

MTS nanoindenter XP

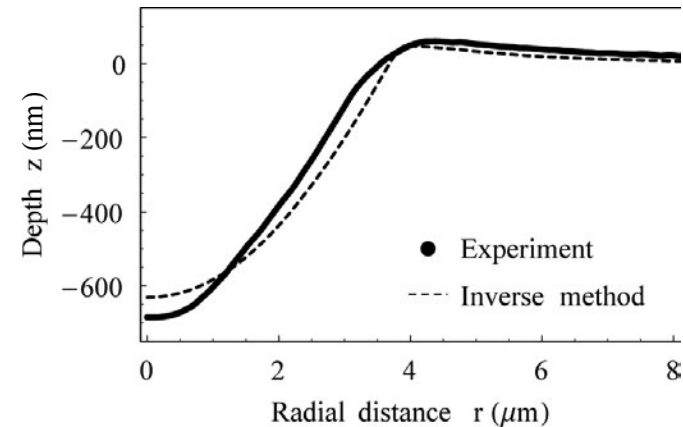
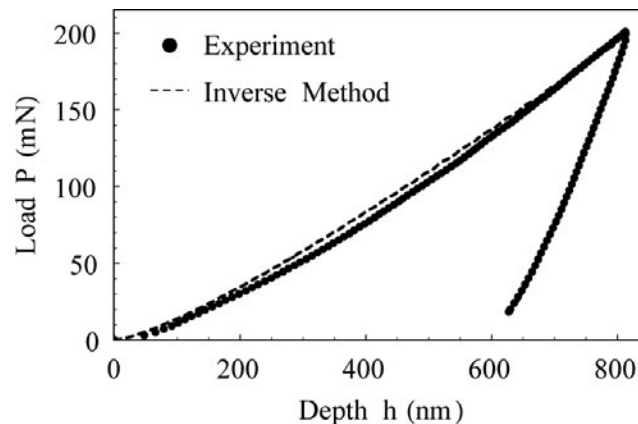
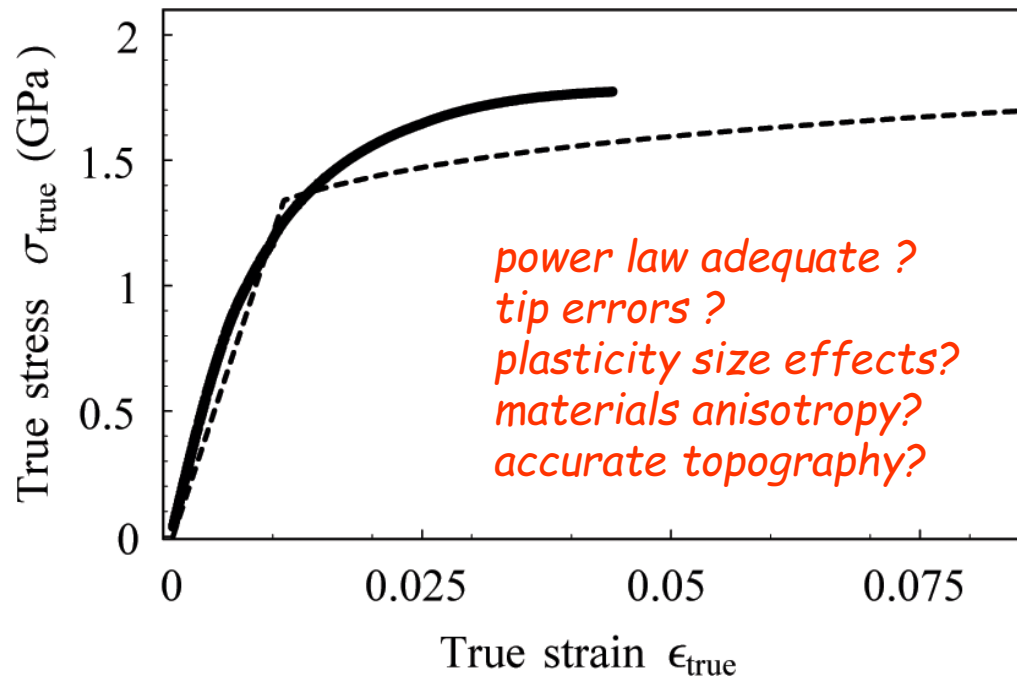
topography measurements:

AFM

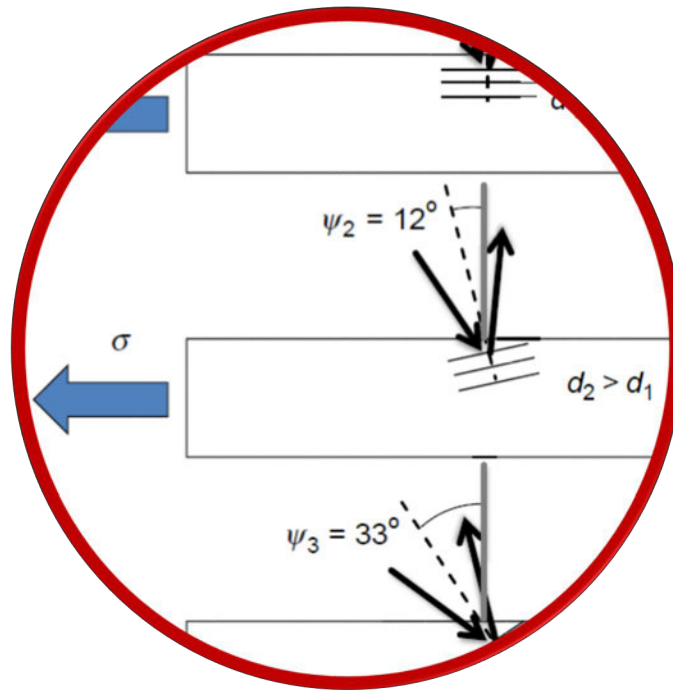
tip geometry:

diamond

spherical $R=10\mu\text{m}$



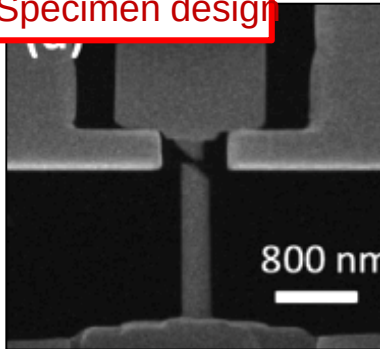
Microscale tensile testing



Challenges of small scale tension

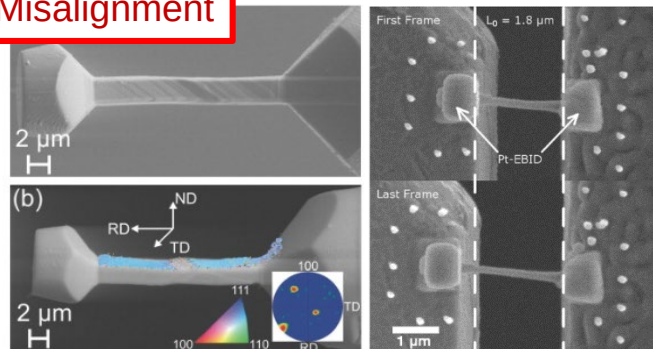
Possible issues in small scale tensile experiments:

Specimen design



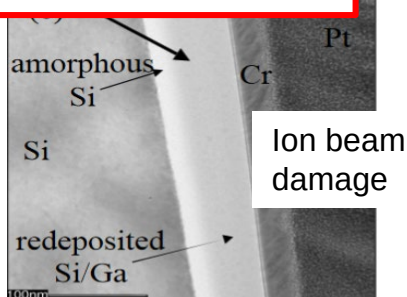
Liontas et al. *Acta Mater.* (2016)

Misalignment



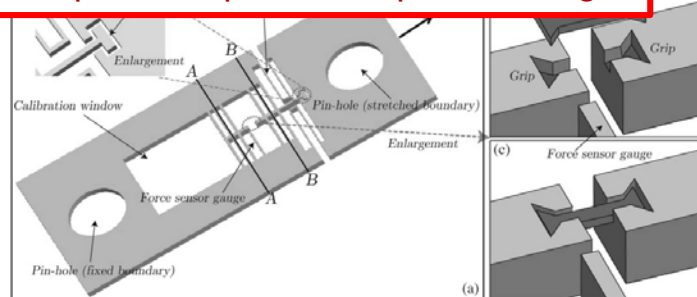
Kiener et al. *Acta Mater.* (2008) Magagnosc et al. *Sci. Rep.* (2015)

Fabrication artifacts



Rajsiri et al. *Microsc Microanal* (2002)

Complex setup and sample handling



Kang et al. *J. Microelectromech. Syst.* (2010)

Requirements for the new methodology:

1. Minimise stress concentrations.
2. Optimise specimen fabrication via FIB.
3. Ensure alignment.
4. Avoid complex and tedious manipulations. No single use setups.

In situ tension: single-crystal copper samples

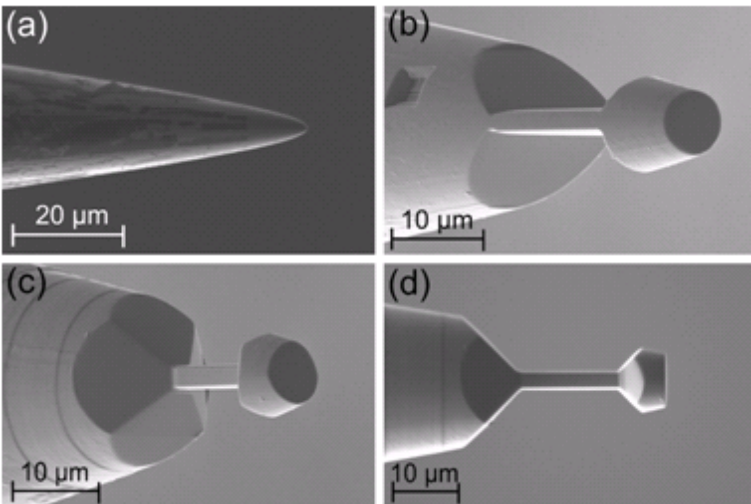


Fig. 1

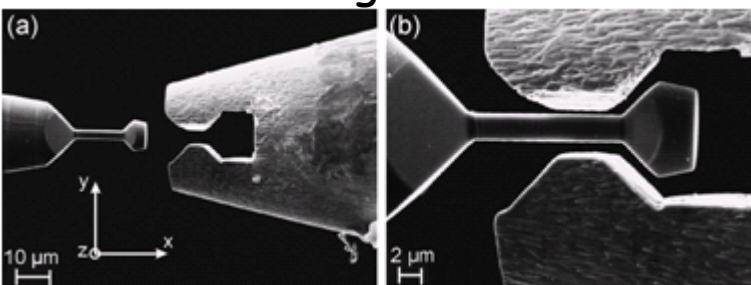


Fig. 2

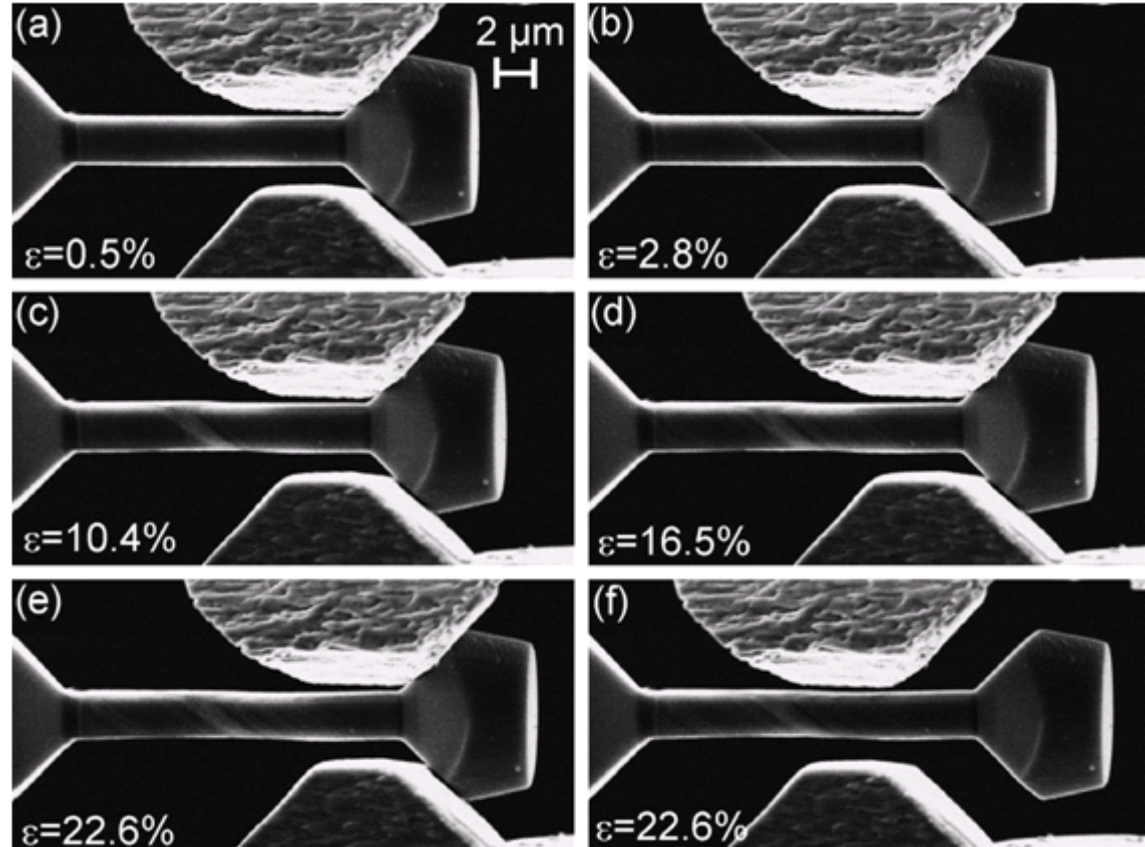
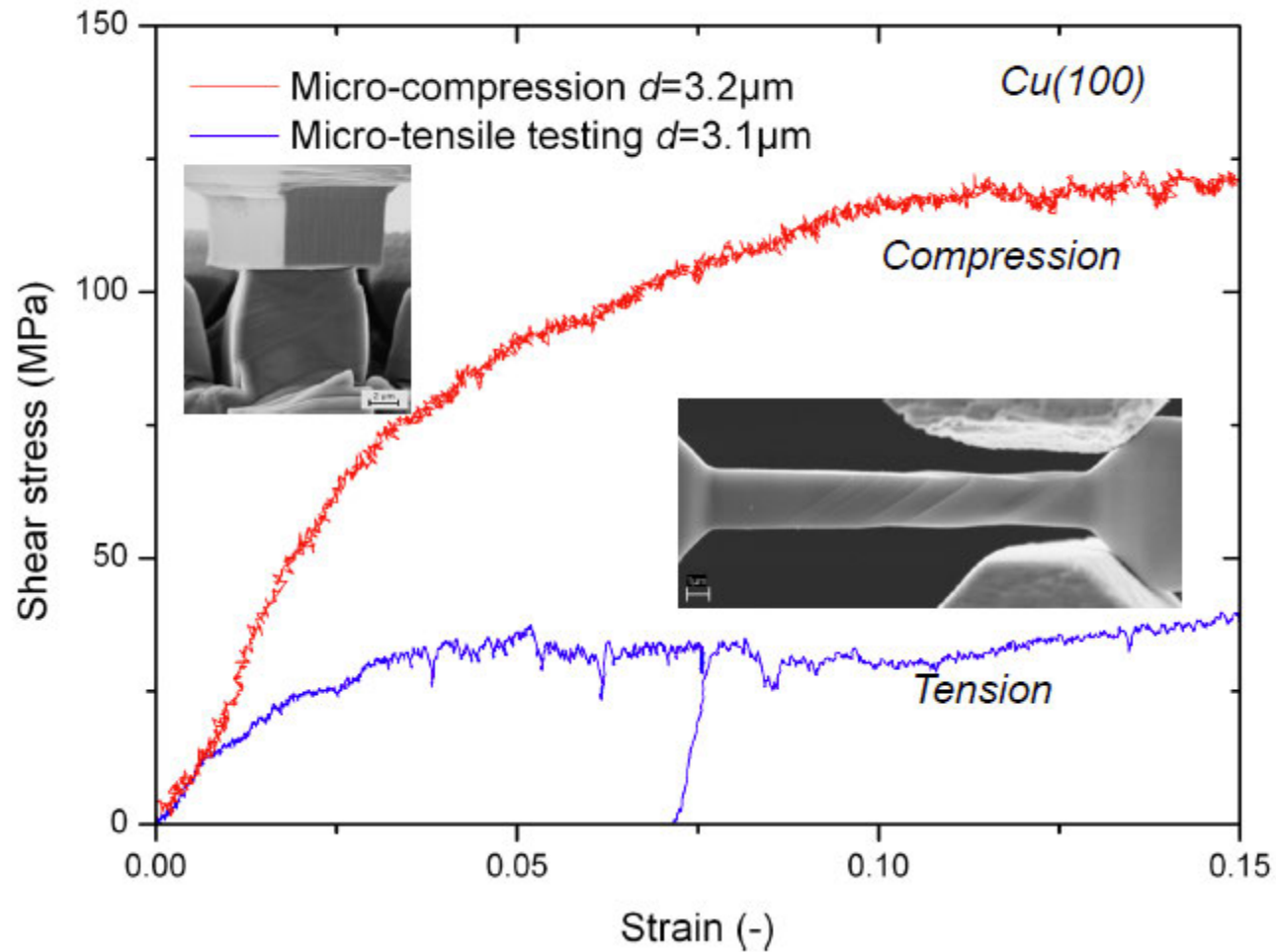


Fig. 3

Compression versus tension

Cu(100) oriented tensile and compression sample



Rotation of the Crystal Lattice

The slip direction rotates towards the tensile axis

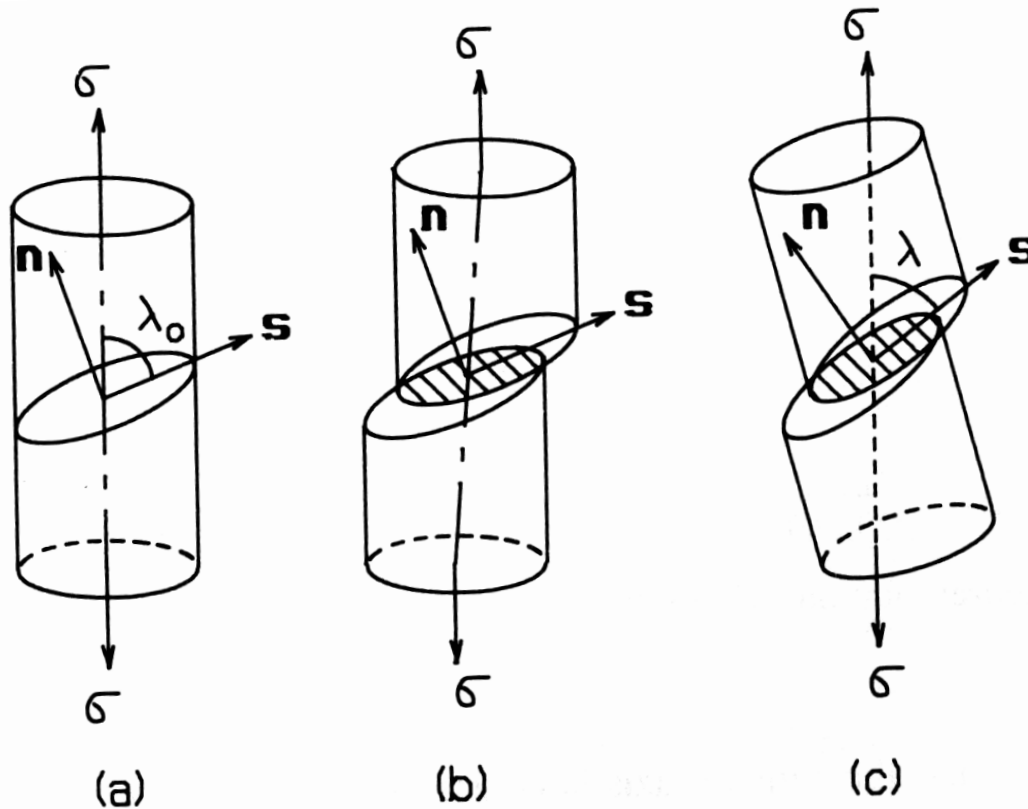
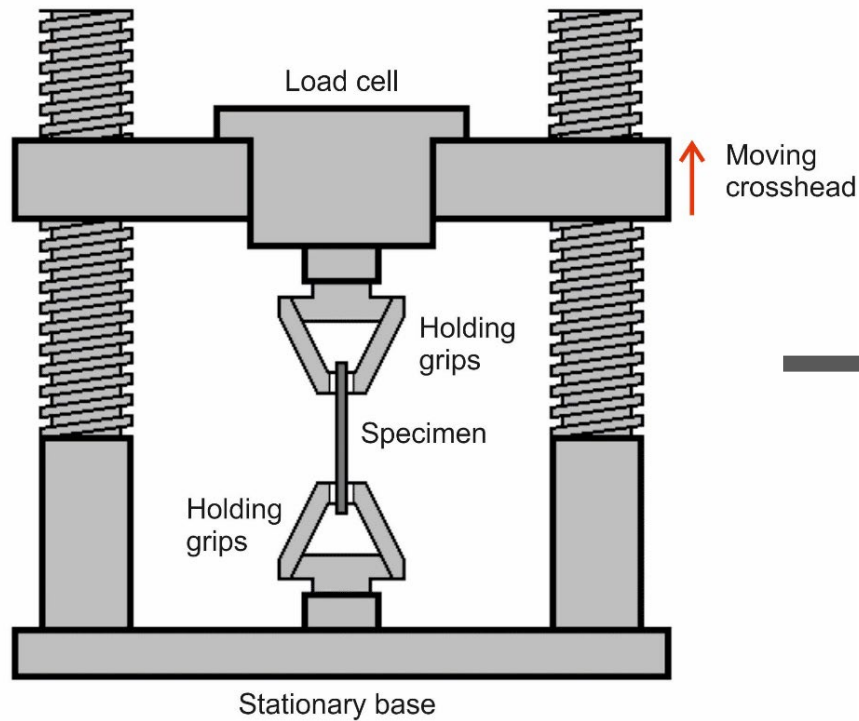


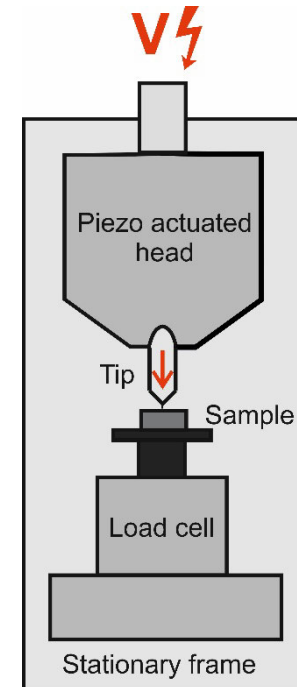
Fig. 10.5 Rotation of crystal lattice in tension

Standard testing at the microscale?

Macroscale



Microscale

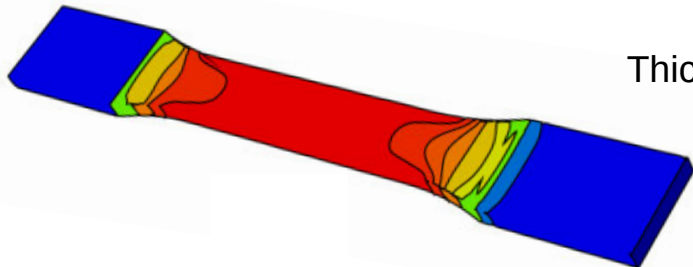


Standard testing at the microscale?

Macroscale

ASTM 638 Type V

Free end



Free end

Variables

Thickness, width, radius, head shape



Microscale

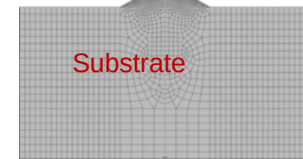
New specimen geometry

Free end



Gripper

Substrate



Goals

Homogeneous stress in the gauge section

Low stress concentration at the radius (<5%)

Constraints

Maximum gauge dimensions = 10 μm (**lamella**)

On bulk substrate (**no micromanipulation**)

FIB milling fabrication

Specimen design

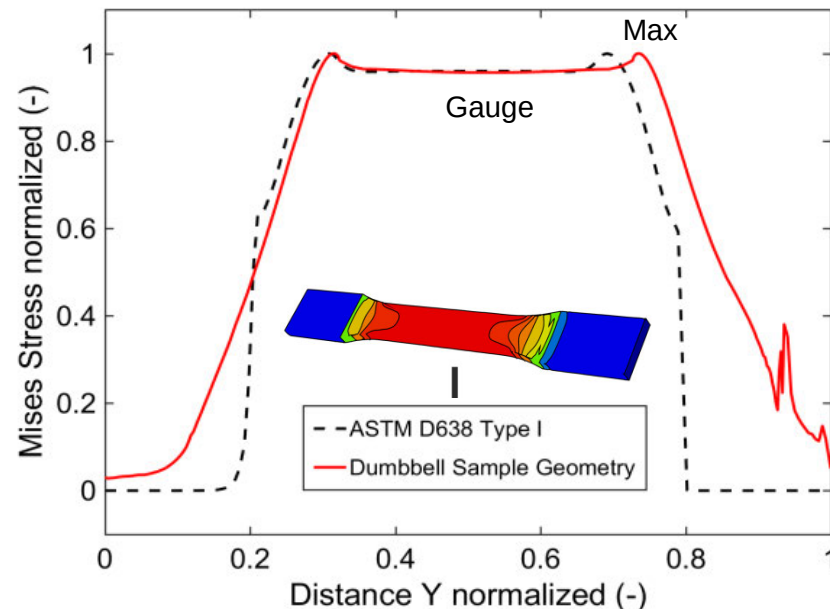
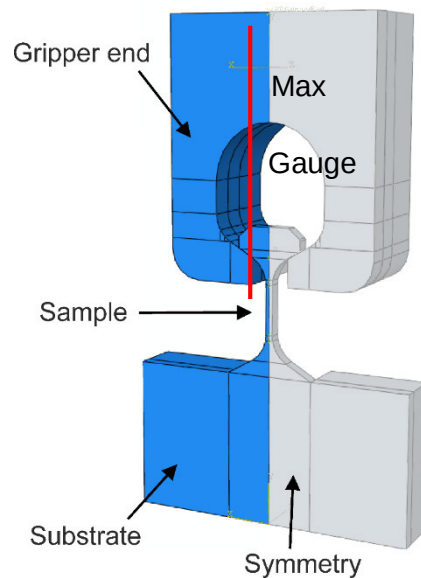
- **Finite elements analysis using Abaqus/Standard:**

- $\frac{1}{4}$ Symmetry, C3D8R (no bending).
- Linear elastic material properties.
- Hourglassing controlled and checked with ALLAE/ALLIE < 1%.

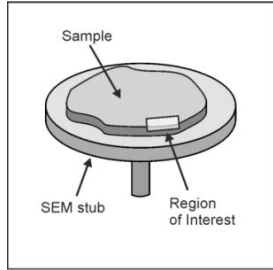
Variables: thickness, width, radius, head;

Fixed: gauge length = 10 μm

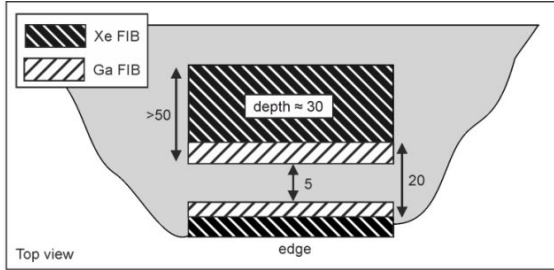
Output: stress profile and stress concentrations



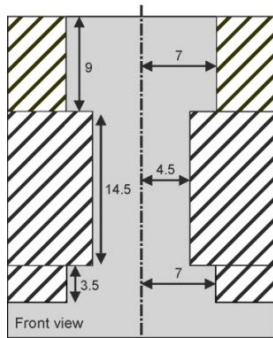
Specimen design



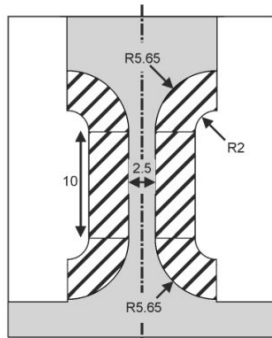
0. Sample on a SEM stub



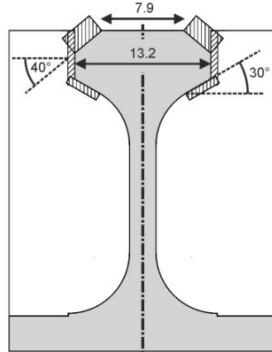
1. Xe plasma-FIB milling (30kV, 30 nA) and Ga FIB (30kV, 4.5nA and 0.7nA)



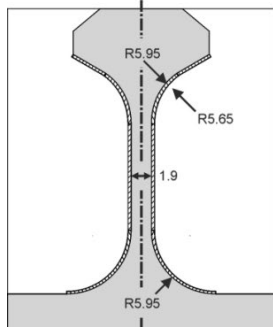
2. Coarse polishing A (30kV, 4.5nA)



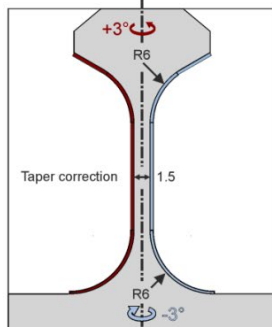
3. Coarse polishing B (30kV, 4.5nA)



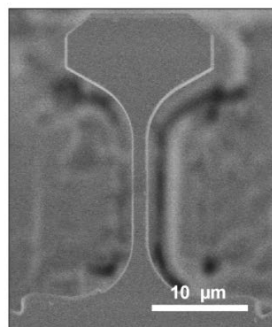
4. Fine polishing A (30kV, 0.7nA)



5. Fine polishing B (30kV, 0.7nA)



6. Taper polishing (15kV, 0.4nA)



Final geometry

Homogeneous stress profile in the gauge

Gauge section length $\geq 4w$.

Low stress concentration at the radius

$$K_c = \frac{\sigma_{max}}{\sigma_{gauge}}$$

Maximise geometry ratio r/w ($r/w \geq 4 \rightarrow K_c < 1.05$).

K_c independent of thickness.

Fabrication via FIB possible

Optimized FIB Milling protocol

Microtensile gripper

Requirements: Solutions:

Mounting
Handling



Large base

No creep
Reproducible



Silicon

Alignment
Gripping

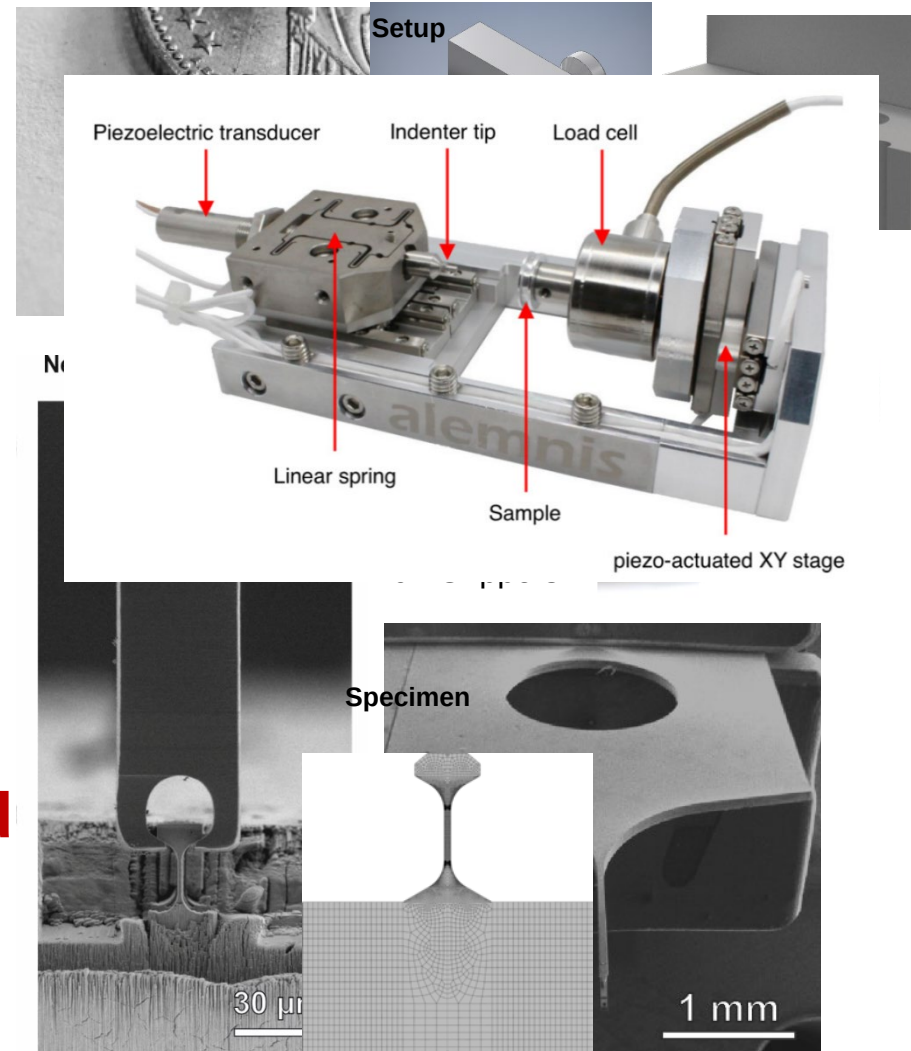


Needle shaped

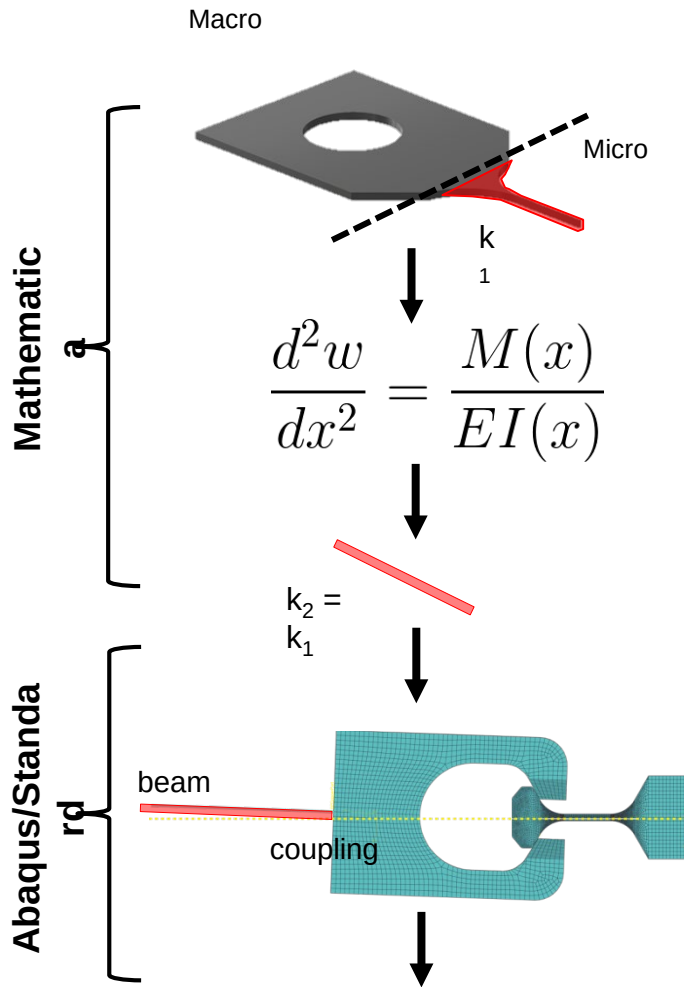
Lateral compliance



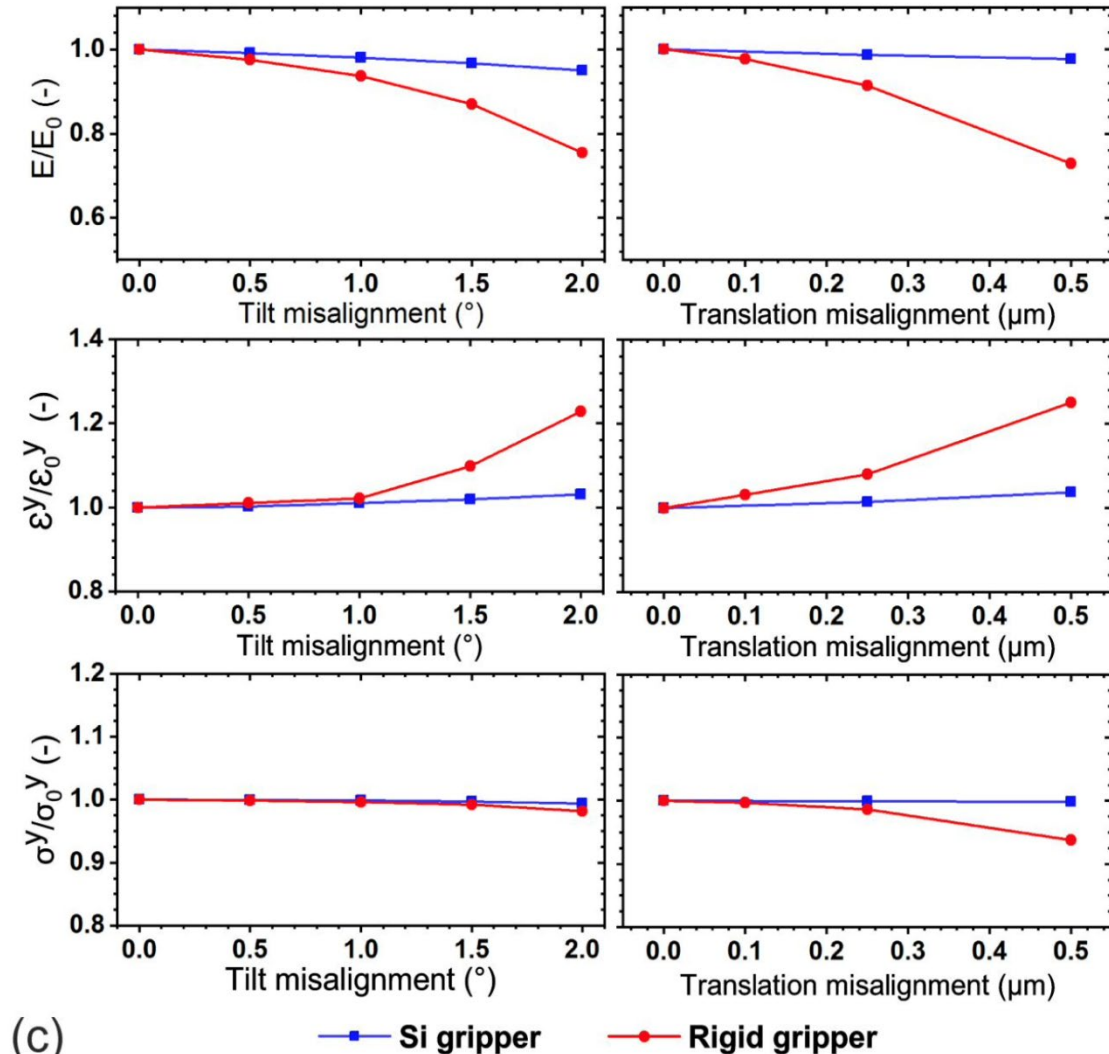
Self-aligning



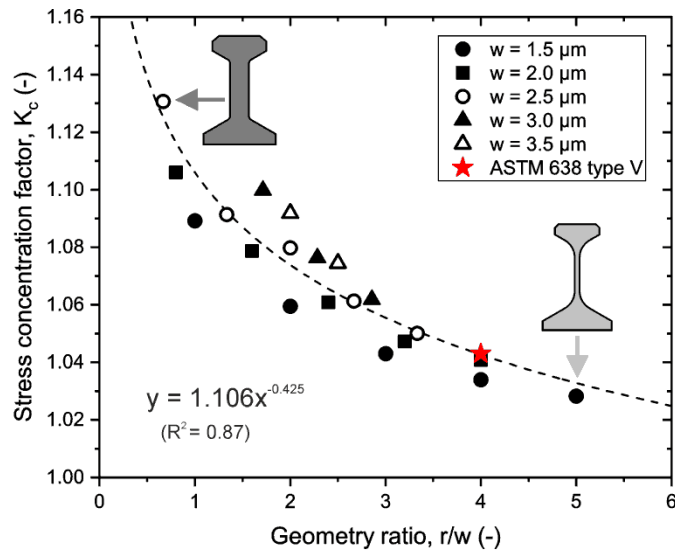
Misalignment tolerance



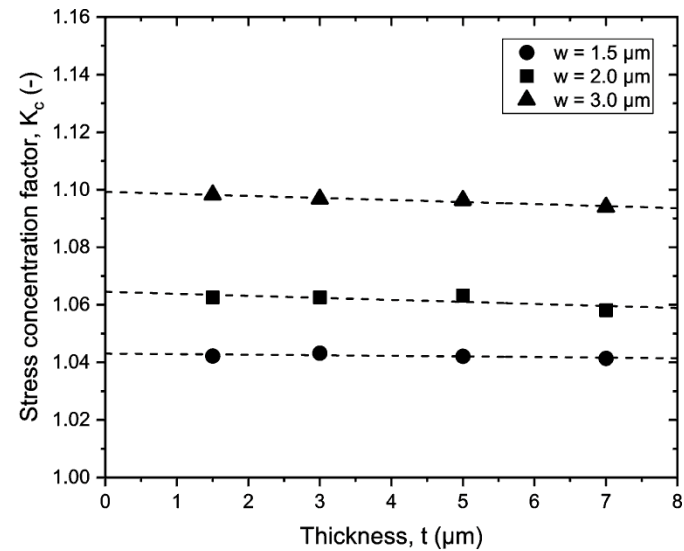
Which needle shape is better?



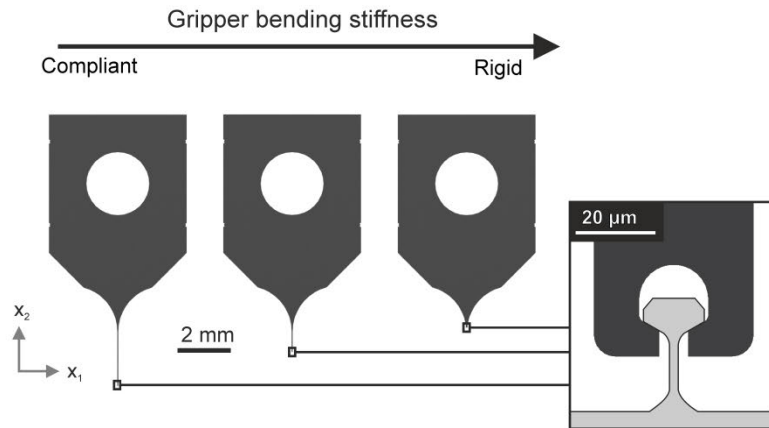
Misalignment tolerance



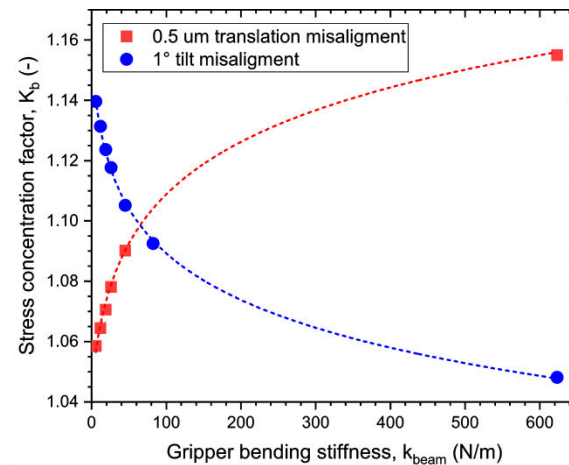
(a)



(b)



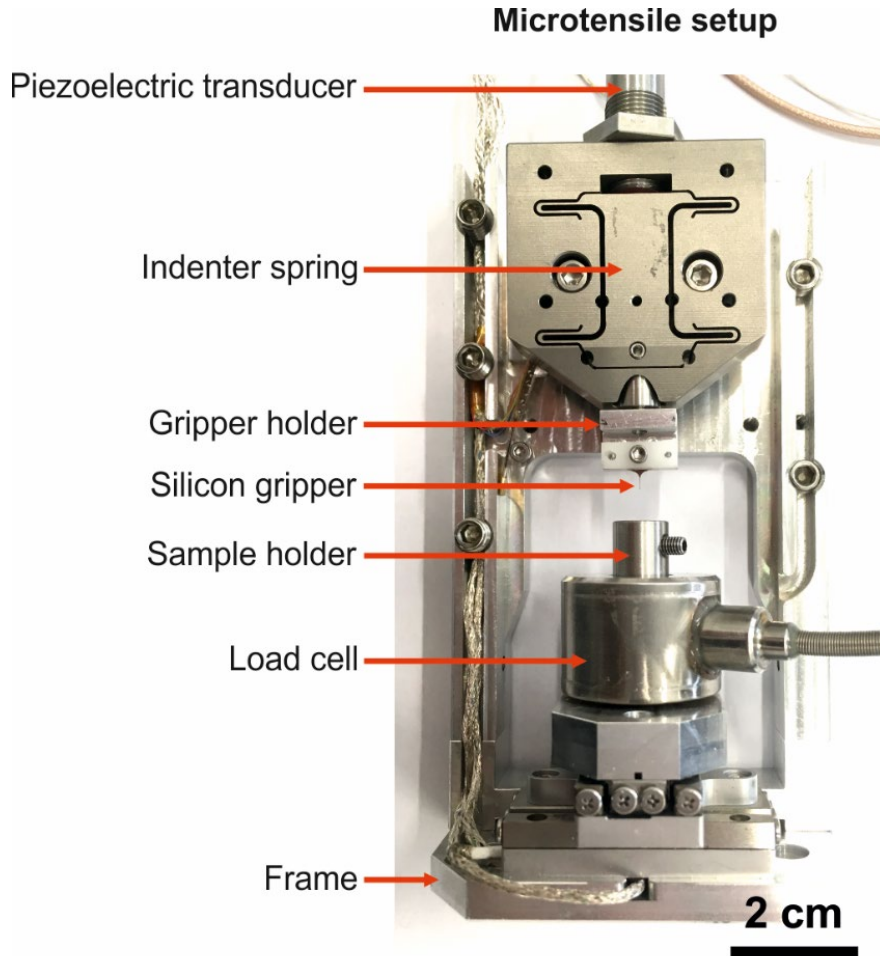
(a)



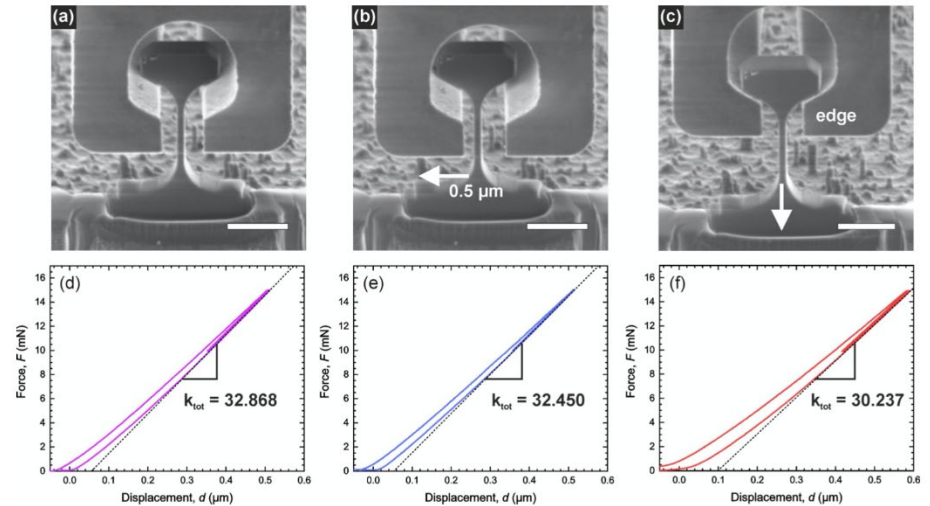
(b)

Microtensile setup

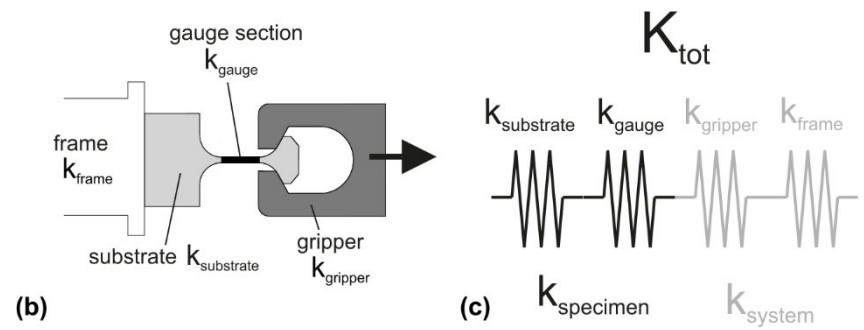
Setup components



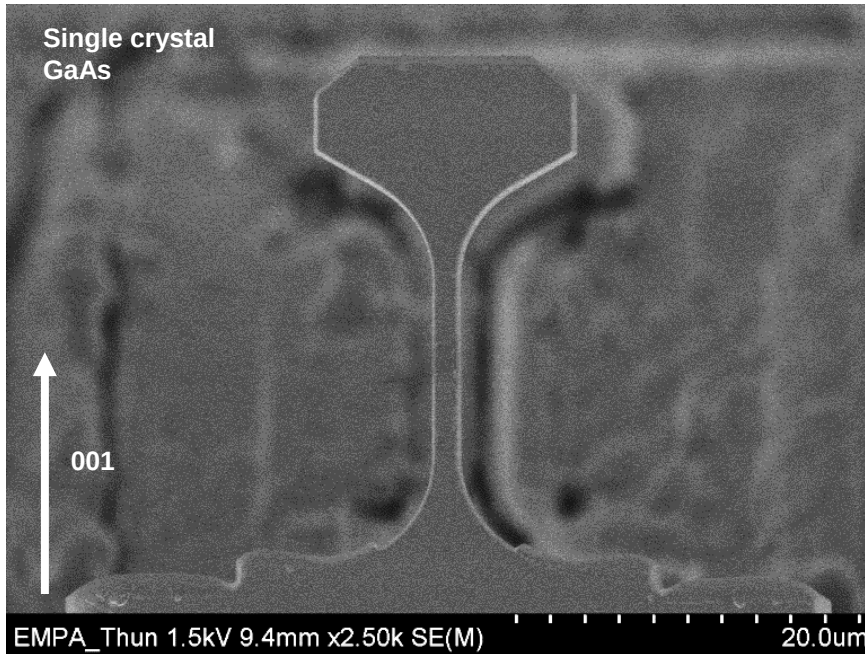
Misalignment tolerance



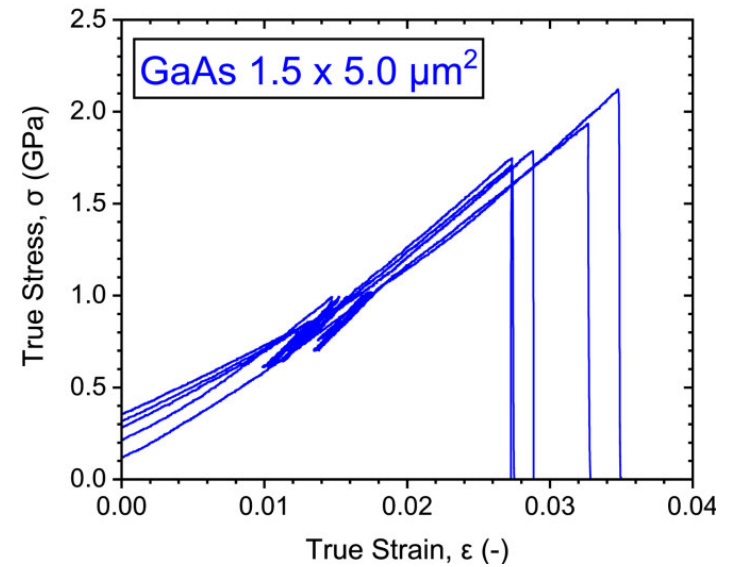
Compliance correction



Validation and application



Experiment on GaAs



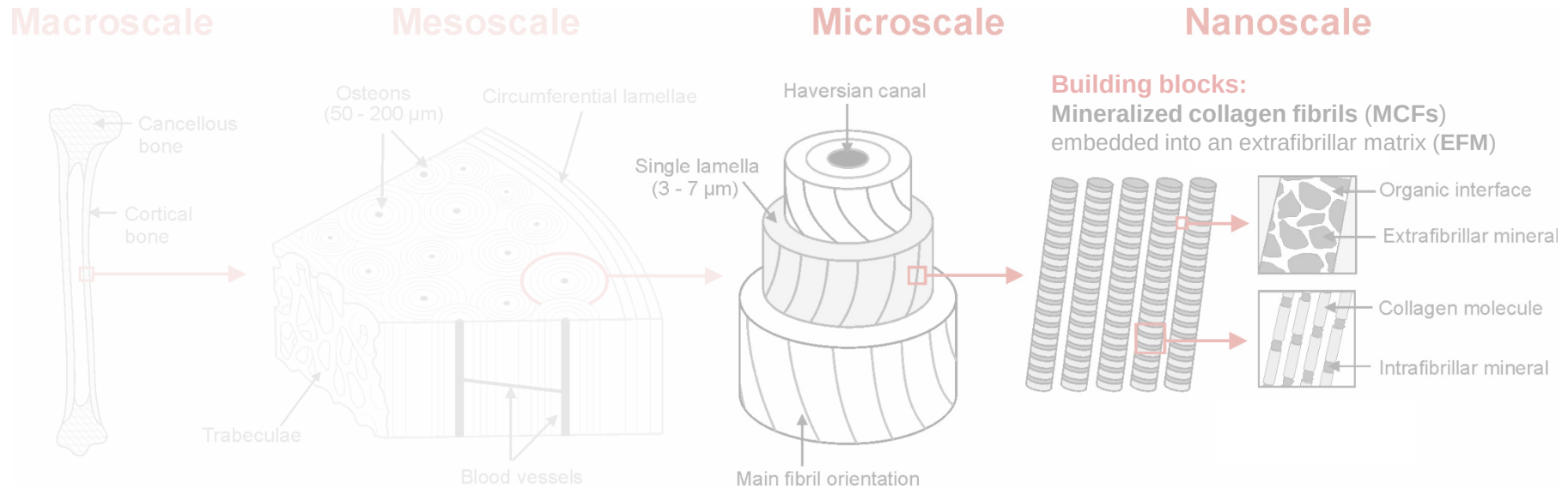
Property	Literature value (GPa)	Measured (N = 5) (GPa)	Relative difference (%)
Elastic modulus E_{001}	85.5		

More information in: A self-aligning microtensile setup: application to single-crystal GaAs microscale tension–compression asymmetry, *Journal of Material Research*, **34**, 2019

Case study: Microtensile properties of bone

Tension-compression asymmetry

Structural hierarchy of bone



Limited selection constituents: collagen, hydroxyapatite minerals, water and non-collagenous proteins

Lamellar bone: most abundant type of bone, MCFs arrays oriented within each lamella.

Properties: lightweight, stiff, strong and tough.

**Microscopic cracks,
blood vessels, cells network**

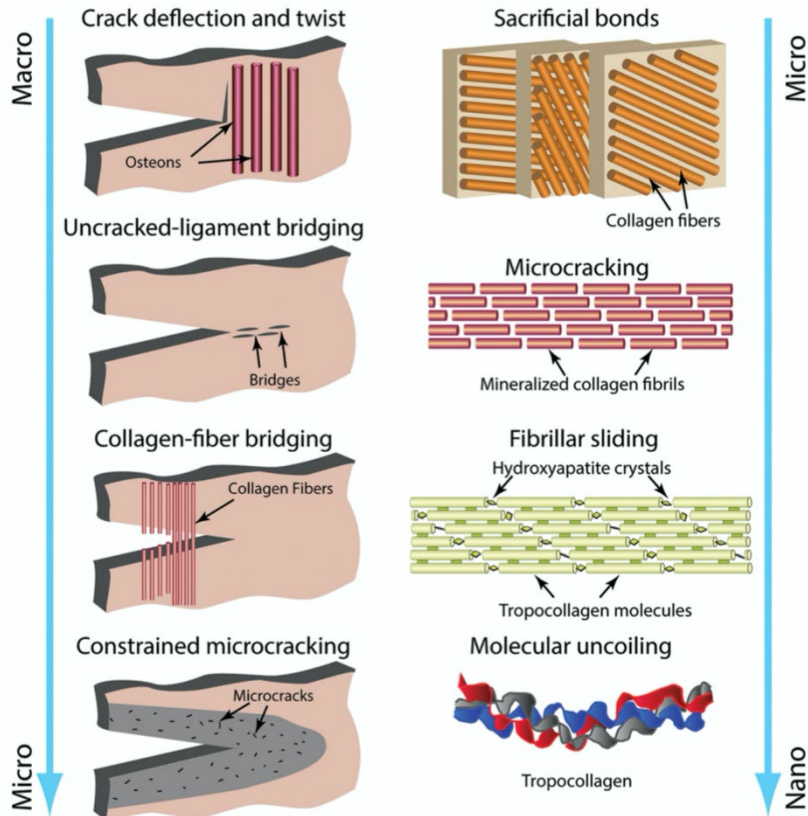
BUT

Tolerance to flaws (healthy)

How? Several **weak interfaces** at different length scales create different toughening mechanisms.

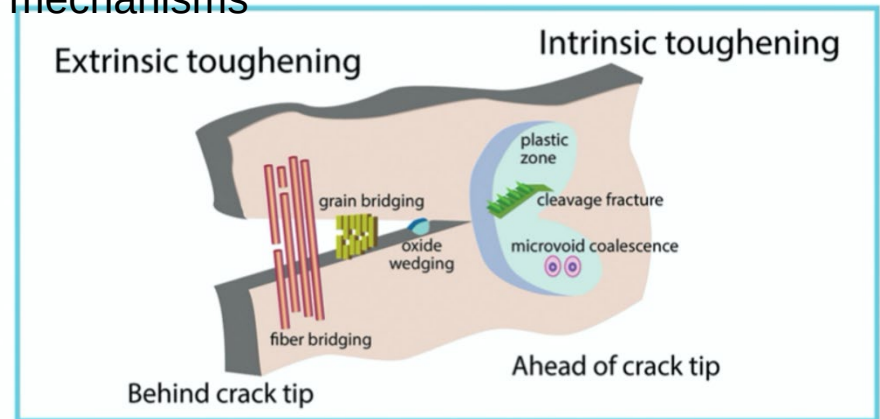
Toughening mechanisms

Several toughening mechanisms in bone



Zimmerman & Ritchie, *Adv. Healthc. Mater.* (2015)

Bone exhibits **two types** of toughening mechanisms



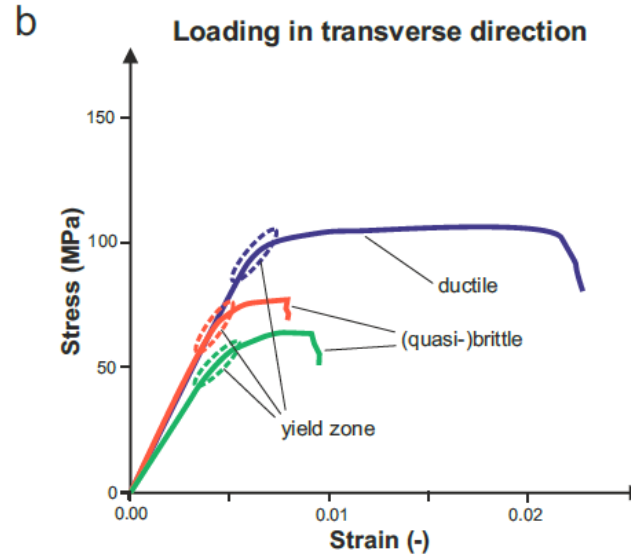
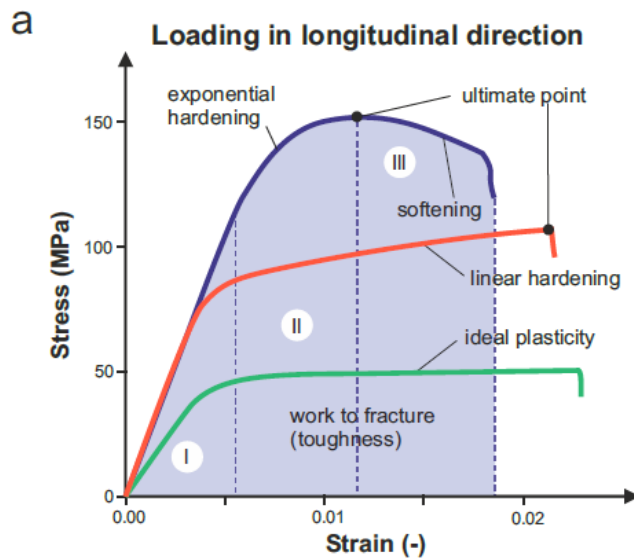
Zimmerman & Ritchie, *Adv. Healthc. Mater.* (2015)

Intrinsic mechanisms:
prevent crack initiation (and growth).

Extrinsic mechanisms:
resist propagation of an existing crack.

The **hierarchical** organization of simple **building blocks** and **interfaces** allows bone to resist fracture.

Macroscale mechanical properties



Loading mode dependent

Anisotropic

Sample orientation



Longitudinal

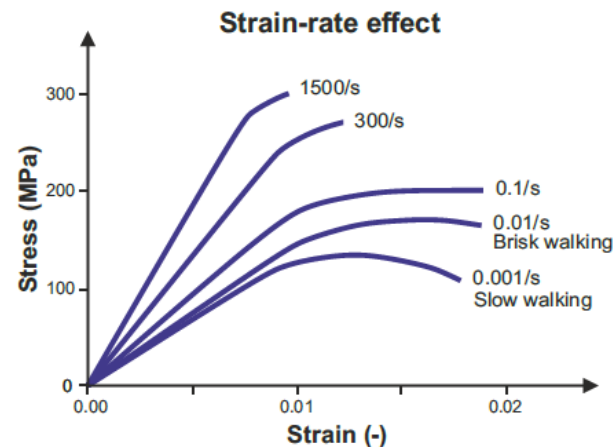
Transverse

Loading mode

■ Compression

■ Tension

■ Shear



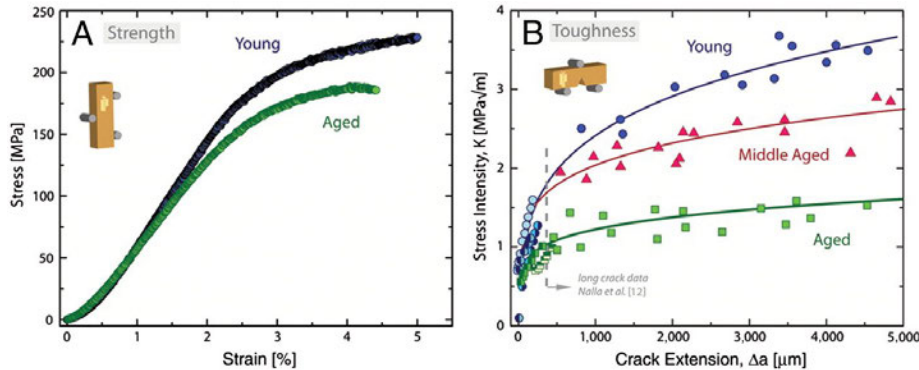
Viscoelastic

(a,b) adapted from Wolfram & Schwiedrzik, *BoneKEy reports* (2016)

(c) adapted from McElhaney J. *Appl. Physiol.* (1966)

Degradation and osteoporosis

Decrease in bone strength and toughness with age **Increase in porosity (bone quantity)**

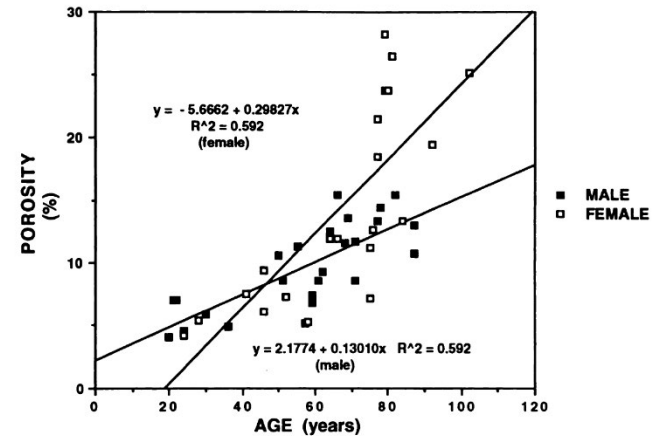


Strength: - 2% every decade*

Zimmerman et al. *PNAS* (2011)

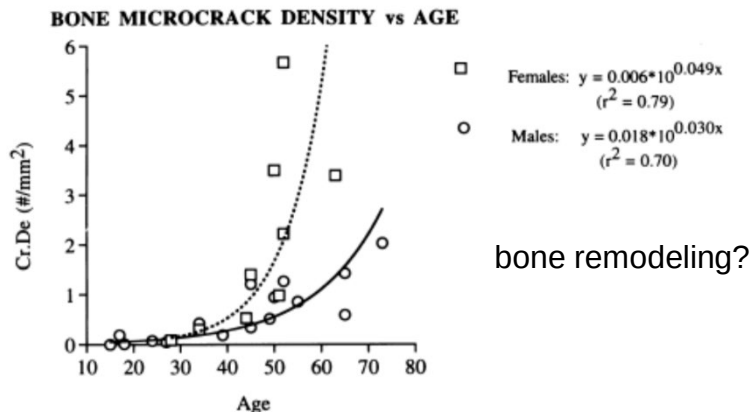
Toughness: - 4% every decade*

*from 40 years old



McCalden et al. *JBJS* (1993)

Osteoporosis is conventional (diagnostic) challenge by conventional (DEXA)



bone remodeling?

Schaffler et al. *Bone* (1995)

Increased **collagen cross-linking** inhibits collagen slip

Snedeker et al. *MLTJ*, 2014

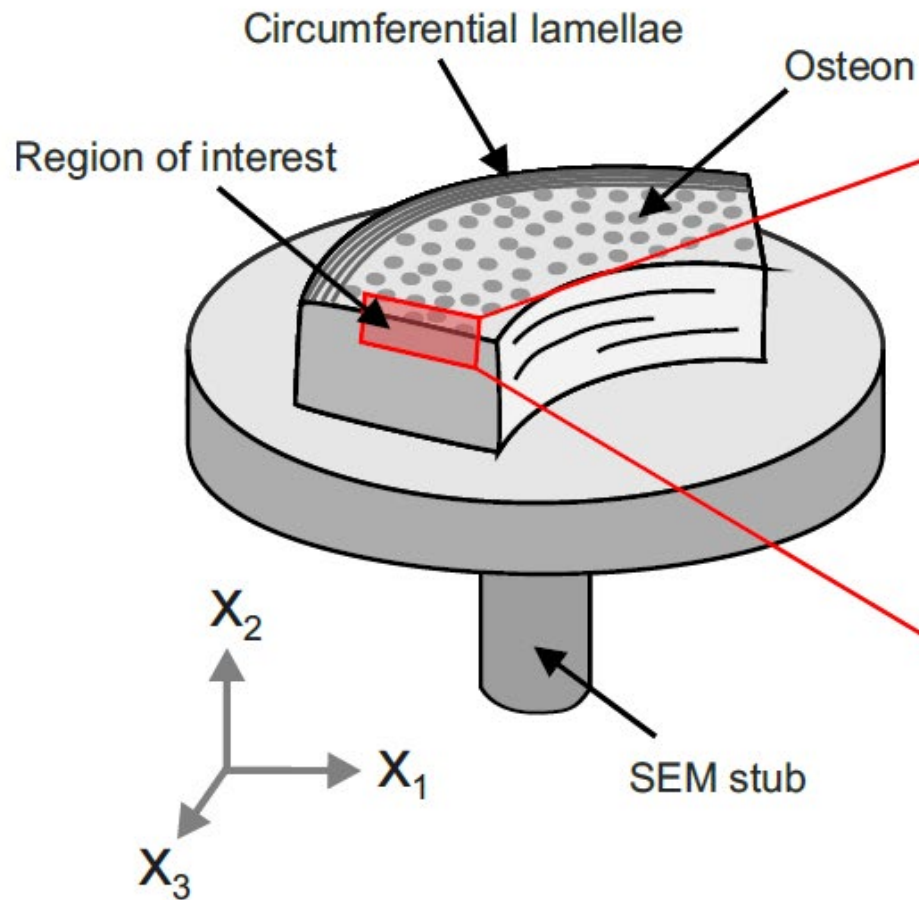
Changes in **interfaces**?

Higher fraction of weak cement lines

Smaller osteons: reduced crack deflection

Zimmerman et al. *PNAS* (2011)

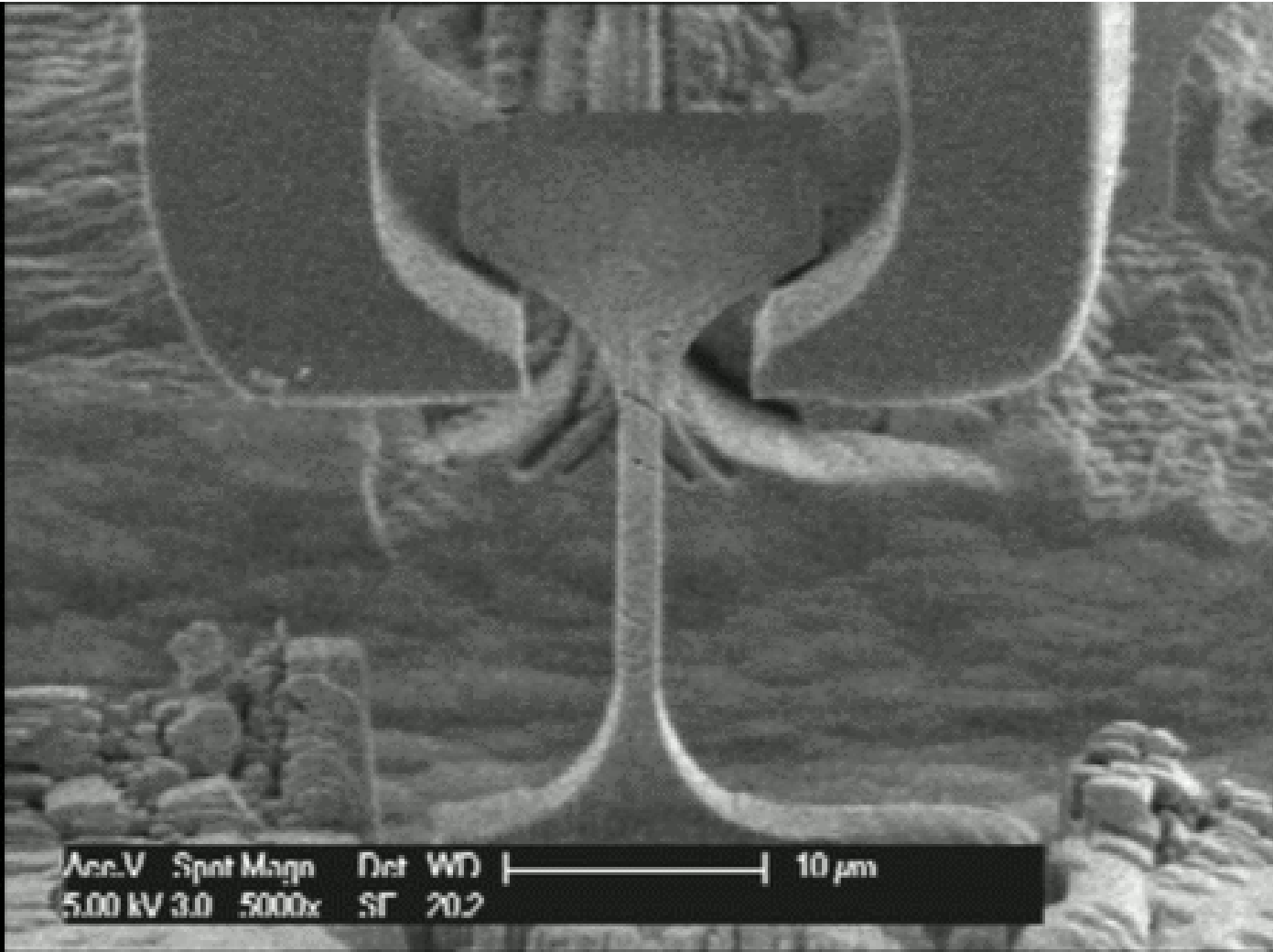
Sample preparation



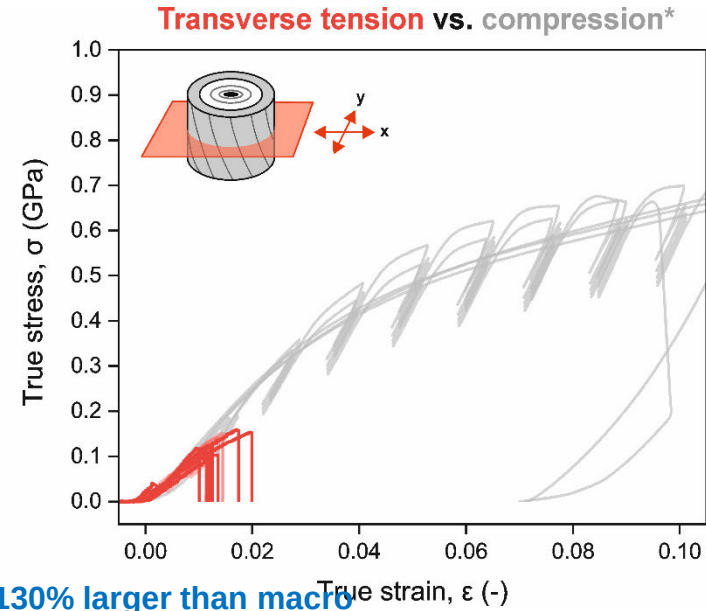
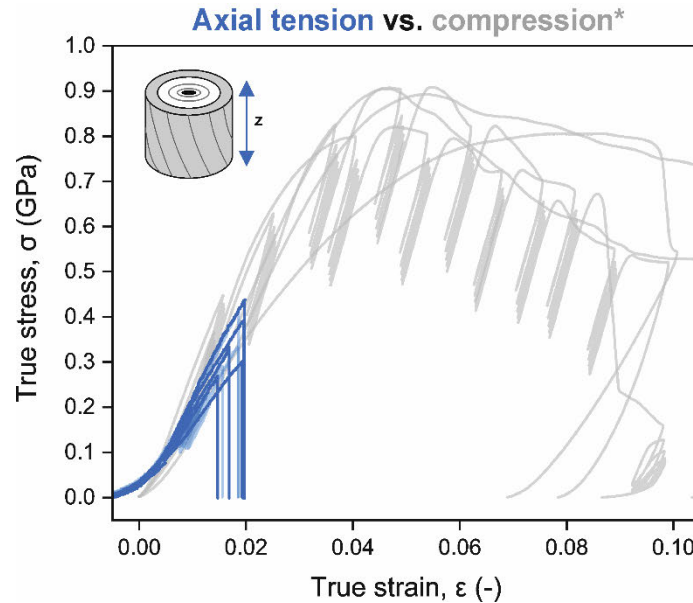
FIB milled specimens



Microtensile experiments



Tension-compression asymmetry



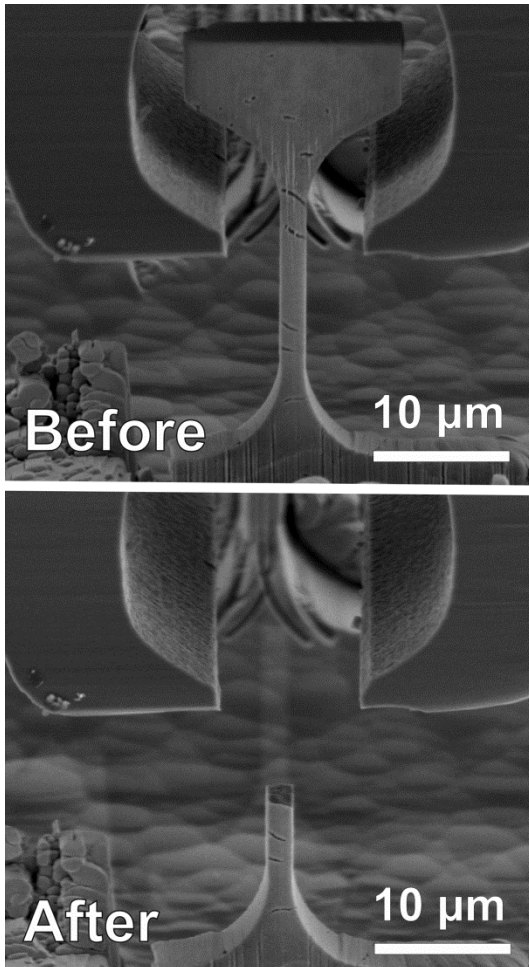
130% larger than macro

Sample Orientation	Loading mode	E (GPa)	$\sigma^{\max}$ (GPa)	$\epsilon(\sigma^{\max})$ (%)	σ^y (GPa)
Axial	Compression*	31.1 ± 6.5	0.75 ± 0.06	5.4 ± 1.7	0.49 ± 0.10
	Tension	28.9 ± 3.4	0.35 ± 0.05	1.8 ± 0.2	-
Transverse	Compression*	16.5 ± 1.5	0.59 ± 0.04	12.1 ± 2.5	0.30 ± 0.02
	Tension	13.6 ± 1.2	0.13 ± 0.02	1.3 ± 0.3	-

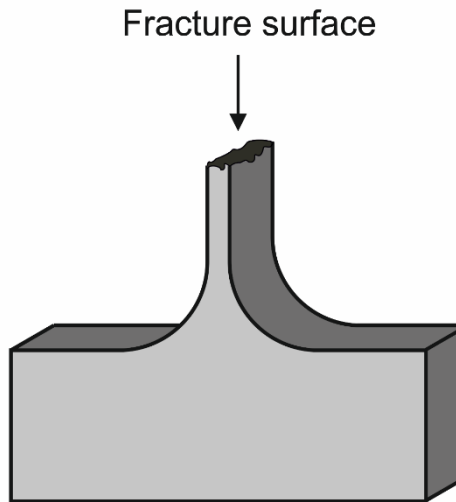
* data obtained from Schwiedrzik et al. *Nat. Mat.* (2014)

- Elastic properties are similar between loading mode and depend on sample orientation.
- Bone is stronger at the microscale (2.3 fold increase, similarly to compression).
- Strength anisotropy is much higher in tension than in compression.

Post-test analysis

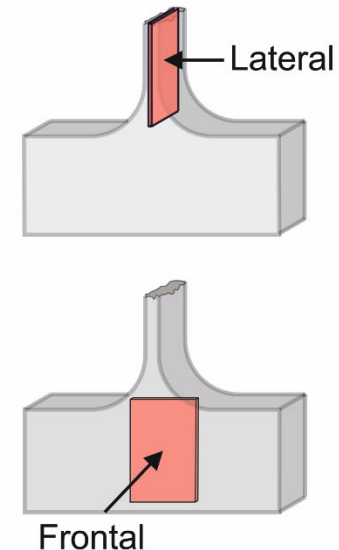


SEM



- + Quick, no further modification
- + Failure information
- Only surface information

STEM

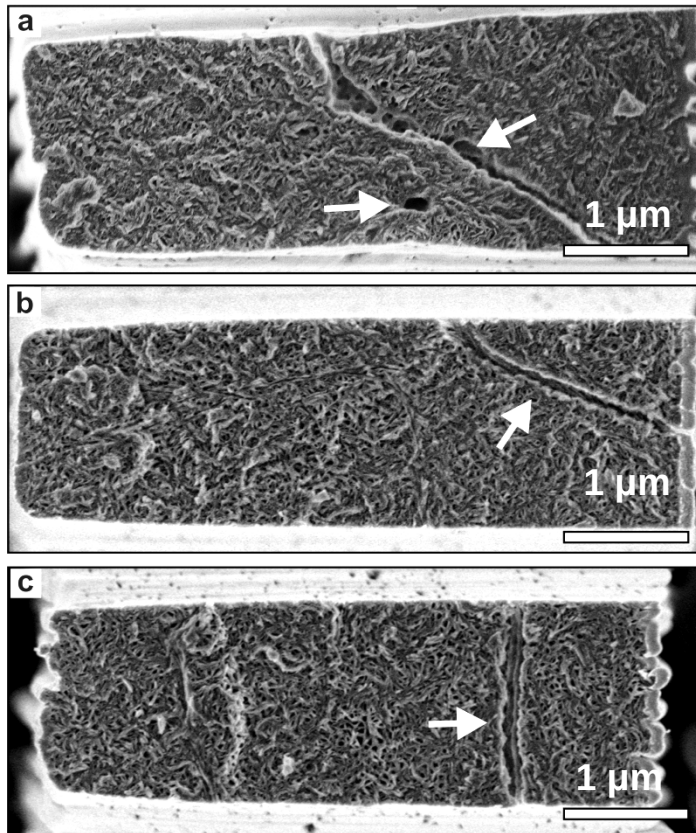


- Tedious process
- Information on 200 nm in thickness
- + Crack dynamics (lateral section)
- + Microstructure (MCF organization)

Failure mode: fracture surfaces

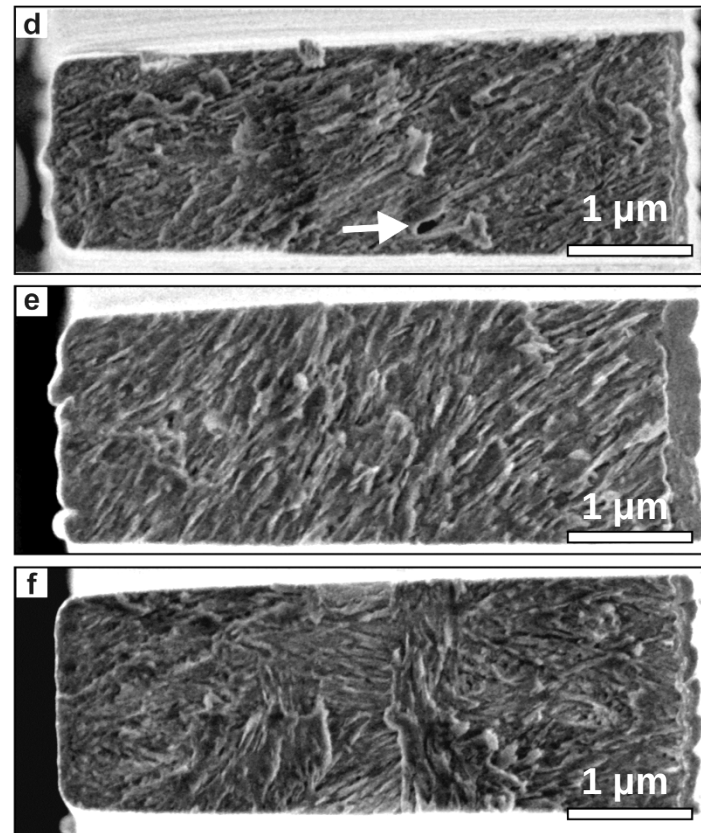
Contrarily to compression, **change in failure mode** between axial and transverse direction.
→ increase in strength anisotropy compared to compression.

Axial fracture (top view)



fibril-matrix **interfacial shearing**

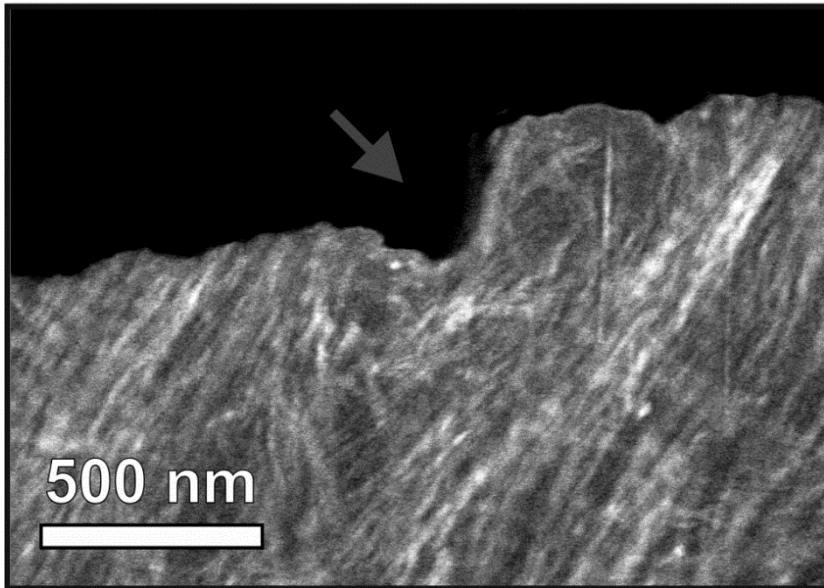
Transverse fracture (top view)



fibril-matrix **tensile debonding**

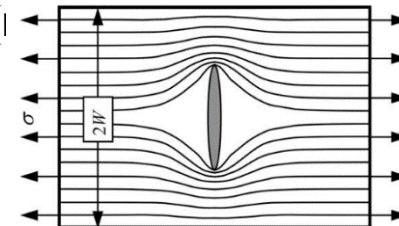
Axial specimens failure (STEM)

Canaliculi: stress concentrators



- ❑ Canaliculi act as **stress concentrators**.
- ❑ Oriented at high angles vs loading direction
- ❑ Fracture toughness (LEFM): $K_{IC} = 0.17 \pm 0.03 \text{ MPa}(\text{m})^{1/2}$
1 order of magnitude **smaller than macroscale**.

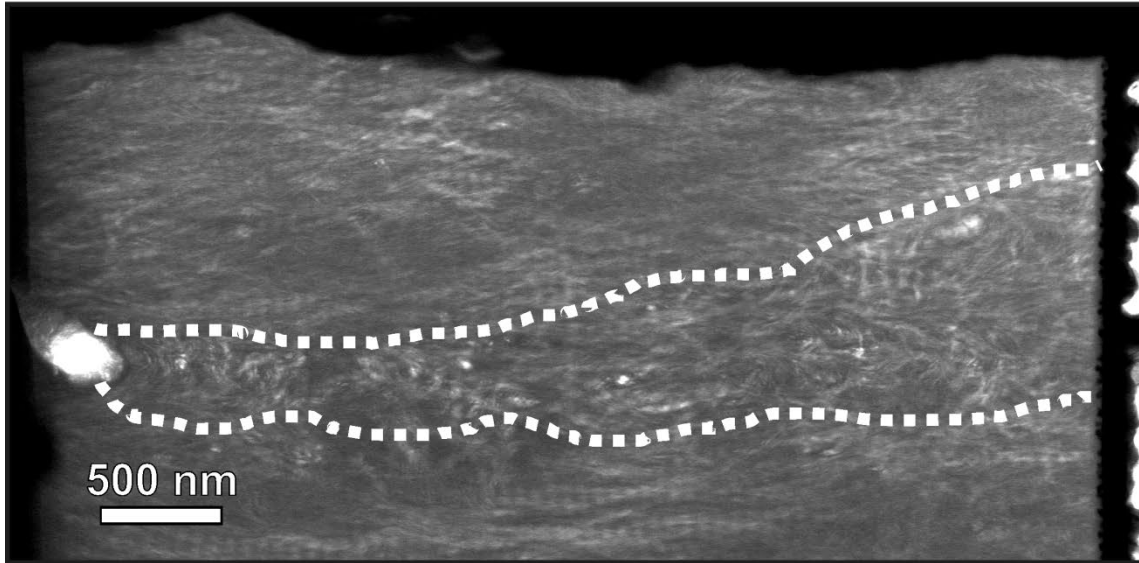
$$K_I = \sigma \sqrt{\pi a} \left[\sec\left(\frac{\pi a}{2W}\right)^{1/2} \right] \left[1 - 0.025 \left(\frac{a}{W}\right)^2 + 0.06 \left(\frac{a}{W}\right)^4 \right]$$



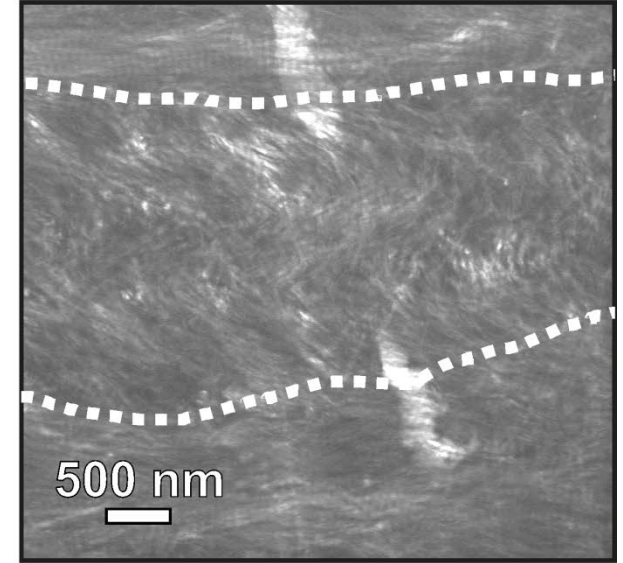
T.L. Anderson, Fracture Mechanics: Fundamentals and Applications, CRC Press 3rd ed. (2005)

Transverse specimens failure (STEM)

Fractured specimen



Undeformed volume



- ❑ Crack always perpendicular to loading direction ($<3^\circ$) even without canaliculi (in 58% cases).
- ❑ Fracture toughness when **canaliculi** is present: $K_{IC} = 0.07 \pm 0.01 \text{ MPa(m)}^{1/2}$
- ❑ The **disordered phases** act as **weak interfaces** → crack deflection.
- ❑ These weak interfaces are not resulting from the tests, but are present in the material.

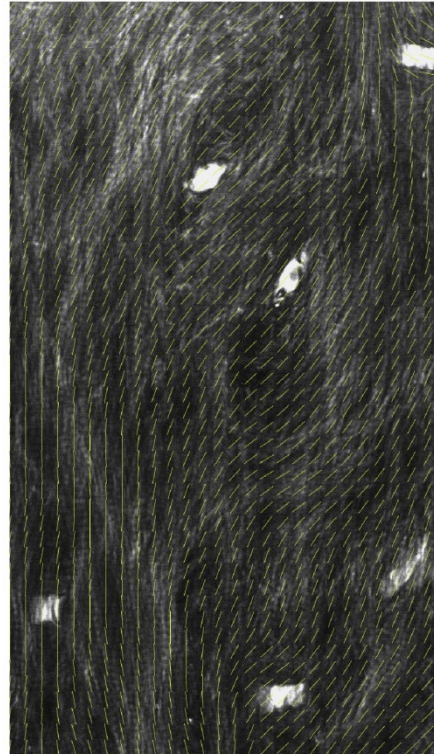
MCF orientation (STEM + ImageJ)

Can we correlate **MCF orientation** and distribution with bone strength?

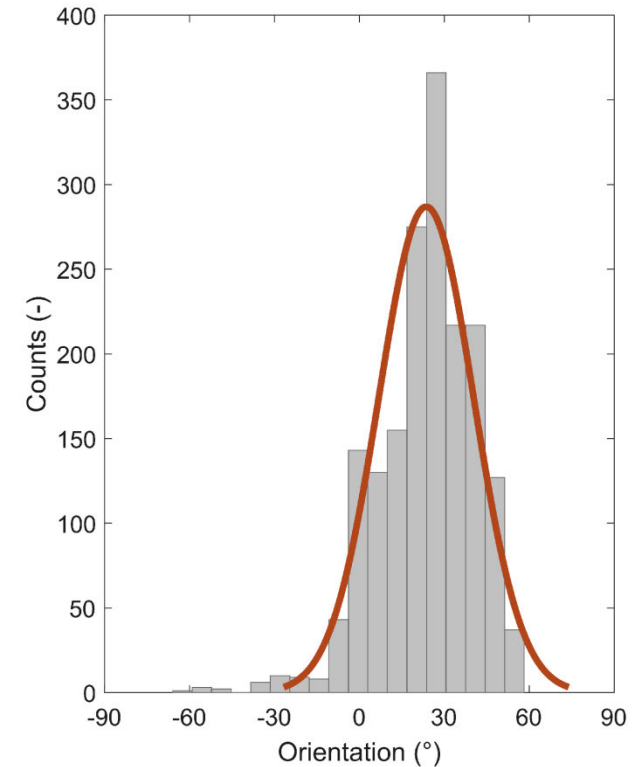
Region of interest



Vector Field (OrientationJ)



Normal distribution



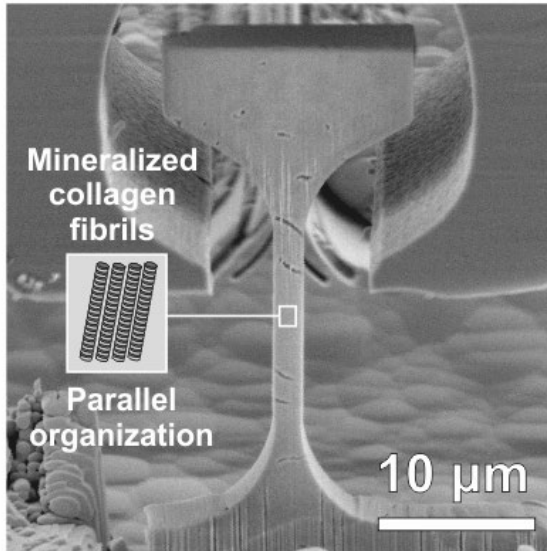
Finite difference gradient over Gaussian window of 150 nm (since banding pattern 67 nm).

ImageJ (NIH, Bethesda, Maryland, USA).

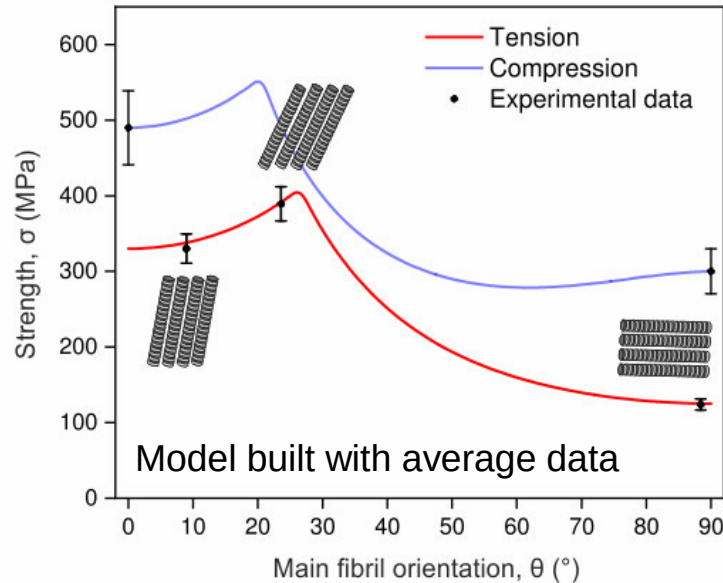
OrientationJ plugin (Biomedical Imaging Group, EPFL, Switzerland, <http://bigwww.epfl.ch/demo/orientation/>)

Single lamella: orientation vs. strength

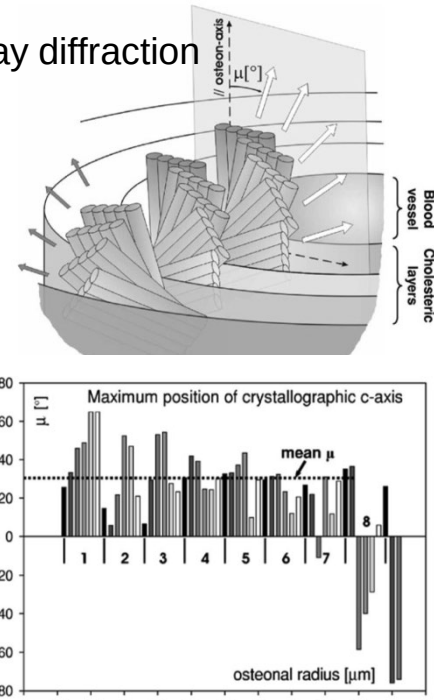
Uniaxial microtensile



Composite failure model



X-ray diffraction



Wagermaier et al. *Biointerphases* 2006.

- ❑ Hashin based composite failure model + mechanical and STEM data.

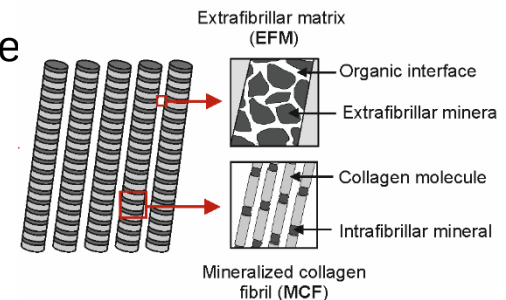
Gu et al. *Compos. Struct.*

(2017)

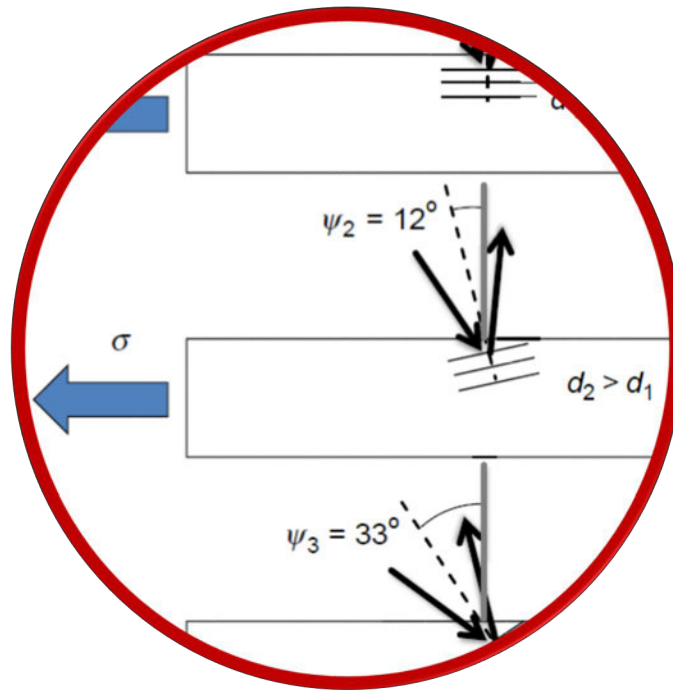
- ❑ Predicts **counterintuitive behavior** yet agreement with experiment

- ❑ High mineral content in the EFM $\rightarrow$ **high shear strength**

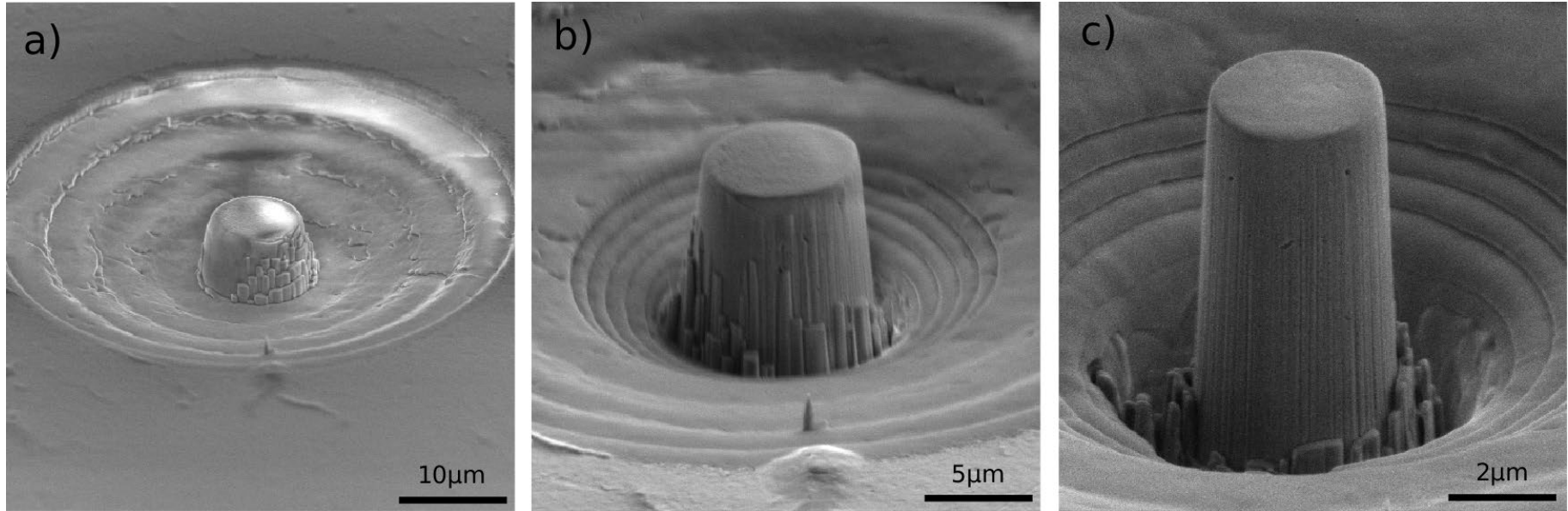
- ❑ High **tolerance** with respect to MCF main orientation.



Microcompression testing

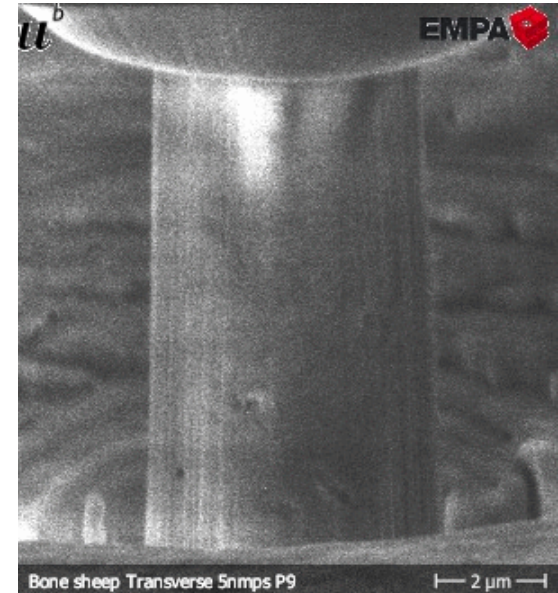
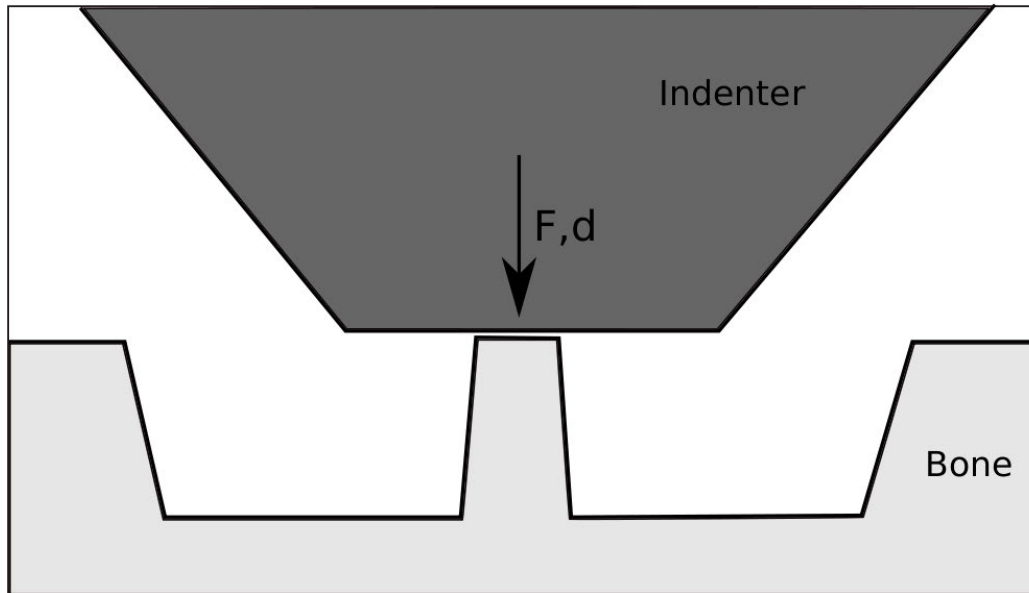


Micropillar Compression



- Micropillars machined using focused ion beam
- Compression with flat punch diamond indenter
- Uniaxial stress state → straightforward interpretation

Micropillar Compression

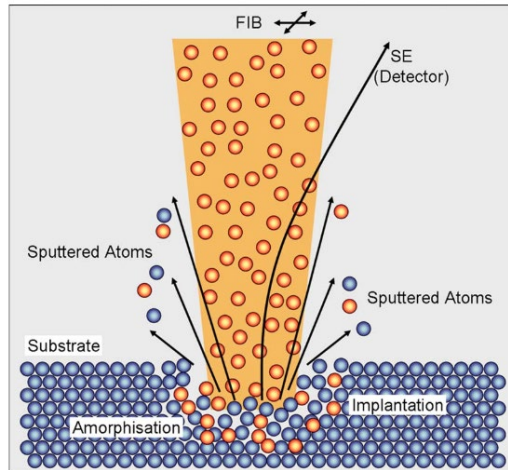


Schwiedrzik et al., Nat. Mat. (2014)

- Micropillars machined using focused ion beam
- Compression with flat punch diamond indenter
- Uniaxial stress state → straightforward interpretation

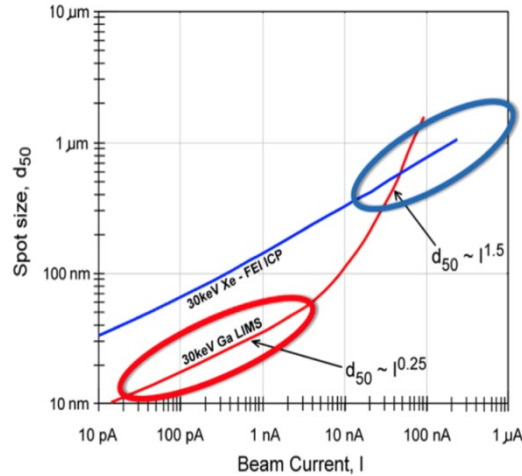
Micropillar compression (and analysis)

Focused ion beam (FIB) milling



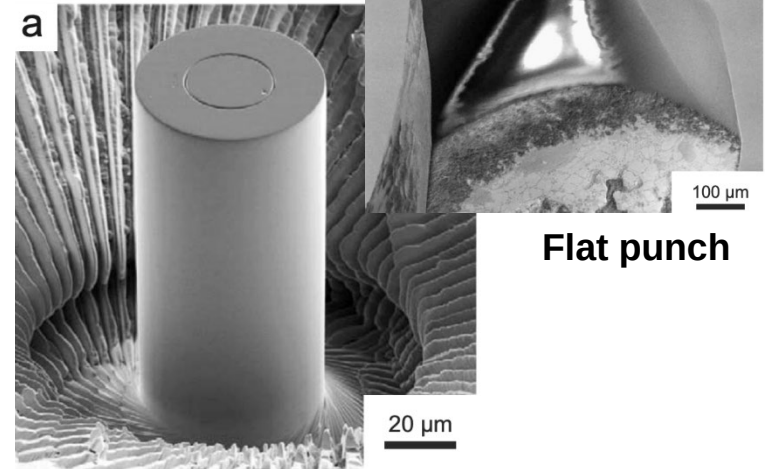
Utke et al. *J. Vac. Sci. Technol. B* (2008)

Different types of FIB



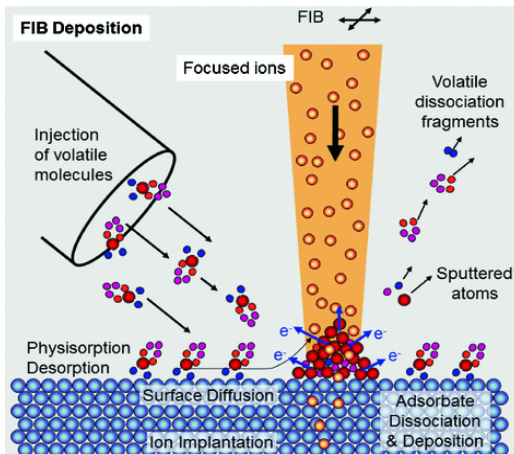
Smith et al. *J. Vac. Sci. Technol. B* (2006)

Compression sample



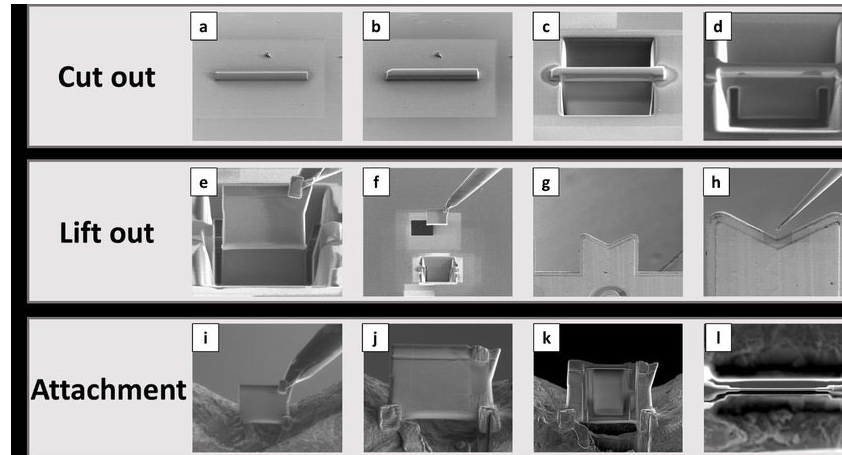
Uchic et al. *Science* (2004)

FIB induced deposition



Shorubalko et al. *Helium Ion Microscopy*, Springer (2016)

Transmission electron microscopy (TEM) lamella preparation



Abed, MSc thesis, University of Toronto (2007)

Micropillar

Compression

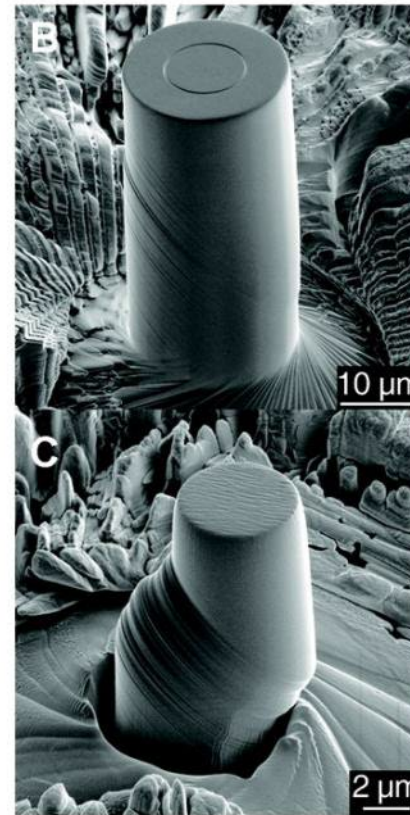
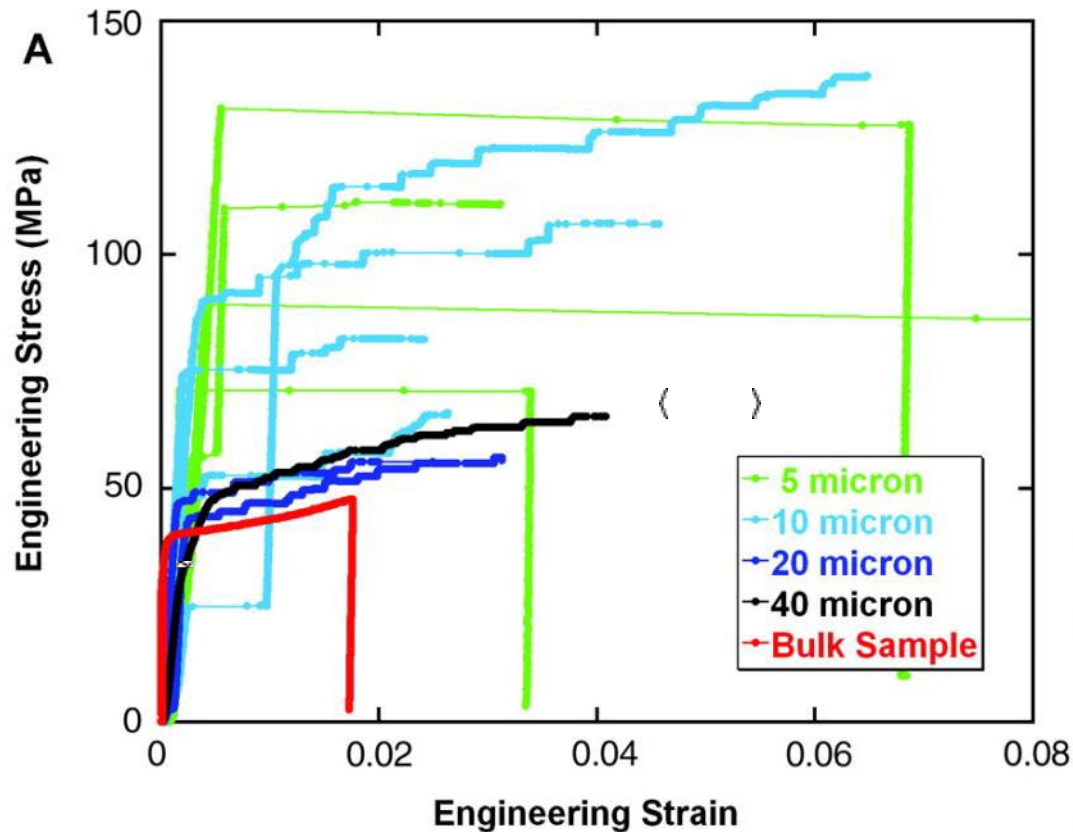
Straightforward
Post-yield behaviour

TEM

Microstructure
Deformation mechanisms

**Powerful
combination for
micro-nanoscale**

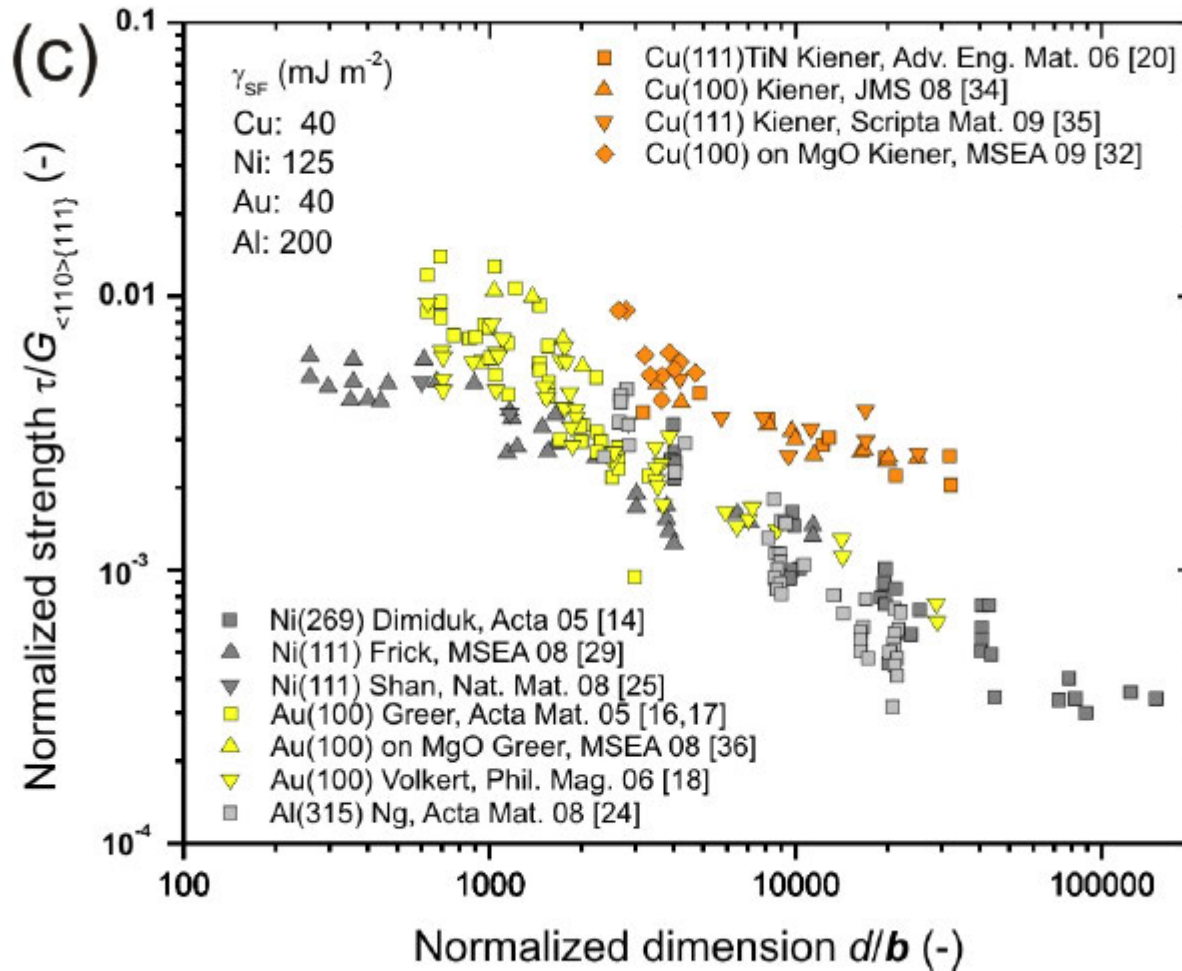
Micro compression tests



MD Uchic, DM Dimiduk, JN Florando, WD Nix (2004) Sample dimensions influence strength and crystal plasticity, *SCIENCE* 305, 986-989

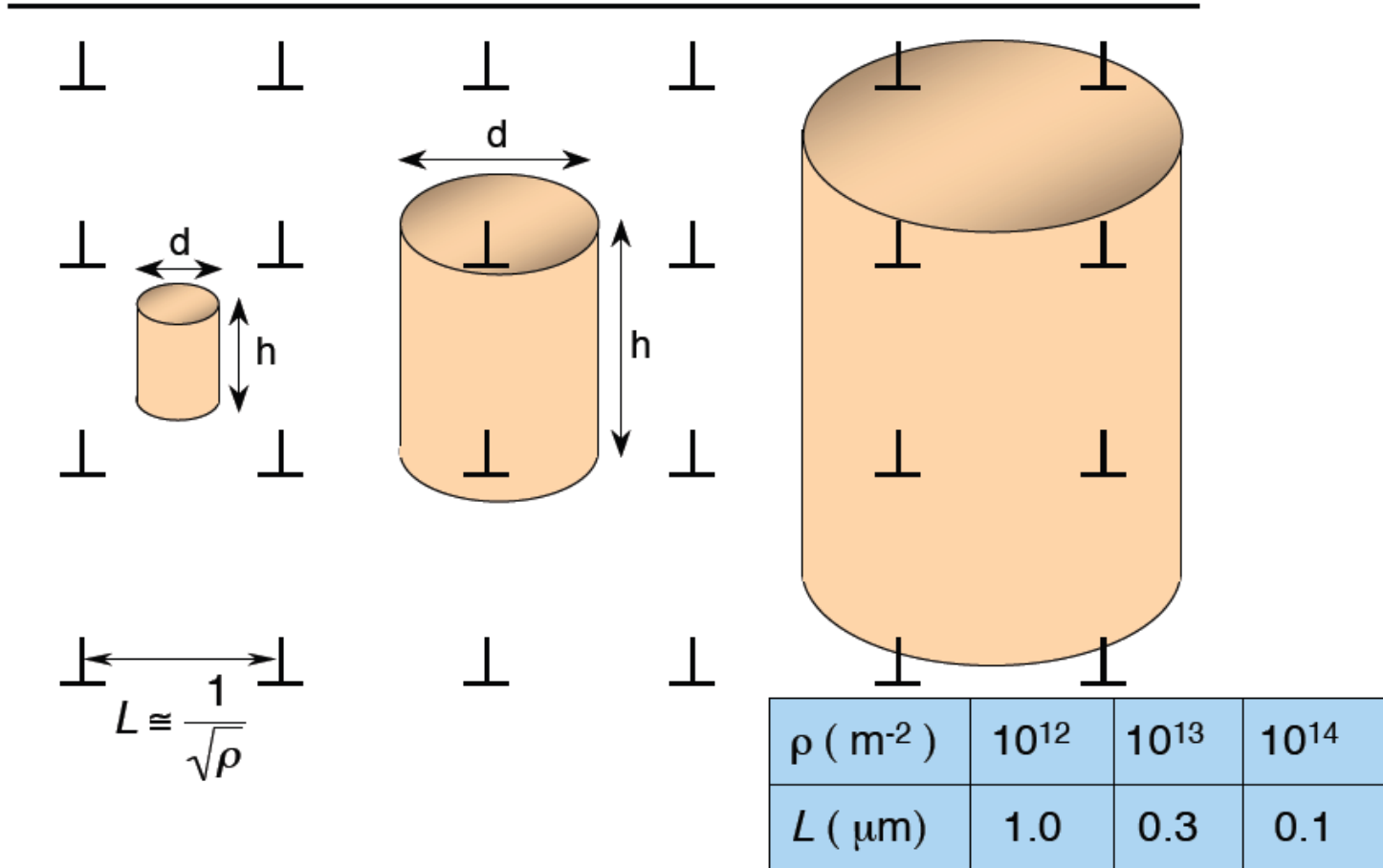
Smaller is stronger

Smaller is stronger



Kiener D, Motz C, Dehm G, Pippan R. *Int. J. Mat. Res.* 2009;100.

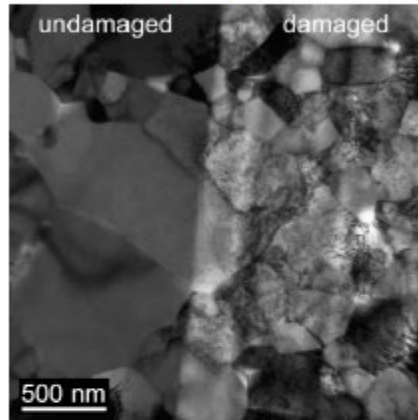
Micro compression tests



Extrinsic influences of FIB milling on pillar strength

Kiener et al, *Mater. Sci. Eng. A* 459, 262 (2007)

TEM of polycrystalline Cu



Important parameters

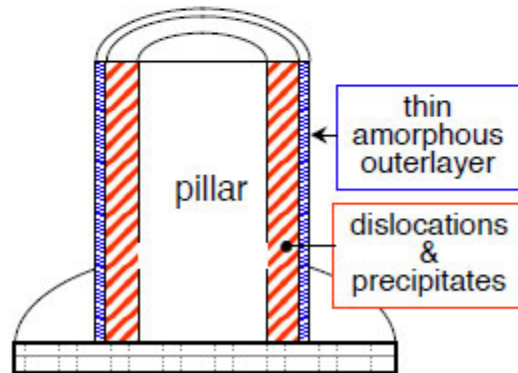
- beam incidence (normal/grazing)
- accelerating voltage (5–30 kV)
- current (10–2000 pA)

Strengthening mechanisms

- hard amorphous film formation
- dislocations
- precipitation

Conclusions

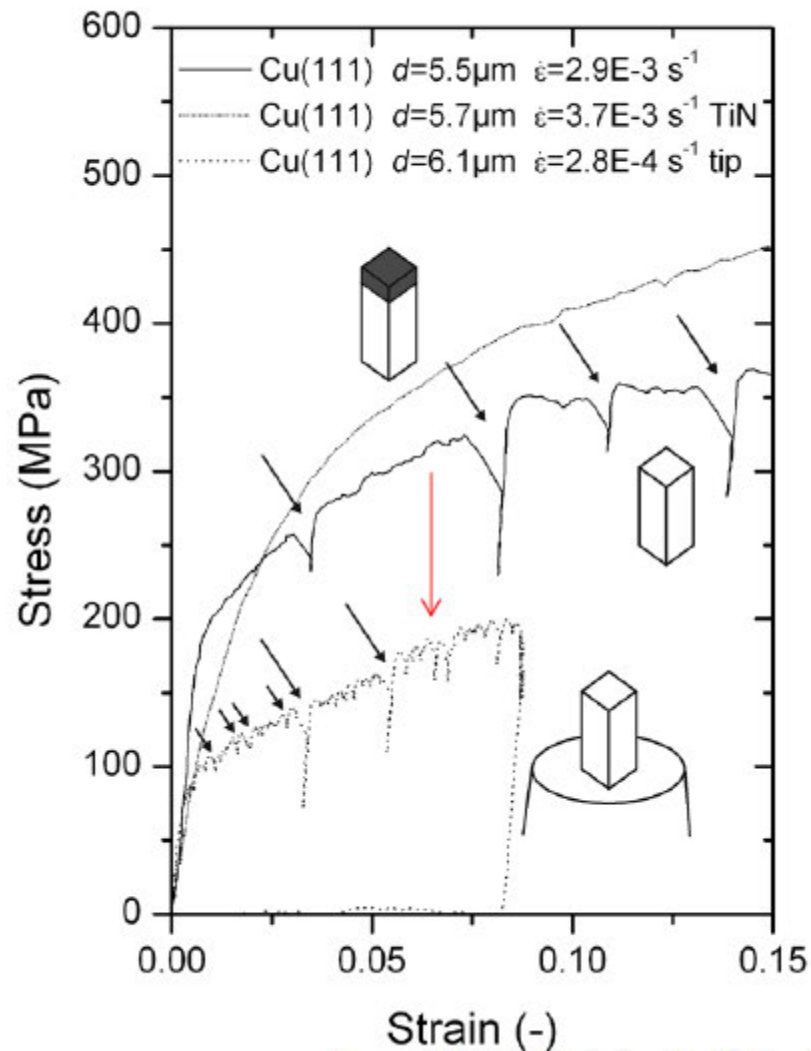
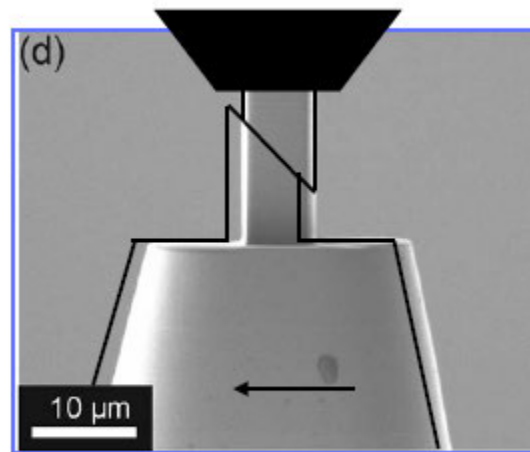
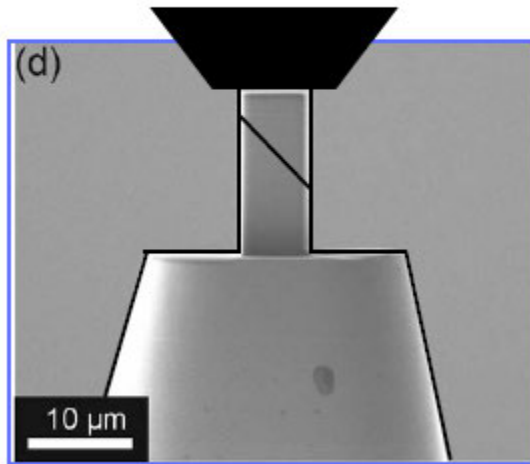
- FIB damage reduced at smaller accelerating voltages & grazing incidence
- even for grazing incidence, effects on strength may be significant for submicron pillars



20

Influence of lateral stiffness

Micro-compression of a **Cu(100)** sample with reduced lateral stiffness



Kiener D, Motz C, Dehm G. Mater. Sci. Eng. A 2009;505:79.

the pain with the strain (-measurement)

Comparison of Modulus values from 200°C,
6.8μm diameter pillar with various corrections:

- Indenter frame compliance
- Pillar sink-in into substrate
- Correction for fillet on pillar base
- Correction for contact thermal drift
- Effective modulus correction using high temperature indenter modulus

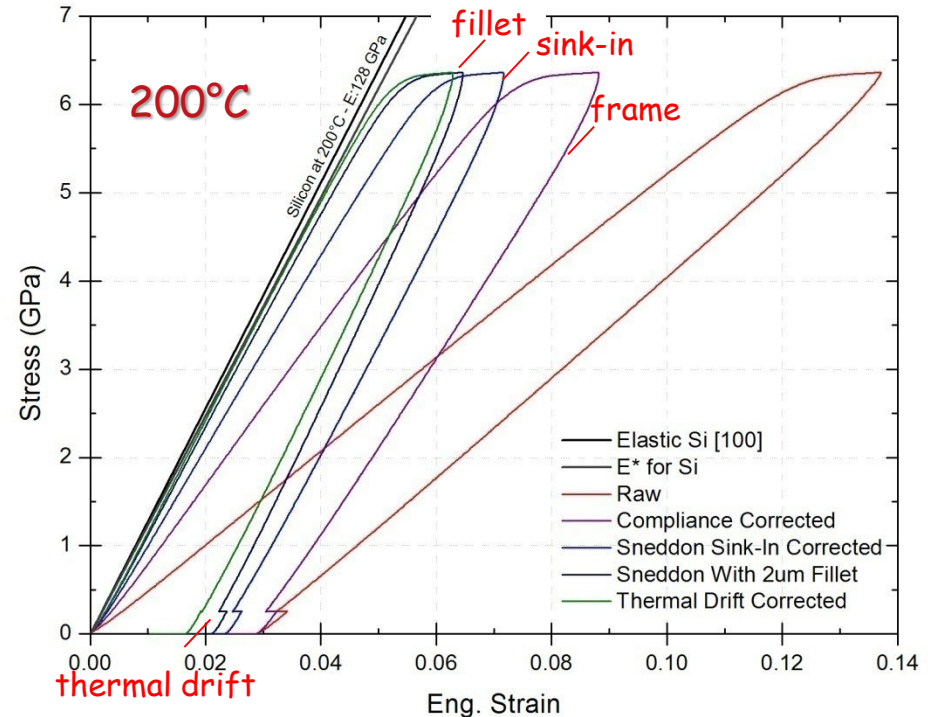
$$\frac{D_{\text{Sink-In}}}{D_{\text{Total}}} = \left(1 + \frac{2}{\pi(1-\nu^2)} \left(\frac{h}{a_c} \right) \right)^{-1}$$

$$a_c = \eta(r_{\text{pillar}} + r_{\text{fillet}})$$

(60 second, constant-load hold period at
1/20th of maximum load during unloading)

$$E^* = \left(\frac{1-\nu_i^2}{E_i} + \frac{1-\nu_s^2}{E_s} \right)^{-1}$$

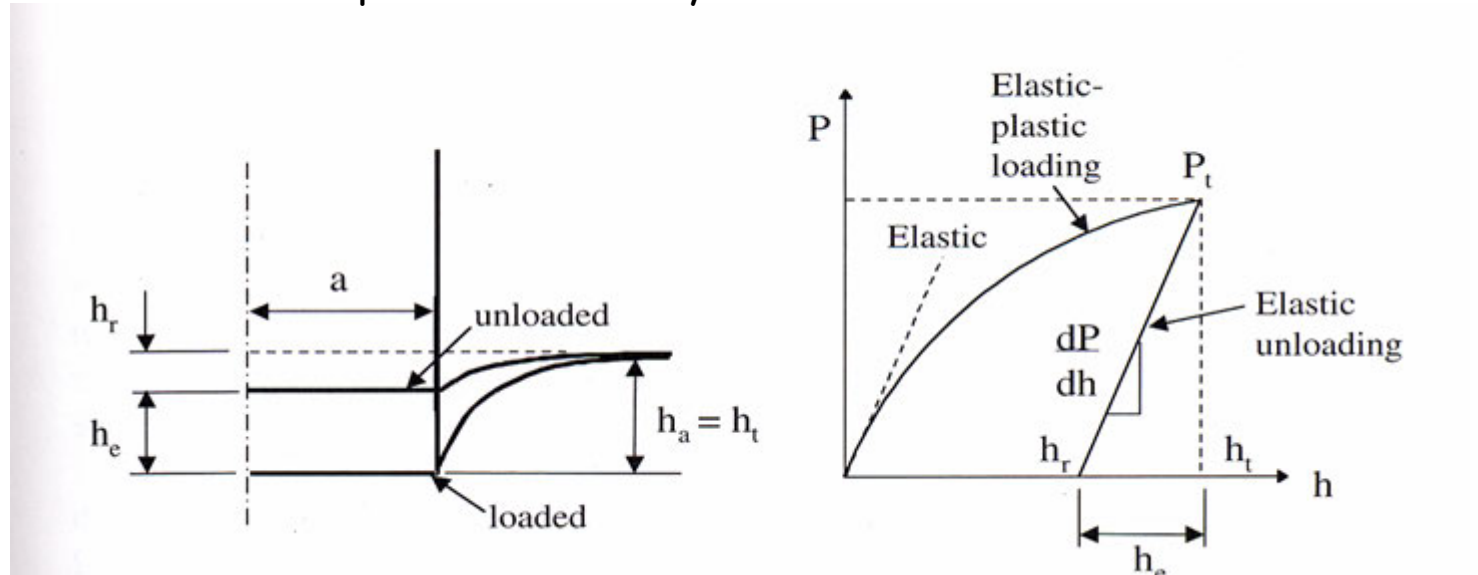
Values converge towards ideal single crystal
[100] value. Micro-pillars are not an ideal
geometry for Young's modulus measurements,
but it is possible.



Alternative: Digital image correlation

"Flat Punch"-Model

Elastic-plastic contact cylinder on flat



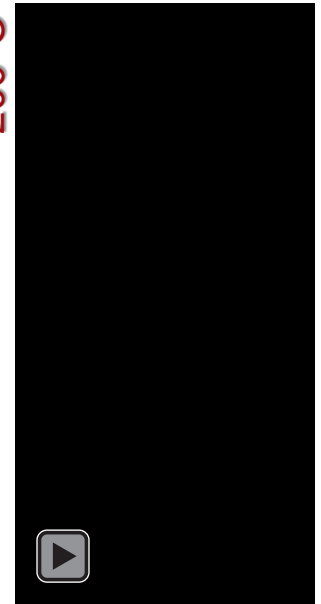
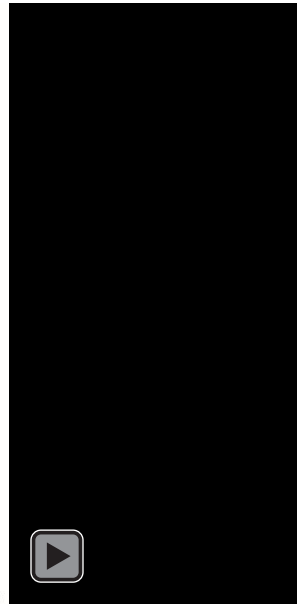
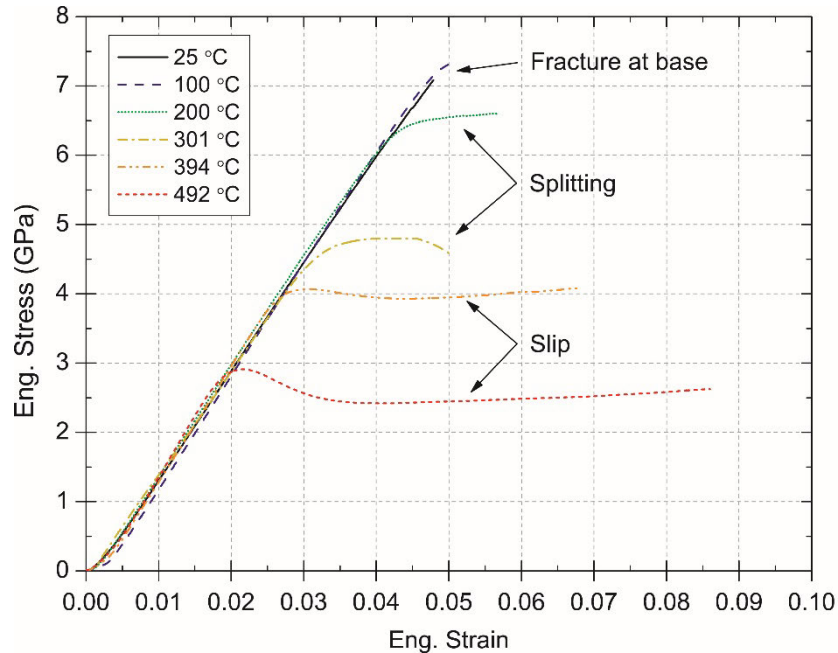
In elastic case:

$$\frac{dP}{dh} = 2aE_r = 2E_r \frac{\sqrt{A}}{\pi}$$

i.e. Young's modulus can be derived from slope of unloading curve:

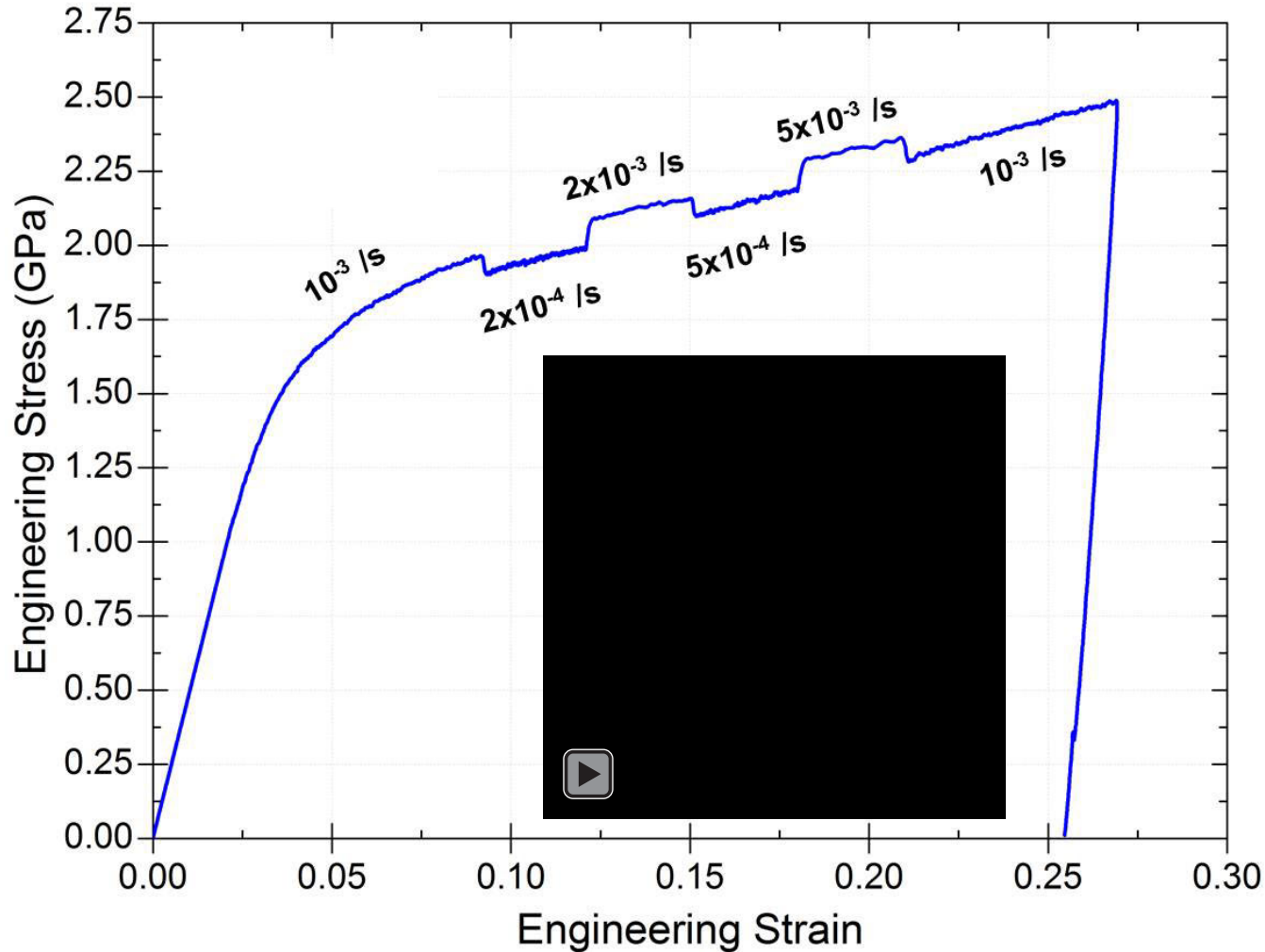
$$E_r = \frac{dP}{dh} \frac{\pi}{2\sqrt{A}}$$

Example: microcompression of silicon <001>



- Transitions between in deformation mechanisms between fracture, splitting, and plasticity directly observed.
- At a diameter of 6.7 μm , the brittle-ductile transition is seen at $\sim 400^\circ\text{C}$ - significantly lower than bulk silicon.
- Classic upper yield point consistent with dislocation nucleation observed during plastic deformation due to system's intrinsic displacement control.

strain rate jump tests



the strain rate
sensitivity exponent

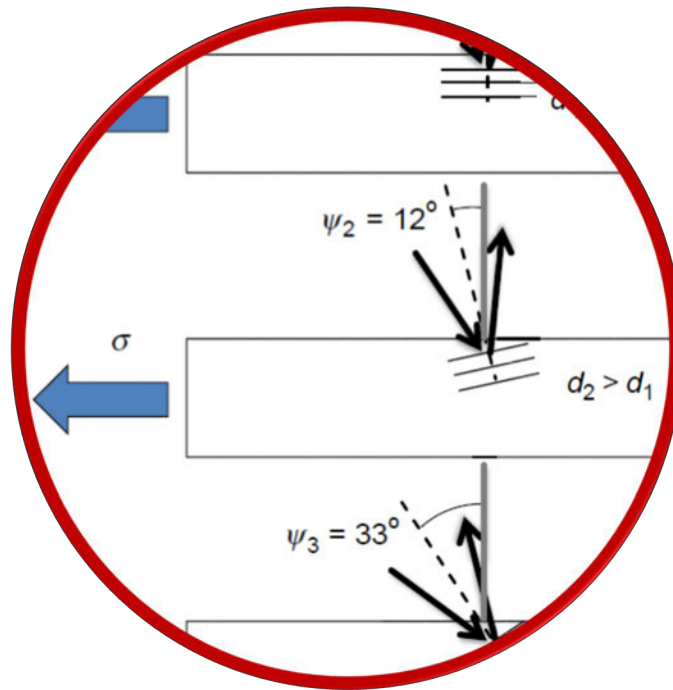
$$m = \frac{d(\ln \sigma_f)}{d(\ln \dot{\epsilon})}$$

the activation volume

$$V = \frac{\sqrt{3}k_B T}{m \cdot \sigma_f}$$

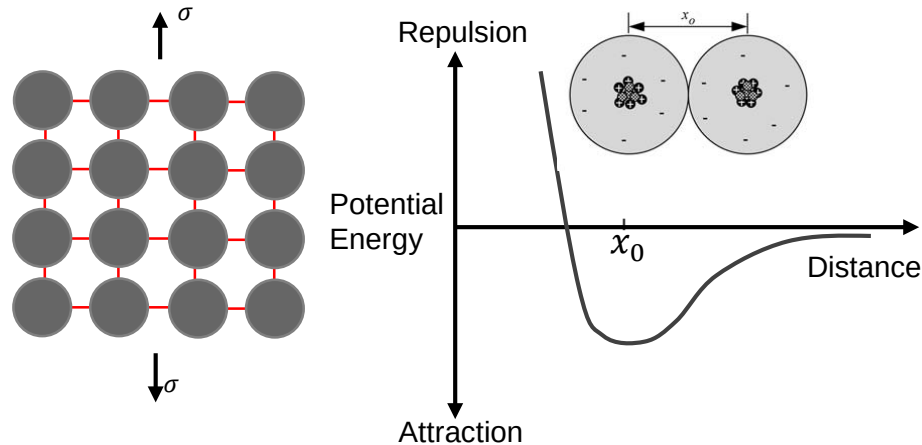
strain rate jump tests are straightforward to perform using a displacement control.
strain rate sensitivity values are obtained by linear extrapolation to the elastic limit.

Microscale fracture testing



Why fracture mechanics?

Ideal

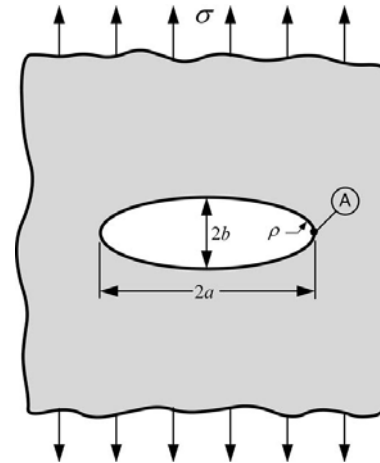


- Perfect material
- σ equal to cohesive stress σ_c to break bonds

Theoretical fracture stress:

$$\sigma_f = \sigma_c \approx \frac{E}{\pi}$$

Real



Sources of flaws:

Casting;
Particle decohesion;
Plastic deformation
...

- Material with flaw
- Stress concentration at flaws
- σ much smaller than σ_c

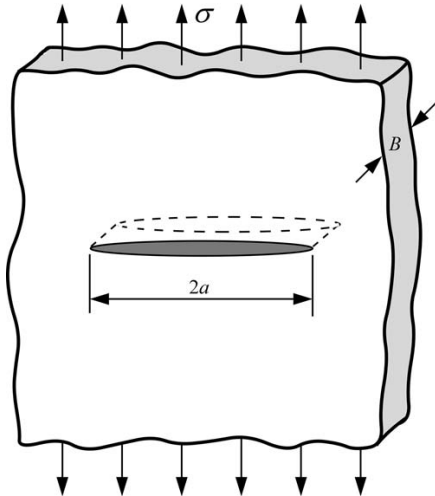
Fracture stress with a flaw:

$$\sigma_f \approx \sigma_c \cdot \sqrt{\frac{x_0}{4a}} \quad \begin{matrix} \sim 10^{-10}m \\ \sim 10^{-6}m \end{matrix} \quad \sim 0.01\sigma_c$$

Study the material resistance to preexisting crack propagation

Two ways to understand fracture toughness

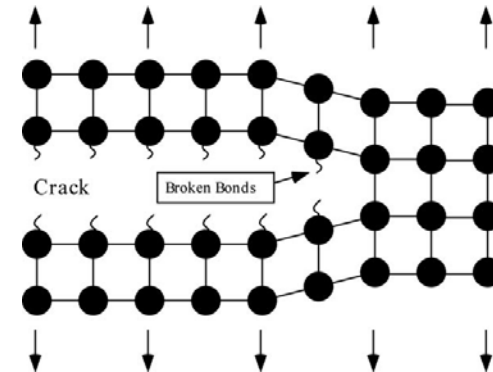
➤ Energy balance: G



Crack can only grow when this process causes the total energy to decrease or remain constant.

Unit: J/m^2 $-\frac{d\Pi}{dA} \geq 2\gamma_s$

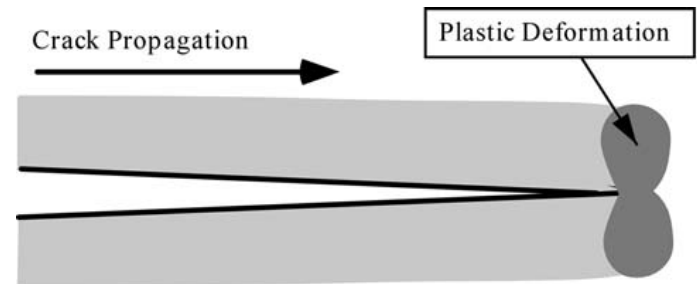
$-\frac{d\Pi}{dA} = G$ energy release rate;



Griffith's theory

*Ideal elastic brittle material

$$G_c = 2\gamma_s$$



Irwin and Orowan theory

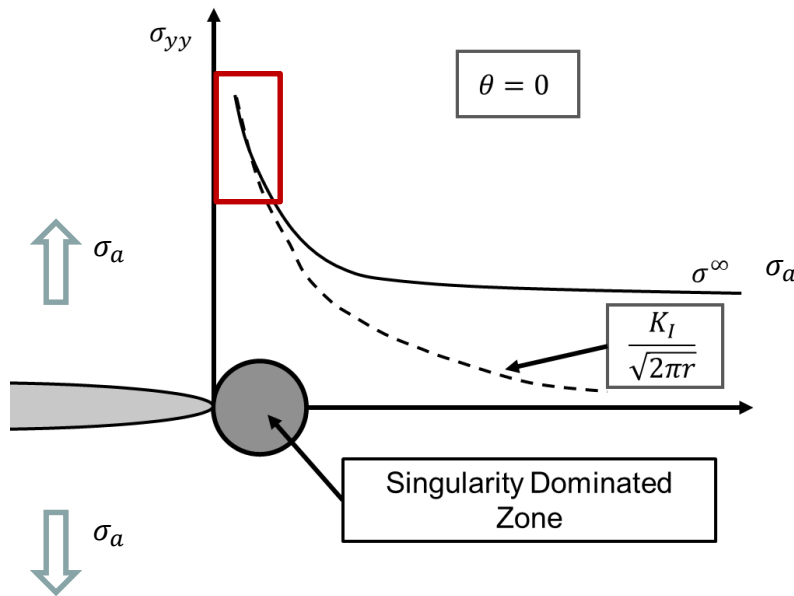
*Metals with plastic zone

$$G_c = 2(\gamma_s + \gamma_p)$$

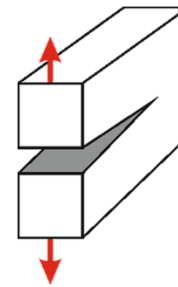
Two ways to understand fracture toughness

➤ Stress distribution: K & J

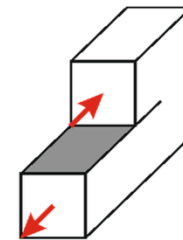
Linear elastic material:



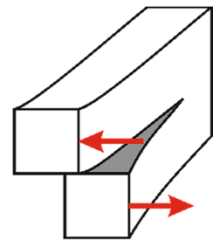
$$\sigma_{ij}(r, \theta) = \frac{K_{I,II,III}}{\sqrt{2\pi r}} f_{ij}(\theta)$$



Mode I
Opening



Mode II
Sliding

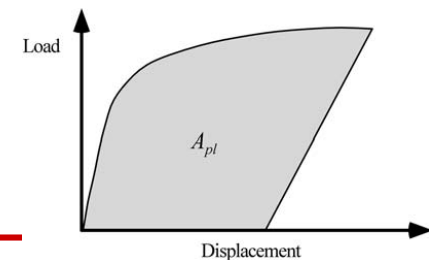


Mode III
Tearing

Elastic Plastic Material:

$$\sigma_{ij}(r, \theta) = c \left(\frac{J}{r} \right)^{\frac{1}{1+n}} s_{ij}(\theta)$$

$$J_{pl} = \frac{\eta A_{pl}}{B b_0}$$

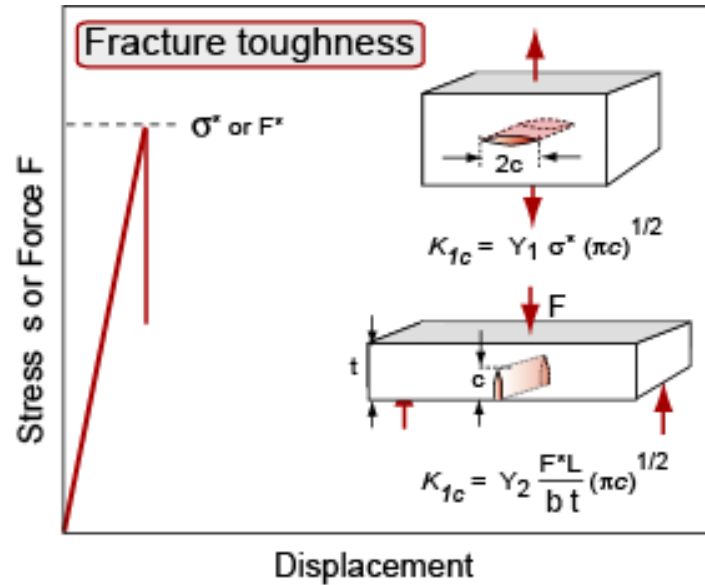


$K_{I,II,III}$: stress intensity factor

Unit: $\text{MPa} \cdot \text{m}^{0.5}$

Unit: J/m^2

Two ways to understand fracture toughness



Definition:

Fracture toughness

$$K_{Ic} = Y_1 \sigma^* \sqrt{\pi c}$$

Plane stress: $E' = E;$

Fracture energy or toughness

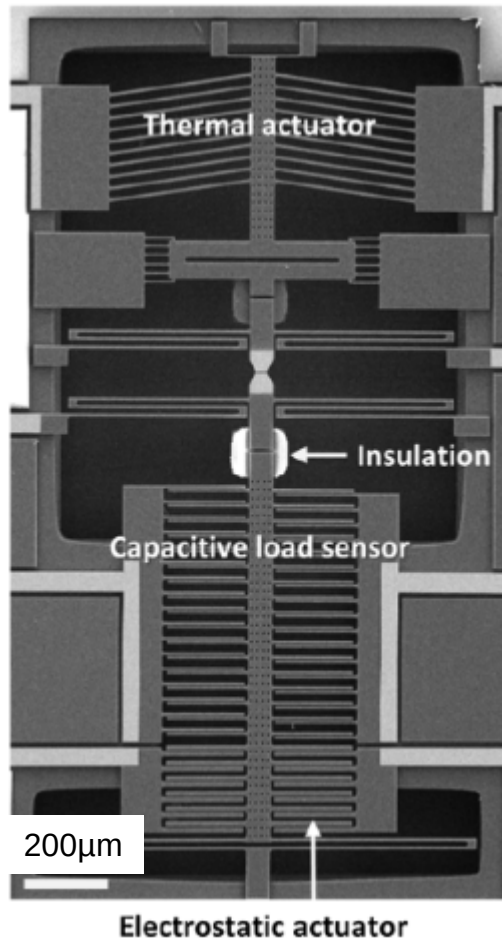
$$G = \frac{K_c^2}{E}$$

Plane strain: $E' = \frac{E}{1 - \nu^2}$

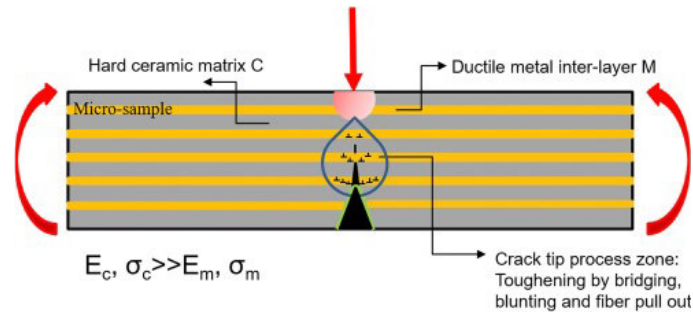
Range of fracture toughness:

0.3 MPa m^{1/2} (glass) to 200 MPa m^{1/2} GPa (steel)

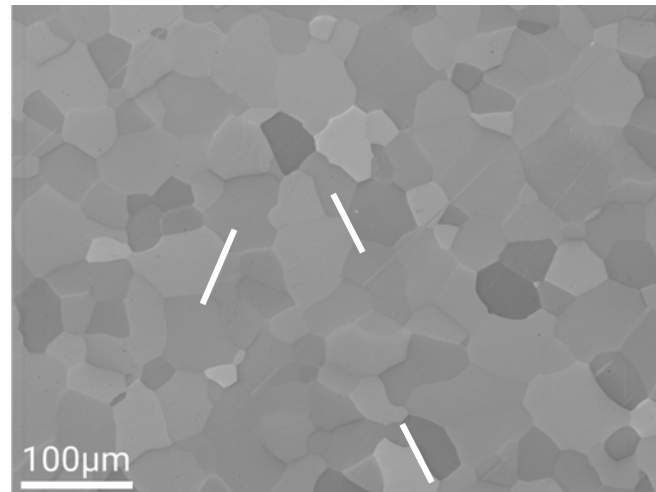
Why microscale fracture testing?



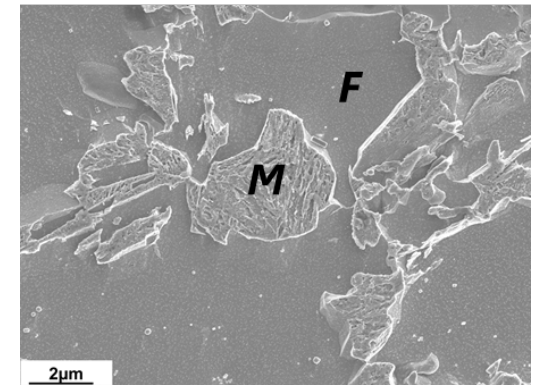
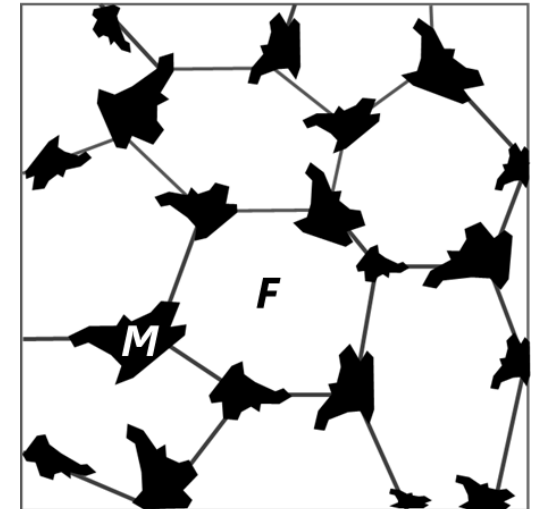
MEMS actuator/sensor



Thin film coating



Interface/boundary brittleness



Damage sensitive phase